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NMR STUDY OF MAGNETIC SUPERCONDUCTOR

$\text{RERh}_4\text{B}_4$  ( RE = Rare Earth )

Yoh Kohori

February 1984

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## ABSTRACT

Pulsed NMR study has been performed in  $\text{RERh}_4\text{B}_4$  (RE = rare earth) to understand the magnetic and superconducting property of the compound microscopically.

The nuclear spin lattice relaxation time  $T_1$  of  $^{89}\text{Y}$ ,  $^{103}\text{Rh}$  and  $^{11}\text{B}$  have been measured in non-magnetic  $\text{YRh}_4\text{B}_4$  and  $\text{LuRh}_4\text{B}_4$  in order to investigate the density of states at each atomic site in  $\text{RERh}_4\text{B}_4$ . The observed  $T_1^{-1}$ 's are compared with the value that are obtained by using the calculated density of states for  $\text{RERh}_4\text{B}_4$ . The agreement of the experimental results with the band calculation is satisfactory for Y(RE) and Rh site. Considerable reduction of the density of states at RE site has been observed. This reduction is responsible for the weak coupling of RE spin and the superconducting electron at  $\text{Rh}_4\text{B}_4$  cluster.

In  $\text{RERh}_4\text{B}_4$  with RE of magnetic ion, Knight shift of  $^{11}\text{B}$  has been measured. The isotropic Knight shift is proportional to  $(g_J-1)J$  for all  $\text{RERh}_4\text{B}_4$ . This means that the conduction electron spin polarization induced by unit RE spin is nearly the same for all  $\text{RERh}_4\text{B}_4$ .

The isotropic Knight shift of  $^{103}\text{Rh}$  was measured in  $\text{SmRh}_4\text{B}_4$ . From the shift data, the conduction electron spin polarization at Rh site is estimated. The obtained value is by one order of magnitude larger than that in Chevrel phase compound.

From  $T_1$  of  $^{11}\text{B}$  in  $\text{RERh}_4\text{B}_4$ , the s-f and/or d-f exchange interaction at RE site have been obtained from the Korringa spin fluctuation of RE spin. The obtained values are by one order of magnitude larger than those found in Chevrel phase compound. This means that s-f exchange interaction play an important role in  $\text{RERh}_4\text{B}_4$  than in Chevrel phase compound.

The crystal field effect on RE ion has been obtained from  $T_1$ . For Dy based compound, the first excited state of  $J_z$  is 130 K above the ground state. This energy spacing is much larger than the exchange interaction between RE ions, then the magnetic properties are much affected by the crystal field effect.

In non-magnetic superconductor  $\text{LuRh}_4\text{B}_4$ , the superconducting energy gap at B site was obtained from  $T_1$  of  $^{11}\text{B}$ . The ratio of the energy gap to the superconducting critical temperature was found to be that of a weak coupling superconductor:  $2\Delta(0)/k_B T_c = 3.5$ .

In antiferromagnetic superconductor  $\text{SmRh}_4\text{B}_4$ ,  $T_1$  was measured both in the normal antiferromagnetic state ( 2.9 kOe ) and in the superconducting antiferromagnetic state ( 790 Oe ). Below 0.3 K,  $T_1$  is proportional to  $T^{-1}$  in the normal state. This means the Weger mechanism governs  $T_1$  of  $^{11}\text{B}$  at low temperature. The nuclear Zeeman energy of  $^{11}\text{B}$  relaxes to the conduction electron band at Sm site. There is no difference between  $T_1$  in the normal state and the superconducting state above 790 Oe. This means Sm site is in gapless or nearly gapless state in this magnetic field.

We observed the zero field NMR of  $^{11}\text{B}$  in  $\text{Dy}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$  and  $\text{Ho}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$ . In Dy-based compound, we found the occurrence of the long range antiferromagnetic ordering above the superconducting transition temperature. The magnetic structure in Dy-based compound is considered to be the same as in Ho-based compound.

## §1 Introduction

In recent years, several ternary compound systems have been discovered which contain large amounts of magnetic ions at regular lattice sites.<sup>1)</sup> Among the ternary compound systems, the crystal structure of two rare-earth ternary compounds,  $\text{REMo}_6(\text{S,Se})_8$  and  $\text{RERh}_4\text{B}_4$  attract much interest.<sup>2,3)</sup> The superconductivity and the long range magnetic order often occur simultaneously in these compounds. As for  $\text{RERh}_4\text{B}_4$ , the superconductivity appears for  $\text{RE} = \text{Y, Lu, Sm, Nd, Er}$  and  $\text{Tm}$ .<sup>3)</sup> In Er based compound the superconductivity occurs at high temperature and is destroyed by the long range ferromagnetic order at low temperature.<sup>3)</sup> In Sm, Nd and Tm based compound, however, superconductivity occurs at high temperature and coexists with antiferromagnetic long range order at low temperature.<sup>3)</sup> In these compounds the superconducting transition temperature is higher than the magnetic transition temperature. The magnetic structure of Er, Nd and Tm based compound are determined by neutron diffraction measurement.<sup>3,4)</sup> Gd, Tb, Dy and Ho based compounds exhibit only ferromagnetic order and superconductivity does not appear.<sup>3)</sup> The coexistence of antiferromagnetic order and superconductivity is also proposed in  $\text{Dy}(\text{Ir}_x\text{Rh}_{1-x})_4\text{B}_4$  and  $\text{Ho}(\text{Ir}_x\text{Rh}_{1-x})_4\text{B}_4$ , with  $0.5 < x < 0.8$ .<sup>5,6)</sup> In these compounds, the magnetic ordering temperature is higher than the superconducting transition temperature. The magnetic structure of Ho based compound is confirmed,<sup>7)</sup> while that of Dy based compound is not yet understood.

In these compounds the superconductivity is considered to be carried by  $\text{Rh}_4\text{B}_4$  cluster, while the magnetism is carried by RE atoms. The exchange interaction between RE magnetic moment and the conduction electron is considered to be small. Jarlborg et al. have carried out the band calculation and obtained the density of states at each atomic site.<sup>8)</sup> The density

of states at RE site is responsible for the coupling of RE spin and the superconducting electrons, while that at Rh site is responsible for the condensation energy of the superconductivity. Jarlborg et al. attributed the relatively small density of states at RE site to the coexistence of magnetic order and superconductivity. It is necessary to investigate the result of band calculation experimentally. It is also important to know the magnitude of exchange interaction between 4f-electron of RE ion and the conduction electron, which yields the exchange field on the superconducting electron.

The  $\text{RERh}_4\text{B}_4$  compounds exhibit complex magnetic properties. For example, Dy compound has the highest  $T_m$  in the series of simple ferromagnetic compound from Gd to Ho.<sup>3)</sup> Shenoy interpreted this phenomenon by taking account the crystal field effect, assuming that the RKKY interaction is proportional to RE spin.<sup>9)</sup> It is necessary to confirm this assumption and also to estimate the magnitude of the conduction electron spin polarization for the understanding of the magnetic properties of  $\text{RERh}_4\text{B}_4$ .

Furthermore it is important to study the interplay of the superconductivity and the magnetism in coexistent state. The antiferromagnetic order coexists with the superconductivity in  $\text{RERh}_4\text{B}_4$ . The temperature dependence of upper critical field implies the reduction of pair breaking effect in the antiferromagnetic state. We intend to study how the superconducting energy gap is modified in antiferromagnetic superconductor. As s-f exchange scattering occurs at RE site, the energy gap may be much affected in RE site than in Rh site. It is therefore important to investigate the energy gap at each atomic site.

In this paper, NMR studies are performed to understand the above problem from the microscopic point of view. We intend to study the reason why the superconductivity and the magnetic order coexist in this compound.



Next we intend to know how the superconducting and magnetic property are modified in antiferromagnetic superconductor.

In order to study the coupling of RE moment and the superconducting electrons at  $\text{Rh}_4\text{B}_4$  cluster, we will investigate the density of states at each atomic site, the conduction electron spin polarization at Rh and B site and also the s-f and/or d-f exchange interaction between RE and the conduction electrons.

The density of states at each atomic site is evaluated from the nuclear spin lattice relaxation time  $T_1$  of respective nuclei.  $T_1$  is determined by the square of both hyperfine field and density of state. From  $T_1$  one can estimate the density of states at each site. Thus we shall measure  $T_1$  of  $^{89}\text{Y}$ ,  $^{103}\text{Rh}$  and  $^{11}\text{B}$  in non-magnetic compounds  $\text{YRh}_4\text{B}_4$  and  $\text{LuRh}_4\text{B}_4$ .

The exchange field on the superconducting electron and also the RE dependence of the magnitude of RKKY interaction are obtained from the conduction electron spin polarization, which yields an isotropic Knight shift in non-magnetic nuclear species in the paramagnetic state. We shall measure the Knight shift of  $^{103}\text{Rh}$  and  $^{11}\text{B}$  in  $\text{RERh}_4\text{B}_4$  and obtain information about the conduction electron spin polarization at Rh and B site.

The s-f and/or d-f exchange interaction between the 4f-electron of RE and the conduction electron yields the Korringa spin fluctuation of RE moment. The Korringa spin fluctuation of RE spin enhances  $T_1^{-1}$  of  $^{11}\text{B}$  through the magnetic dipole coupling and RKKY coupling between RE and  $^{11}\text{B}$ . Thus  $T_1$  of  $^{11}\text{B}$  provides informations about s-f exchange interaction at RE site.

The crystal field effect affects the RE spin fluctuation. Then we obtain an information about the crystal field effect from the analysis of  $T_1$ .

In order to determine the superconducting energy gap in antiferromagnetic superconductor, we shall measure  $T_1$  of  $^{11}\text{B}$  in  $\text{SmRh}_4\text{B}_4$  in antiferromagnetic and superconducting state. When  $T_1$  is governed by the relaxation to the conduction electrons,  $T_1$  is proportional to  $T^{-1}$  in the normal state and increases exponentially in superconducting state owing to the appearance of the superconducting energy gap in the conduction electron band. Hence from the measurement of  $T_1$ , one can confirm the appearance of superconductivity and obtain the magnitude of energy gap. Furthermore by the measurement on respective nuclei, we can determine the energy gap at each atomic site.

It is necessary to confirm the antiferromagnetic order of  $\text{Dy}(\text{Ir}_x\text{Rh}_{1-x})_4\text{B}_4$  and make similar investigation as in  $\text{SmRh}_4\text{B}_4$ , since more informations are expected to be available in Dy compound as the coexistence region in Dy compound is larger than in  $\text{SmRh}_4\text{B}_4$ .

## § 2 Experimental procedures

### 1) Sample preparations

The samples of  $\text{RERh}_4\text{B}_4$  were prepared by arc melting in an argon atmosphere. The starting elements were rare earth of 99.9% purity, Rh of 99.95% purity and B of 99.8% purity. Weight loss after melting was typically 1% in these compounds. The ingots were annealed at  $1100^\circ\text{C}$  for 7 days in a tantalum crucible under high vacuum. The ingot was crushed to powder ( about  $74\text{ }\mu\text{m}$  ) for the NMR and X-ray measurements. X-ray analysis showed that the sample formed the  $\text{CeCo}_4\text{B}_4$  structure.<sup>10)</sup>

### 2) $T_c$ measurements

The superconducting transition temperature was measured by susceptibility measurement ( Shawlow Devline method ).<sup>11)</sup>

### 3) $^4\text{He}$ cryostat and $^4\text{He}$ flow cryostat

Temperature between 1.2K and 4.2K was obtained by pumping liquid  $^4\text{He}$ . The temperature was determined by vapor pressure. Temperature above 4.2 K was achieved by passing helium gas over the sample. The temperature was determined by a thermo-couple junction placed near the sample.

### 4) $^3\text{He}$ cryostat

A cryostat used for NMR study at  $^3\text{He}$  temperature is of the single-cycle type. Figure illustrates the apparatus.  $^3\text{He}$  pot is made of Pb glass which does not contain B. As B in usual soda glass sometimes prevented our B NMR study, we used Pb glass for  $^3\text{He}$  pot.

Incoming  $^3\text{He}$  gas is liquified through a tube which is in thermal contact with a  $^4\text{He}$  bath( 1.45 K ), and liquid  $^3\text{He}$  enters  $^3\text{He}$  pot. Finally the  $^3\text{He}$  pot becomes filled with liquid and a temperature 0.45 K is achieved by pumping. The temperature was measured by carbon resistor in liquid  $^3\text{He}$ . The resistor was calibrated against the NMR intensity and  $T_1$  of Pt.(  $T_1T = 29.2$  msec for Pt which is used in this measurement ) The temperature was controlled by feedback of the thermometer output to the heater in liquid  $^3\text{He}$ . A superconducting magnet was immersed in liquid  $^4\text{He}$  to provide steady magnetic field. Receiver coil was wound on a sample to maximize filling factor and was immersed directly in liquid  $^3\text{He}$ . The transmitter coil was located in  $^4\text{He}$  bath to avoid the rf heating.

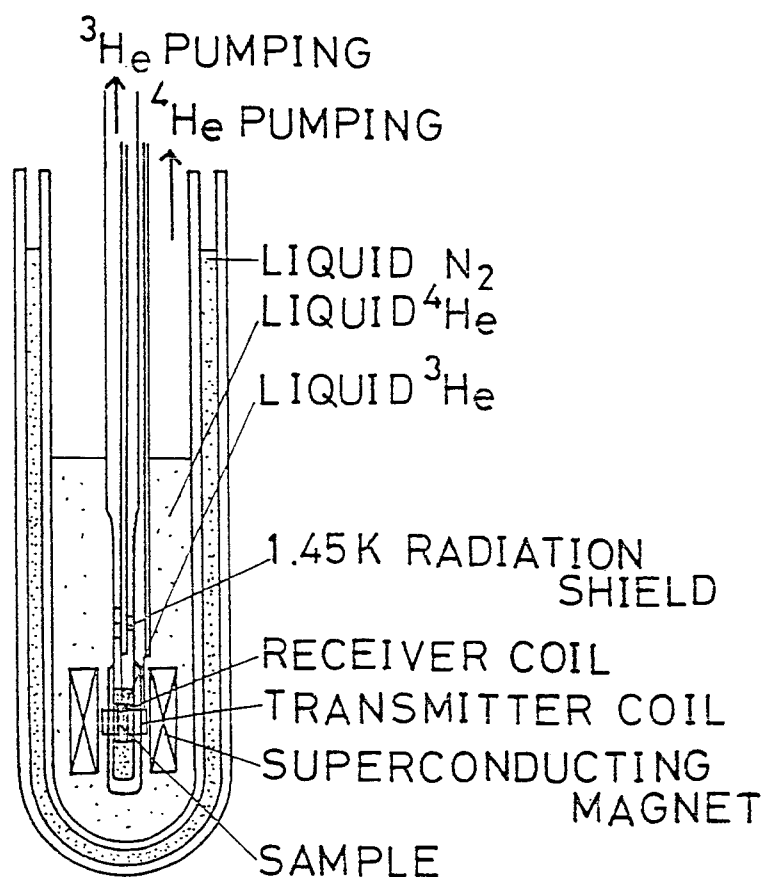


Fig.1 The single-cycle type  $^3\text{He}$  cryostat and the NMR arrangement

## 5) Dilution refrigerator

$^3\text{He}$ - $^4\text{He}$  dilution refrigerator has been used to obtain low temperature below 0.3 K. The principal parts of a continuously operating dilution refrigerator are shown in Fig. 2-1. The phase separation occurs in the mixing chamber and cooling is produced there by driving  $^3\text{He}$  atoms from the boundary to the lower dilute phase. The continuous dissolution of  $^3\text{He}$  atoms from the concentrated to the dilute phase is obtained by circulating  $^3\text{He}$  in the system by means of a pump at room temperature. Incoming gas is first precooled and liquified in the condenser attached to the  $^4\text{He}$  pot ( 1.1K ). The liquid then enters the still at 0.7K, the continuous exchanger, the step heat exchangers and finally the mixing chamber. After crossing the phase boundary,  $^3\text{He}$  atoms driven by an osmic pressure gradient, proceed through the heat exchangers to the still and are removed from the still by pumping. A commercial Oxford Instrument 150 microwatt dilution refrigerator was used for this investigation. The base temperature of this dilution refrigerator is 11.0 mK and cooling power at 100 mK is 150 microwatt. The experimental arrangement is shown in Fig. 2-2. The sample was in direct contact with liquid helium inside the mixing chamber. In order to produce cooling at the base of the long glass tube, it is necessary to bring the concentrated helium 3 stream close to the powdered sample. To do this a bent stainless steel tube is provided. The sample temperature was measured by carbon resistance thermometer at the mixing chamber. The resistor was calibrated against the NMR intensity and  $T_1$  of Pt .

The crossed coil system was used for NMR. The cylindrical receiver coil of 0.01 mm diameter was wound on the glass tube to maximize the filling factor and was thermally anchored to the mixing chamber. The transmitter coil was saddle shape and was thermally anchored to the cold plate. The steady magnetic field was produced by a Helmholtz coil, which was located in the  $^4\text{He}$  bath. Warming up of the sample by eddy current was excluded by reduced repetition rate. The base temperature was 40 mK with applying rf pulses.

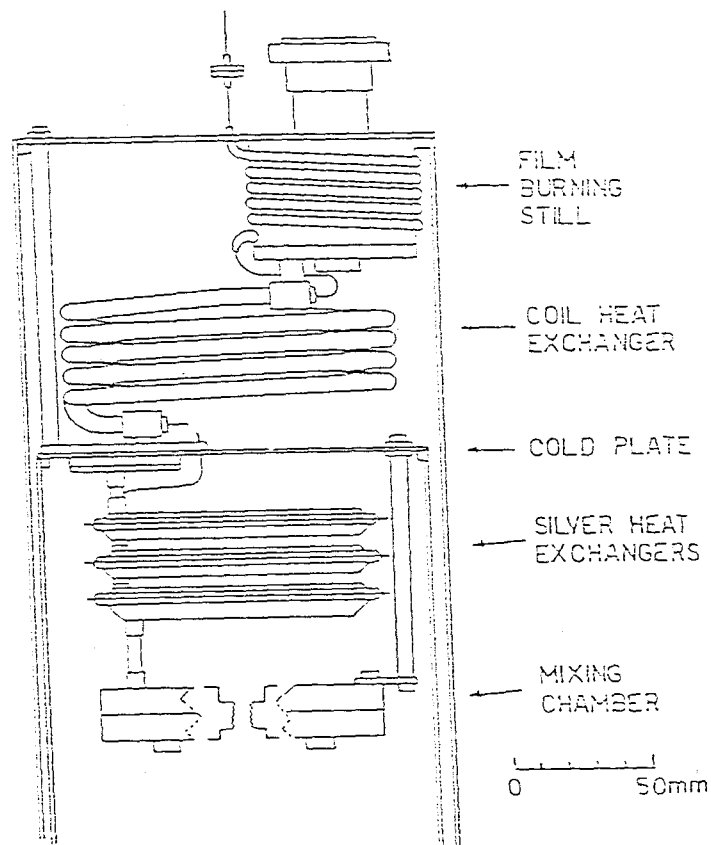


Fig.2-1 The principal parts of a continuously operating dilution refrigerator

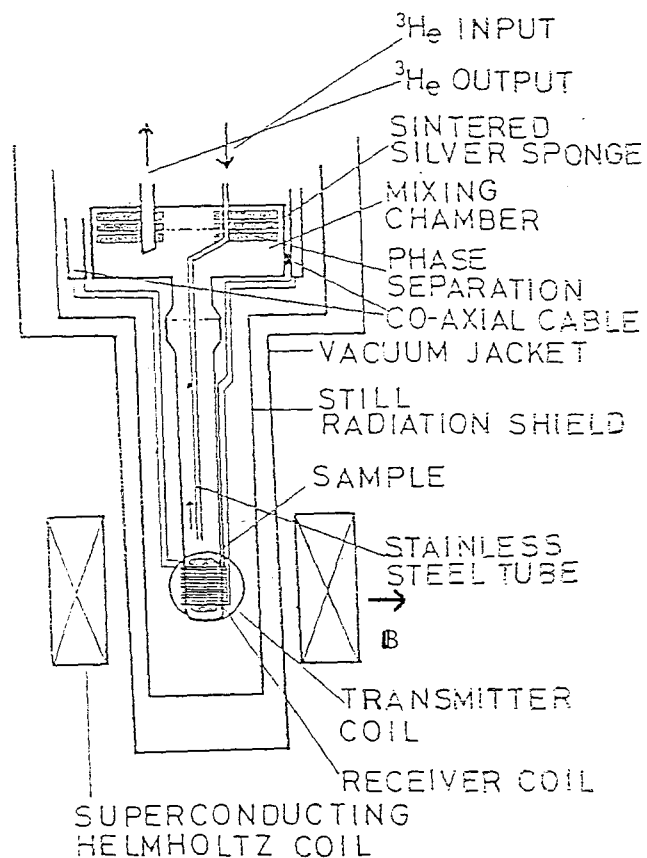


Fig.2-2 The NMR arrangement in the dilution refrigerator

## 6) NMR technique

The NMR shift, line width and spin lattice relaxation time  $T_1$  are important parameters in metal, being sensitive probes of the character of the conduction electron spins at the Fermi surface and character of the localized moments.

The NMR measurements were performed by the phase coherent pulsed spectrometer in the frequency range of 1-20 MHz. In the measurement of low frequency NMR, the signal averager was used to improve the signal to noise ratio. Furthermore, the fast recovery of the receiver system was secured with a shunt chopper.

### 6-1) Resonance shift measurement

Resonance shift of  $^{11}\text{B}$  and  $^{103}\text{Rh}$  were obtained by the following frequency field ratio.<sup>12)</sup>

$$^{11}\text{B}: \nu/H = 1.366 \text{ KHz/Oe}, \quad ^{103}\text{Rh}: \nu/H = 0.13 \text{ KHz/Oe}$$

### 6-2) $T_1$ measurement

In many systems encountered in NMR, when the interactions contributing to the line width ( quadrupolar or magnetic ) are so strong that  $\Delta H_{\text{inhomo}}$  is much larger than  $H_1$ , the spin system can not be saturated completely by the single pulse. Then the recovery of the nuclear spin after the single pulse is not exponential which yields an ambiguity in  $T_1$  measurement. The problem of incomplete spin saturation can frequently be circumvented by using the saturation comb method. The saturation comb consists of a train of  $n$  identical (  $n = 4-20$  ), equally spaced pulses applied within a time less than  $T_1$ . This pulse train is followed by a pulse-echo sequence to monitor the recovered magnetization. Indeed we have used a train of 10 saturation pulses above 1.2 K, and about 80% of nuclear magnetization recovers exponentially. In the temperature below 1K, rf heating becomes a serious problem, and special precautions ( e.g., reduced pulse repetition rate, reduced number of saturation pulses. ) were necessary to assure reliable data. At  $^3\text{He}$  temperature, pulse repetition rate is 5-10 sec and number of saturation pulses is 3-5. When

we used  $^3\text{He}$ - $^4\text{He}$  dilution refrigerator, pulse repetition rate is 20-30 sec and number of saturation pulses is 2-3.

About 40% of the nuclear magnetization recovers exponentially in this pulse condition.



### §3 The crystal structure of $\text{RERh}_4\text{B}_4$

The structure of ternary rhodium borides was determined by Vandenberg and Mattias<sup>10)</sup> as shown in Fig. 3. The lattice parameters of the Rh compounds are shown in Table 1. The space group is  $\text{P4}_2/\text{nmc}$  ( No. 137 ), with the atomic position as follows ( origin at  $\bar{4}m2$  ) 2RE in 2(b)  $(0,0,1/2)$ ,  $(1/2,1/2,0)$ ; 8Rh in 8(g)  $(0, x_{\text{Rh}}, z_{\text{Rh}})$ , etc., with  $x_{\text{Rh}} = 0.248$ ,  $z_{\text{Rh}} = 0.137$  : 8B in 8(g):  $(x_{\text{B}}, 0, z_{\text{B}})$ , etc., with  $x_{\text{B}} = 0.325$  and  $z_{\text{B}} = 0.847$ . The B atoms form pairs parallel to the a axis and are surrounded by five Rh atoms. The interatomic distance in the  $\text{CeCo}_4\text{B}_4$  structure is shown in Table 2.

Table 1. Cell parameter of the tetragonal  $\text{RERh}_4\text{B}_4$ .

	a (Å)	c (Å)
$\text{YRh}_4\text{B}_4$	5.308	7.403
$\text{NdRh}_4\text{B}_4$	5.333	7.468
$\text{SmRh}_4\text{B}_4$	5.312	7.430
$\text{GdRh}_4\text{B}_4$	5.309	7.417
$\text{TbRh}_4\text{B}_4$	5.303	7.404
$\text{DyRh}_4\text{B}_4$	5.302	7.395
$\text{HoRh}_4\text{B}_4$	5.293	7.379
$\text{ErRh}_4\text{B}_4$	5.292	7.374
$\text{TmRh}_4\text{B}_4$	5.287	7.359
$\text{LuRh}_4\text{B}_4$	5.294	7.359

Table 2 Interatomic distance in  $\text{YRh}_4\text{B}_4$  ( in Å )

Rh-1Rh: 2.63	Y -4Rh: 2.99	B -2Y : 3.03
-2Rh: 2.75	-8Rh: 3.14	-1Y : 3.09
-1Rh: 2.66	B -1Rh: 2.17	
-2Rh: 3.14	-2Rh: 2.17	
B -1B : 1.86	-2Rh: 2.25	

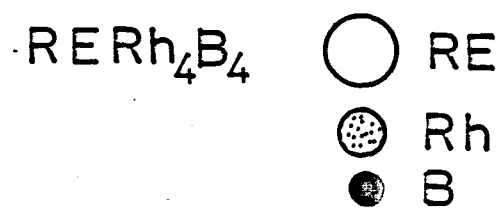
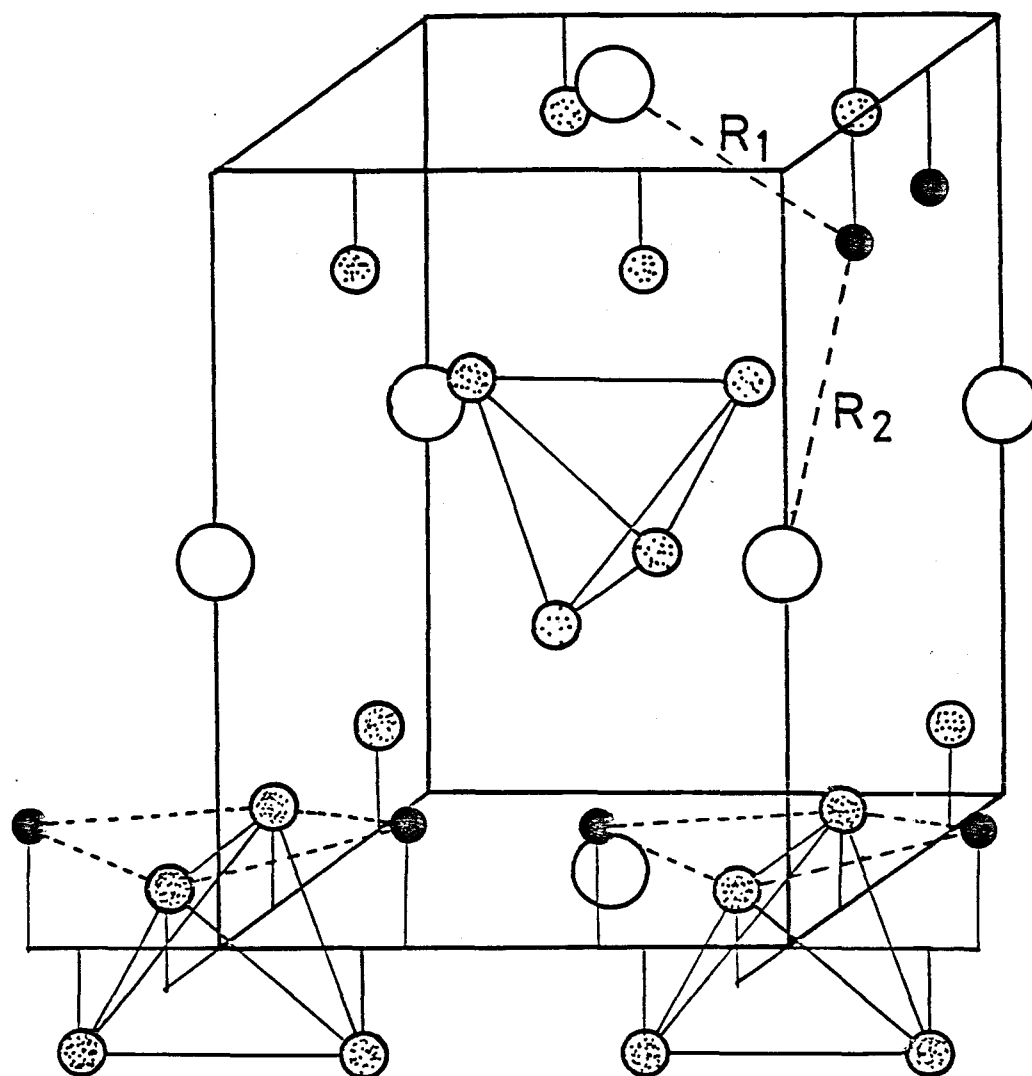


Fig.3 The crystal structure of  $\text{RERh}_4\text{B}_4$

## §4 Experimental results and discussions

### ( 1 ) Non-magnetic compounds $\text{YRh}_4\text{B}_4$ and $\text{LuRh}_4\text{B}_4$

The highest superconducting temperatures among the  $\text{RERh}_4\text{B}_4$  compounds are displayed by the non-magnetic compounds  $\text{LuRh}_4\text{B}_4$  ( $T_s = 11.5\text{K}$ ), which has a completely filled 4f electron shell and  $\text{YRh}_4\text{B}_4$  ( $T_s = 10.8\text{K}$ ) which has no 4f electrons.<sup>3)</sup> We performed NMR study of  $\text{YRh}_4\text{B}_4$  and  $\text{LuRh}_4\text{B}_4$  to know the density of states at each site of  $\text{RERh}_4\text{B}_4$  and the superconducting properties.

#### ( 1-1 ) The density of states ( DOS ) at RE, Rh and B site

In ternary boride  $\text{RERh}_4\text{B}_4$  Jarlborg and Freeman carried out ab initio self-consistent band structure calculations on three of these ternary borides (Y, Ho and Er).<sup>8)</sup> They have found that the weak f-s and f-d interaction in this compound is attributed to the negligibly small density of states of s- and p-electrons at RE site and small density of states of d-electron at RE site (1/3 the value of  $N_d(E_F)$  in Ho metal) as shown in Table 3.

In order to investigate DOS at each site experimentally, we measured the nuclear spin lattice relaxation time of  $^{89}\text{Y}$  ( RE site ),  $^{103}\text{Rh}$  and  $^{11}\text{B}$  in  $\text{YRh}_4\text{B}_4$  and  $\text{LuRh}_4\text{B}_4$ . In the normal state, the relation  $T_1T = \text{const.}$  is observed for each site, which is shown in Fig.4 and Fig.5, respectively.  $T_1T$  of  $^{103}\text{Rh}$  in  $\text{YRh}_4\text{B}_4$  and  $\text{LuRh}_4\text{B}_4$  are 25 secK, and  $T_1T$  of  $^{89}\text{Y}$  is 92 secK.<sup>13)</sup>  $T_1T$  of  $^{11}\text{B}$  is 55secK.  $T_1$  of  $^{11}\text{B}$  is also measured by Kumagai and Fradin, their value is  $T_1T = 46 \text{ secK}$ , which is slightly shorter than ours.

The important contributions to the relaxation rates arise from core-polarization hyperfine interaction with d-electron and orbital hyperfine interaction with p- and d- electron, as well as from the contact hyperfine interaction with s-electron.  $(T_1T)^{-1}$  may be expressed as

$$R = R_s + R_{orb}^p + R_{cp}^d + R_{orb}^d, \quad (1)$$

where  $R_s$ ,  $R_{cp}$  and  $R_{orb}$  represent the rate through the Fermi contact, core-polarization and orbital hyperfine interactions, respectively. We simply estimate  $R_{cp}$  and  $R_{orb}$  in tight-binding approximation. Then  $R_s$ ,  $R_{cp}$  and  $R_{orb}$  are written as following,

$$R_s = 2hk_B\gamma_N^2 (H_s N_s(E_F))^2, \quad (2)$$

$$R_{orb}^p = 4hk_B\gamma_N^2 (H_{orb}^p N_p(E_F))^2, \quad (3)$$

$$R_{orb}^d = 2hk_B\gamma_N^2 (H_{orb}^d N_d(E_F))^2 (2/3 \cdot f \cdot (2-5/3 \cdot f)) \quad (4)$$

$$R_{cp}^d = 2hk_B\gamma_N^2 (H_{cp}^d N_d(E_F))^2 (1/3 \cdot f^2 + 1/2 \cdot (1-f)^2) \quad (5)$$

where  $\gamma_N$  is the gyromagnetic ratio of the concerned nucleus. The density of states at the Fermi energy for s-, p- and d-electrons for one direction of the spin are denoted by  $N_s(E_F)$ ,  $N_p(E_F)$  and  $N_d(E_F)$  respectively and  $f$  is the average fractional admixture of 4-d ( $\Gamma_5$ ) state at the Fermi surface. We assume  $f=1$  or  $3/5$  as  $R$  is not so sensitive to  $f$ . We refer the value  $H_s$ ,  $H_{orb}^p$  and  $H_{cp}^d$  for  $^{89}\text{Y}$  and  $^{103}\text{Rh}$  to those of the pure Y and Rh metal following Asada et al.<sup>14,15)</sup> These assumed values are given in Table 3 together with the calculated relaxation rate. This estimation agrees with the experimental relaxation rate. As for  $^{11}\text{B}$ , we calculate  $T_1$  by using the atomic hyperfine field  $H_s$ <sup>16)</sup> and  $N_s(E_F)$ <sup>8)</sup> at B site. The result is shown in Table 3. The calculated value is smaller than the experimental value. The discrepancy may become small if we take into account the contribution from p-electron and the change of the hyperfine field in the compound from the atomic value.

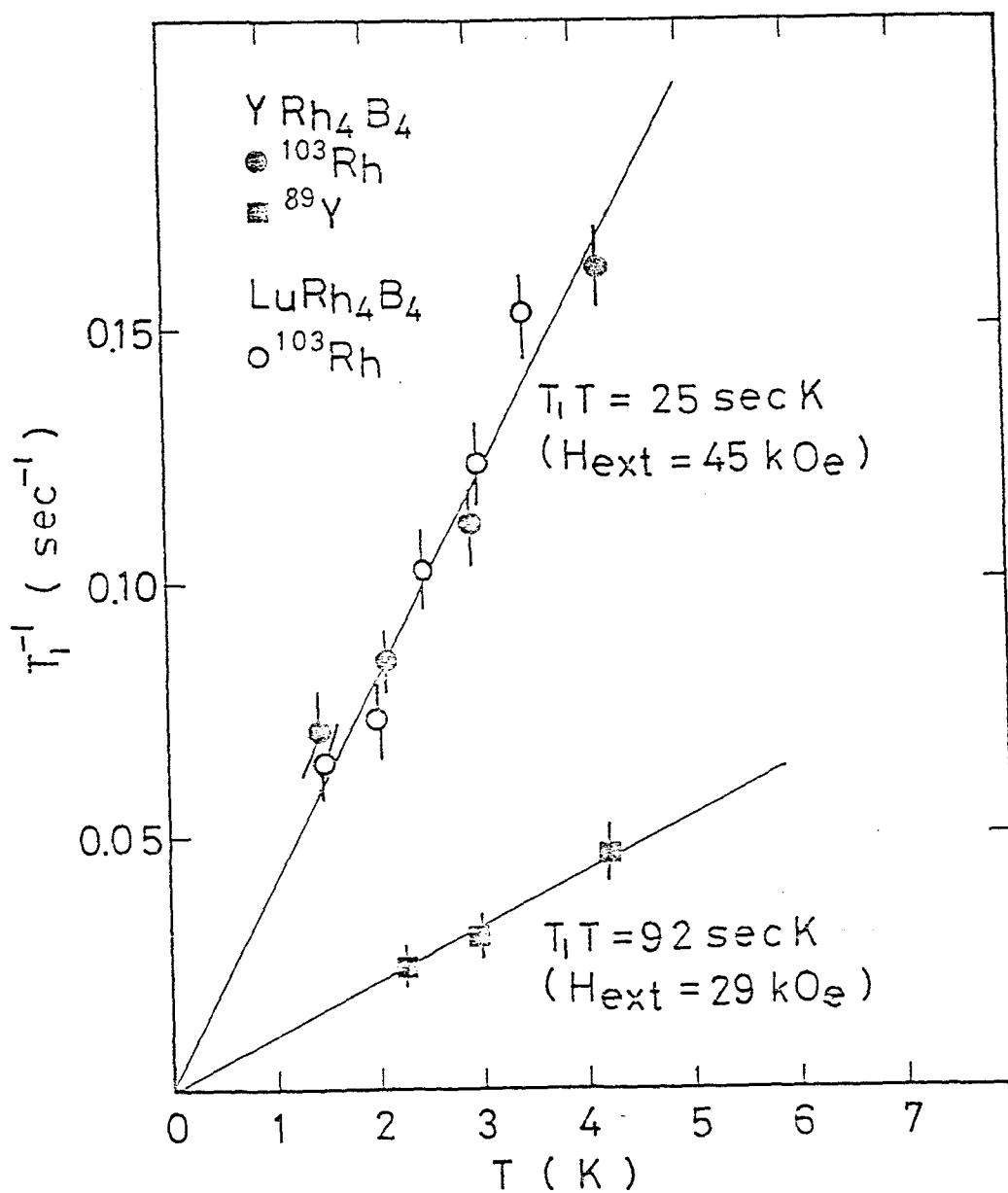


Fig.4 Temperature dependence of  $T_1$  of <sup>89</sup>Y and <sup>103</sup>Rh in YRh<sub>4</sub>B<sub>4</sub> and LuRh<sub>4</sub>B<sub>4</sub>.

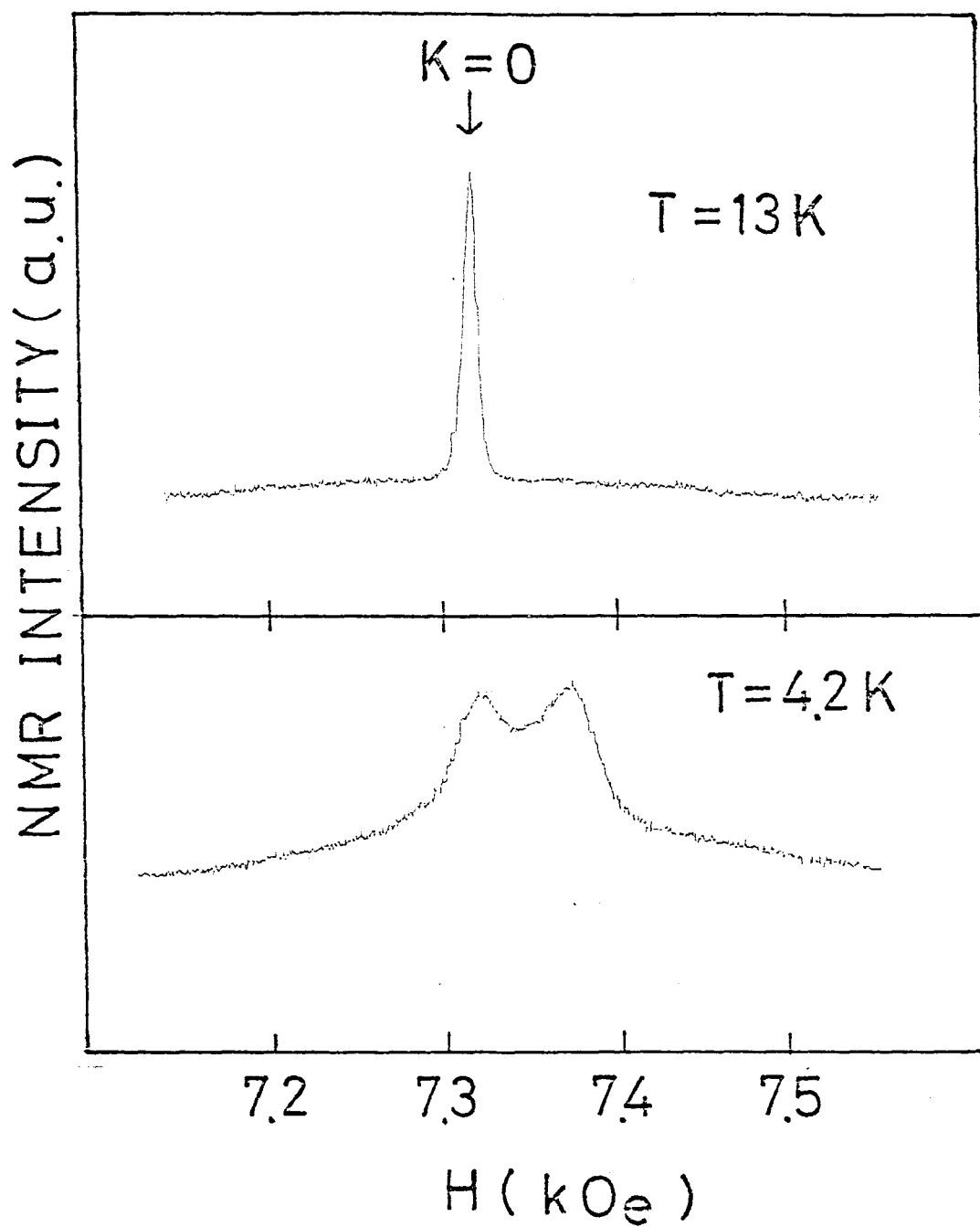


Fig. 5-1  $^{11}\text{B}$  NMR of  $\pm 1/2$  transition of quadrupole split lines in  $\text{LuRh}_4\text{B}_4$   
The system is in normal state at  $T = 13\text{ K}$ .

Fig. 5-2  $^{11}\text{B}$  NMR spectrum in  $\text{LuRh}_4\text{B}_4$  in superconducting mixed state. An additional broadening and a negative shift are observed.

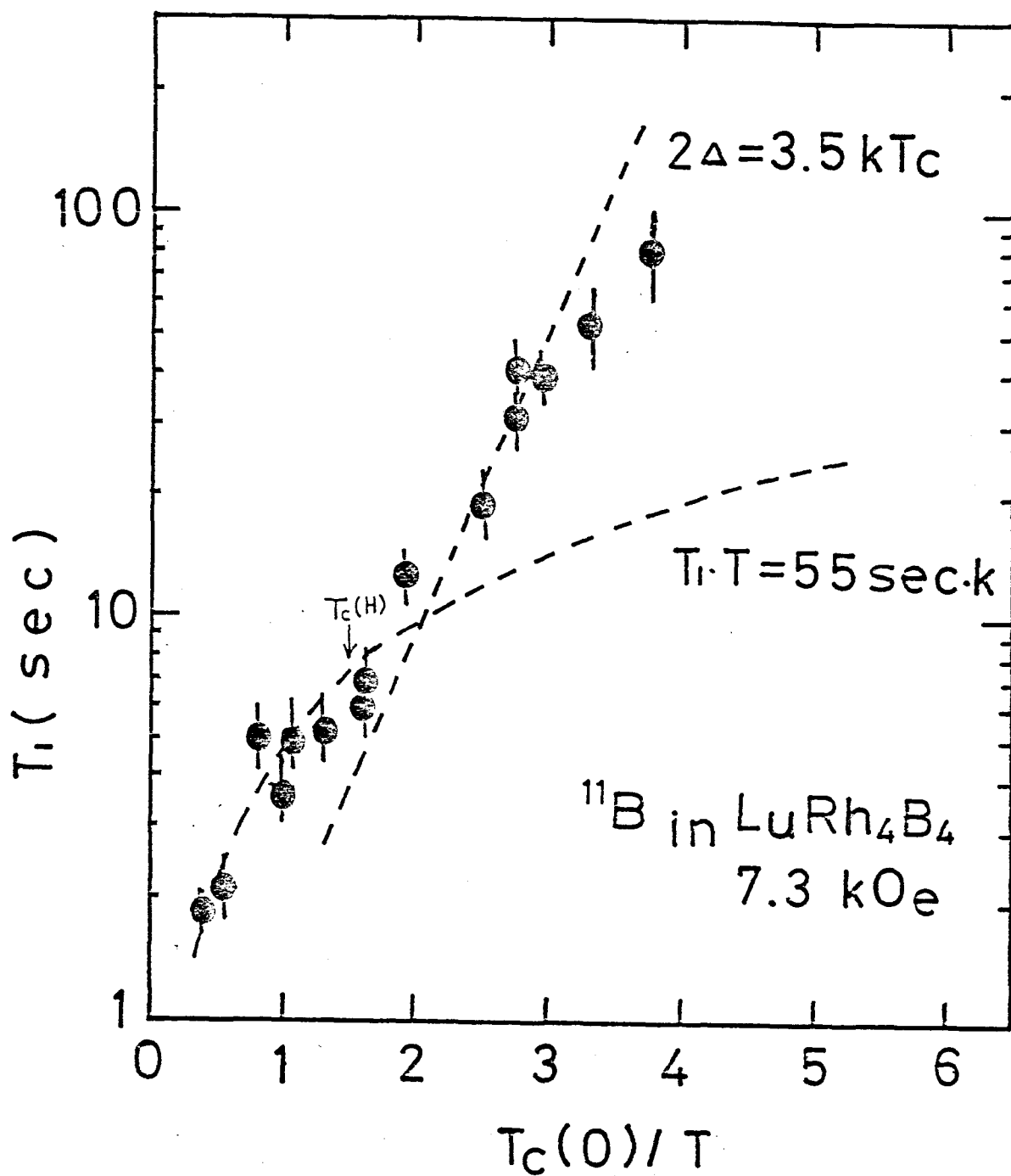


Fig.6 Temperature dependence of  $T_1$  of  $^{11}\text{B}$  in  $\text{LuRh}_4\text{B}_4$ . The arrow indicates the  $T_c(H)$  at 7.3 kOe.

Table 3

Comparison of calculated and observed  $T_1$  in  $\text{LuRh}_4\text{B}_4$  and  $\text{YRh}_4\text{B}_4$ .  $N(E_F)$  is in units of ( state/eV · atom · spin )  $H_{\text{hf}}$  is in (  $10^6$  Oe ) and  $(T_1 T)^{-1}$  is in ( sec · K )<sup>-1</sup>.

	$N_s(E_F)$	$N_p(E_F)$	$N_d(E_F)$	$H_s$	$H_{\text{orb}}^p$	$H_{\text{orb}}^d$	$H_{\text{cp}}^d$	$(T_1 T)^{-1}_{\text{cal}}$	$(T_1 T)^{-1}_{\text{exp}}$
$^{89}\text{Y}$	0 <sup>a</sup>	0.037 <sup>a</sup>	0.35 <sup>a</sup>	8.8 <sup>b</sup>	1.29 <sup>b</sup>	0.16 <sup>b</sup>	-0.21 <sup>b</sup>	$f=1$ 0.0087	0.011
$^{103}\text{Rh}$	0.018 <sup>a</sup>	0.074 <sup>a</sup>	0.41 <sup>a</sup>	9.8 <sup>c</sup>	2.5 <sup>c</sup>	0.98 <sup>c</sup>	-0.12 <sup>c</sup>	$f=1$ 0.0085 0.025 $(f=3/5)$ (0.039)	0.04
$^{11}\text{B}$	0.009 <sup>a</sup>			1.0 <sup>d</sup>				0.0044	0.022 <sup>e</sup> 0.018

a) reference 8)

b) reference 14)

c) reference 15)

d) reference 16)

e) reference 13)



( 1-2 ) NMR in superconducting mixed state

In type II superconductor the field penetration  $\lambda$  is much larger than the superconducting coherent length  $\xi$ . (  $\xi \ll \lambda$  ) Then the surface energy of a wall separating normal and superconducting region becomes negative. In order to maximize the surface to volume ratio for the normal region, the normal and superconducting regions are finely divided and normal region forms a filament of small diameter. Each filament has a hard core of radius  $\xi$ , where the superconducting electron density is reduced as shown in Fig.7. The field is maximum at the center of the filament but extends to the superconducting region with a distance  $\lambda$ .

In the intermediate fields  $H_{c1} < H < H_{c2}$ , where the vortices ( filaments of normal regions ) form a dense lattice. The detailed calculation shows that the most favorable arrangement is triangle lattice.<sup>17)</sup>

Then the magnetic flux density B is

$$B = \phi_0 n_L = \frac{2}{\sqrt{3}} \cdot \phi_0 / d^2 \quad (6)$$

where  $\phi_0$  is one quantum of flux ,

$$\begin{aligned} \phi_0 &= ch/2e \\ &= 2 \times 10^{-7} \text{ G cm}^2 \end{aligned} \quad (7)$$

d is the distance between the nearest neighbor filaments and  $n_L$  is the number of flux per unit area.

Thus field penetrates into the superconducting state. The field distribution is expressed by mean square root of field.

$$\begin{aligned} \Delta H &= ( \langle H^2 \rangle - \langle H \rangle^2 )^{1/2} \\ &= \frac{B}{\sqrt{4\pi} \lambda} \left( 1 + \left( \frac{2\pi\lambda}{d} \right)^2 \right)^{-1/2} \end{aligned} \quad (8)$$

Figure 5-2 shows  $^{11}\text{B}$  NMR of  $\pm 1/2$  transition of quadrupole split lines in superconducting mixed state of the non-magnetic compound  $\text{LuRh}_4\text{B}_4$ . The excess broadening compared with that in the normal state is observed. This line broadening is associated with the field inhomogeneity  $\Delta H$  of eq.8. By using this equation  $\lambda$  is estimated to be  $1000\text{\AA}$  in  $\text{LuRh}_4\text{B}_4$ . The negative shift of the spectrum is associated with diamagnetism of superconductivity.

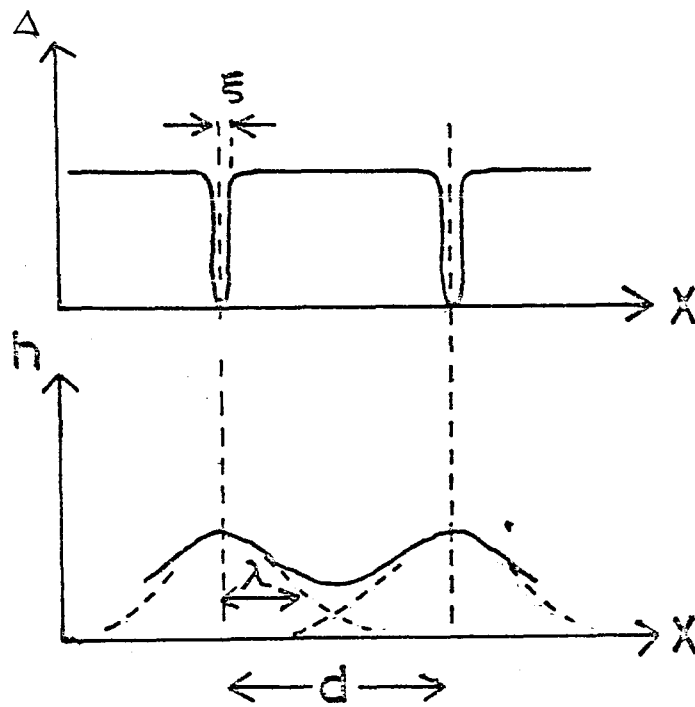


Fig.7 Structure of vortex line in a type II superconductor. The magnetic field is maximum near the center of the vortex line. Going outwards,  $h$  decreases because of the screening in an electromagnetic region of radius  $\approx \lambda$ . Owing to the superposition of nearest neighbor contribution the field penetrates into the superconducting state. On the other hand superconducting electron density is reduced only in a core region of radius  $\xi$ .

$T_1$  in BCS superconductor is described in general form <sup>18)</sup>

$$\frac{T_1^N}{T_1^S} = \frac{2}{k_B T} \int \frac{(E E' + \Delta^2) f(E) (1 - f(E'))}{[(E^2 - \Delta^2)(E'^2 - \Delta^2)]^{1/2}} dE \quad (9)$$

$$E' = E \pm \hbar \omega_n$$

where  $\Delta$  is the superconducting energy gap,  $\omega_n$  is rf frequency and  $f(E)$  is the Fermi-Dirac distribution function of the quasiparticle excitation energy  $E$ . This relaxation due to the nuclear hyperfine interaction with the conduction electrons shows an enhancement just below  $T_S$  due to the sharp peak in the density of states at the gap edge and an exponential behavior on temperature at low temperature with  $2\Delta = 3.5 k_B T_S$ .

In  $\text{LuRh}_4\text{B}_4$   $T_1$  of  $^{11}\text{B}$  in the superconducting state was measured. The result is shown in Fig.6.  $T_1$  changes exponentially as  $\exp(\Delta/k_B T)$  with  $2\Delta = 3.5 k_B T_S$  ( $T_S = 11 \text{ K}$ ). The energy gap obtained from  $T_1$  is just the same value as obtained by BCS theory. This means  $\text{LuRh}_4\text{B}_4$  is a weak coupling superconductor.

( 2 ) NMR study of  $\text{RERh}_4\text{B}_4$  compound

( RE is magnetic ion ) - Knight shift measurement

$\text{RERh}_4\text{B}_4$  compounds exhibit complex magnetic properties. For example, Dy compound has the highest  $T_m$  ( 11.2 K ) in the series of simple ferromagnetic compound from Gd to Ho, as shown in Fig.8.

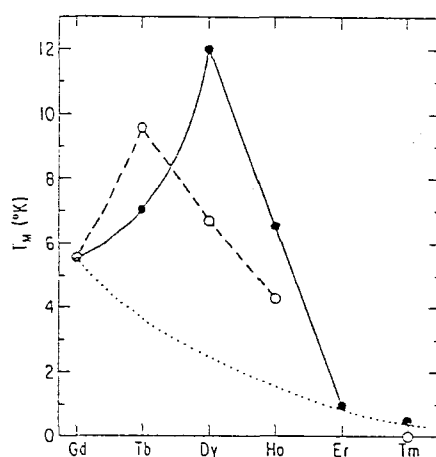


Fig.8 Magnetic transition temperature, closed circle: the observed value, dotted line: the value predicted by deGennes rule , open circle: the value obtained by the molecular field model with  $B_2^0$  crystal field parameter.

In order to understand the magnetic properties microscopically we performed NMR study in  $\text{RERh}_4\text{B}_4$  compound. ( RE = Nd, Sm, Gd, Tb, Dy, Ho, Er and Tm )

( 2-1 ) Knight shift of  $^{11}\text{B}$

We measured the Knight shift of  $^{11}\text{B}$  to see the variation of the conduction electron spin polarization with RE in dense  $\text{RERh}_4\text{B}_4$  system. In the paramagnetic state the localized moments induce a uniform conduction electron spin polarization, which yields the Knight shift of the non-magnetic nuclear species.

The typical spectra obtained for RE = Gd, Sm and Tm are shown in Fig.9-1, Fig.10-1 and Fig.11 respectively. These NMR spectra are anisotropic in paramagnetic state. We analyzed the spectra by using the conventional form for isotropic and anisotropic shift ,

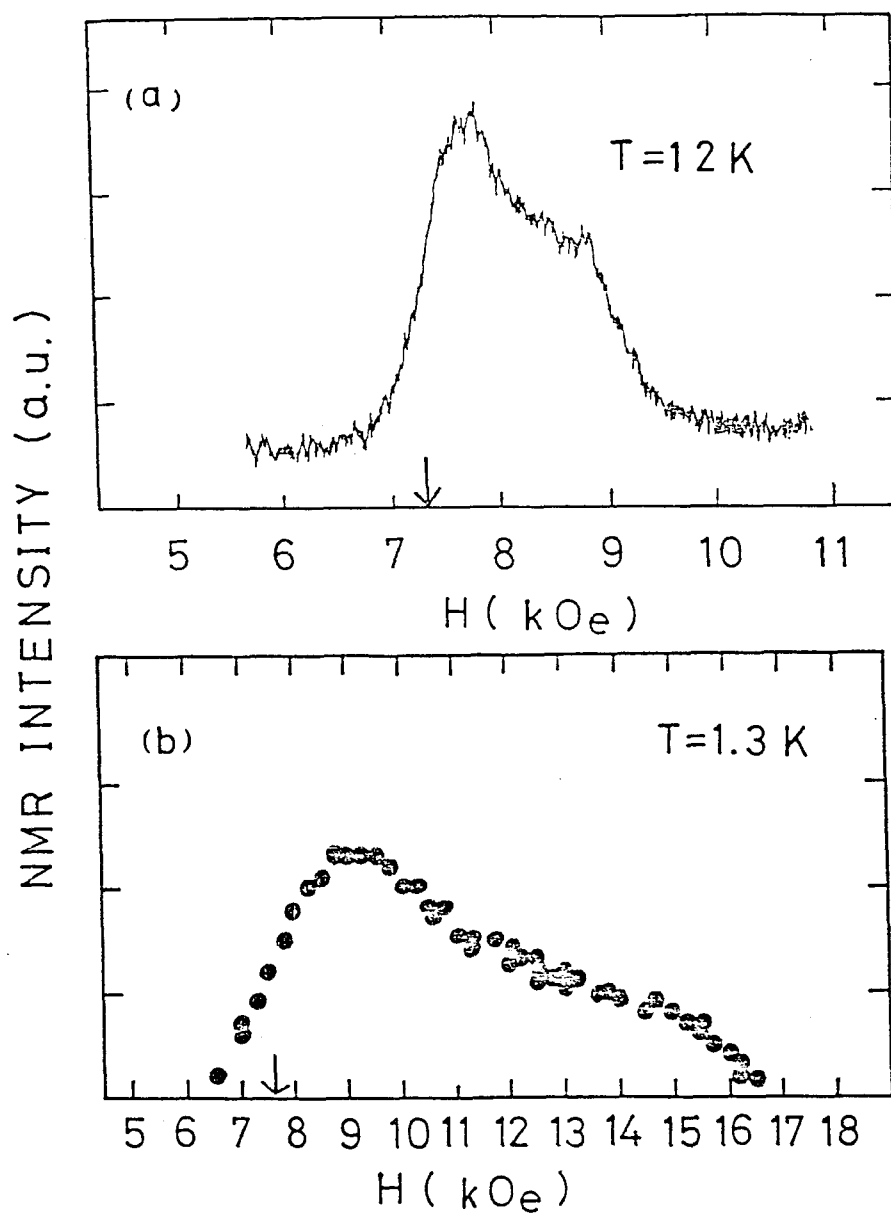


Fig. 9-1 NMR spectrum of  $^{11}\text{B}$  in  $\text{GdRh}_4\text{B}_4$  at  $T = 12\text{ K}$  and  $f = 10.0\text{ MHz}$ . The system is in paramagnetic state, the arrow means  $K = 0$ .

Fig. 9-2 NMR spectrum of  $^{11}\text{B}$  in  $\text{GdRh}_4\text{B}_4$  at  $T = 1.3\text{ K}$  and  $f = 10.0\text{ MHz}$ . The system is in ferromagnetically ordered state.

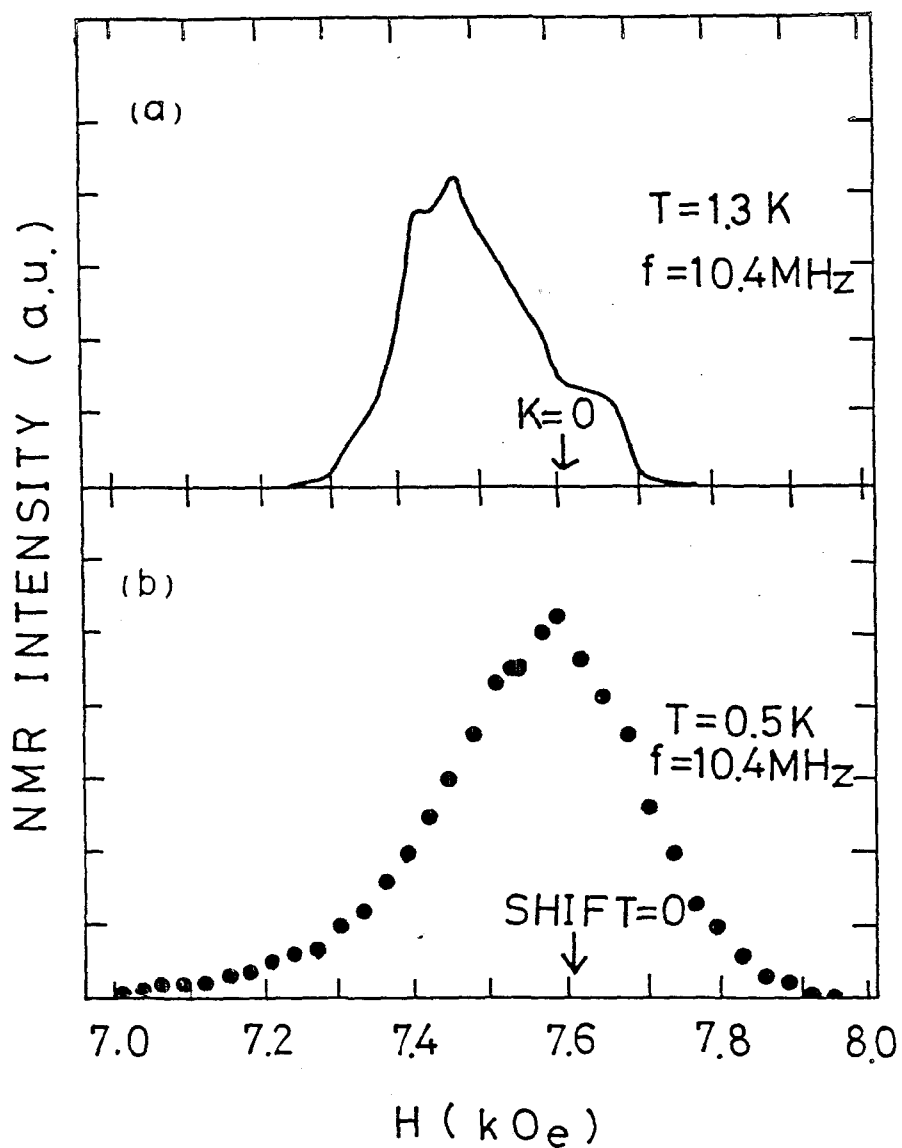


Fig. 10-1 NMR spectrum of  $^{11}\text{B}$  in  $\text{SmRh}_4\text{B}_4$  at  $T = 1.3 \text{ K}$  and  $f = 10.4 \text{ MHz}$ . The system is in paramagnetic and normal state.

Fig. 10.2 NMR spectrum of  $^{11}\text{B}$  in  $\text{SmRh}_4\text{B}_4$  at  $T = 0.5 \text{ K}$  and  $f = 10.4 \text{ MHz}$ . The system is in antiferromagnetic and normal state.

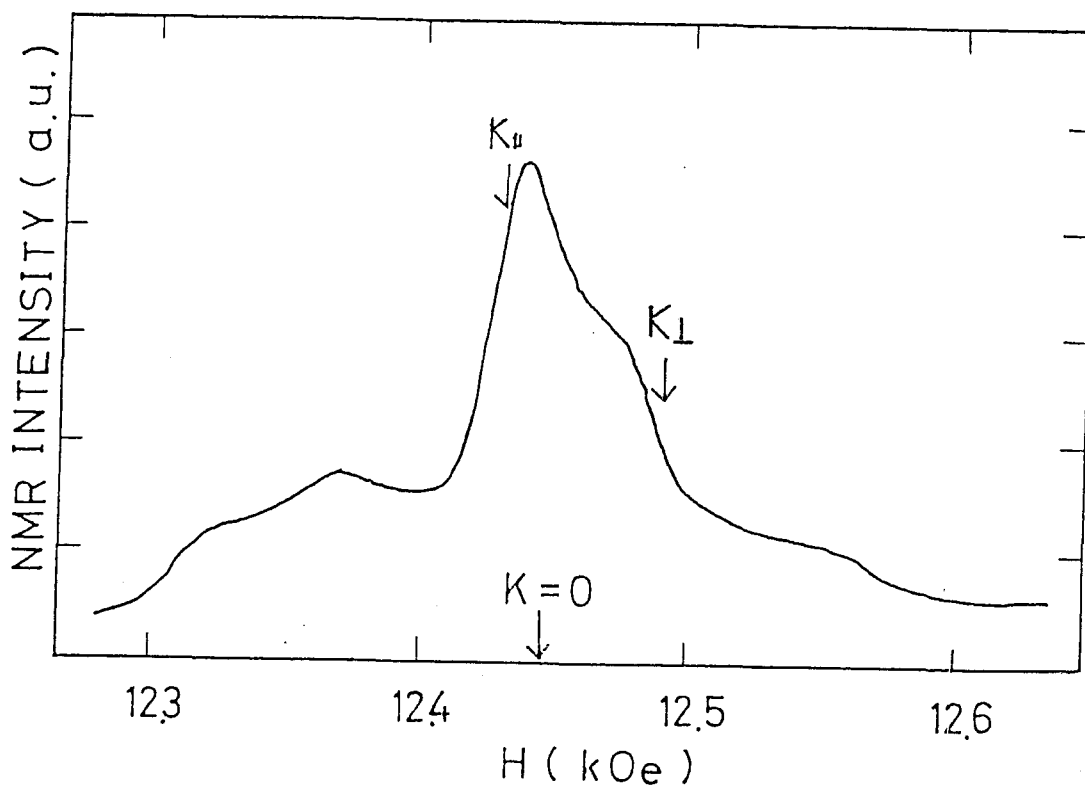


Fig. 11 NMR spectrum of  $^{11}\text{B}$  in  $\text{TmRh}_4\text{B}_4$  at  $T=300\text{K}$  and  $f=17.0\text{MHz}$ .

$$K = K_{\text{iso}} + 1/2 \cdot K_{\text{anis}} (3 \cos^2 \theta - 1) \quad (10)$$

$K(\theta=90^\circ)$  is determined at 85% of the peak height and  $K(\theta=0^\circ)$  is determined at 50% of the shoulder height as the spectrum has an extra Gaussian broadening.

By using  $K(\theta=90^\circ)$ ,  $K(\theta=0^\circ)$  and eq. 10,  $K_{\text{iso}}$  and  $K_{\text{anis}}$  are determined.

The isotropic and anisotropic hyperfine coupling constants,  $A_{\text{iso}}$  and  $A_{\text{anis}}$  are obtained from the Knight shift and the susceptibility data,  $\chi_f$ .

$$K_{\text{iso}} = A_{\text{iso}} \cdot \chi_f \quad (11)$$

$$K_{\text{anis}} = A_{\text{anis}} \cdot \chi_f$$

In Gd and Sm compound  $K$  vs  $\chi$  plot with temperature as an implicit parameter is shown in Fig.12 and Fig.13 respectively.

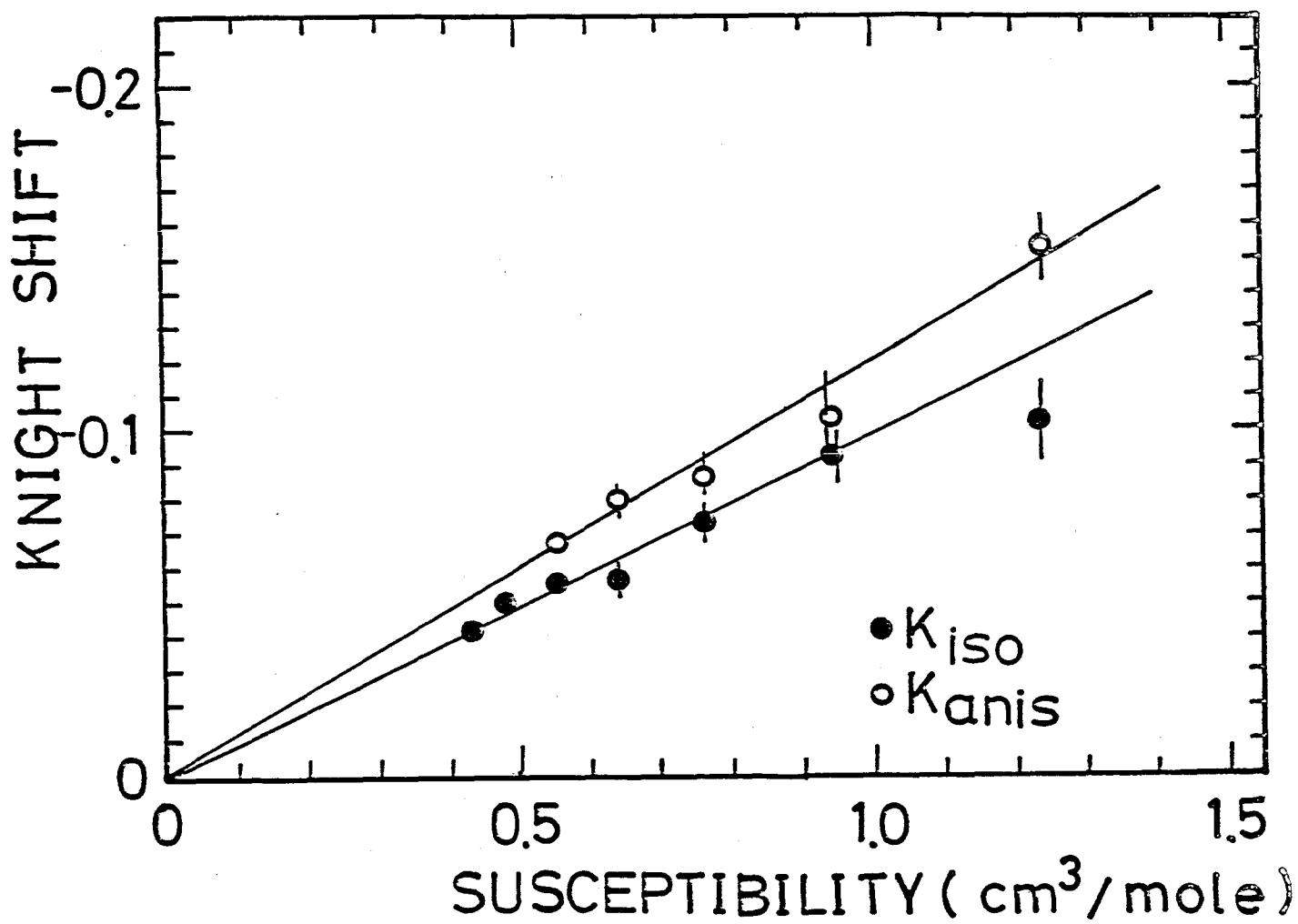


Fig. 12 Isotropic and anisotropic Knight shift of  $^{11}\text{B}$  in  $\text{GdRh}_4\text{B}_4$  vs susceptibility.



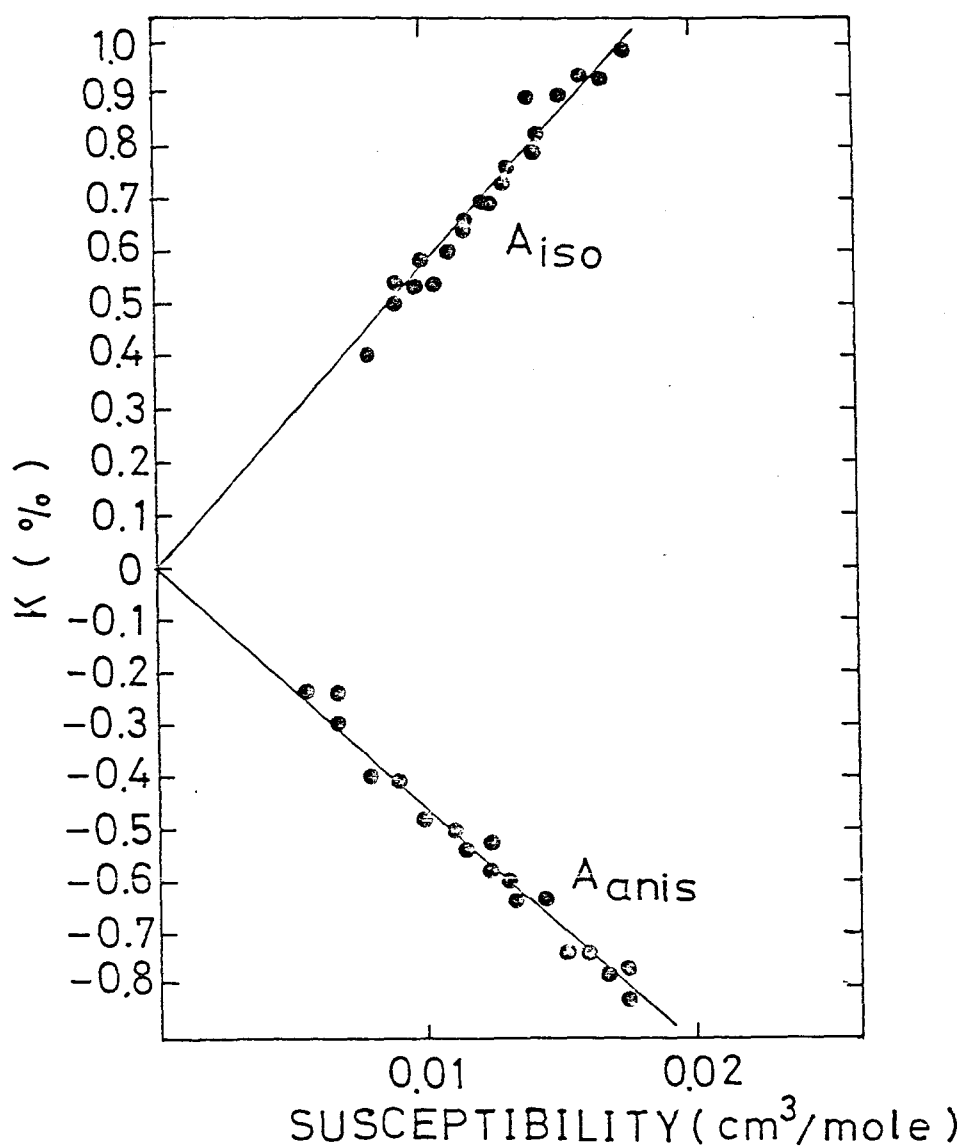


Fig. 13 Isotropic and anisotropic Knight shift of  $^{11}\text{B}$  in  $\text{SmRh}_4\text{B}_4$  vs susceptibility.

In Nd, Tb, Dy, Ho, Er and Tm compound Knight shifts are obtained at 300K. With the susceptibility data, the hyperfine coupling constants are obtained in Ry, Ho, Er, Tm and Nd compounds. For RE = Tb we used the free atom value for the effective moment, as there is no susceptibility datum. The obtained coupling constants are shown in Fig.14 and Fig.15 respectively.

The isotropic shifts are all negative for the heavy RE and positive for the light RE. This shift is induced by the conduction electron spin polarization at B site. Especially conduction electron, which has s-symmetry at B site is responsible for this shift. We can evaluate the conduction electron spin polarization by using a simplified uniform polarized model.<sup>19)</sup>

$$K_{iso} = A_{iso} \cdot \chi_f \quad (12)$$

$$A_{iso} = \frac{g_J - 1}{g_J} \cdot \frac{4 J_{sf} N_s(E_F) H_S}{9\mu_B}$$

where  $g_J$  is the Landé g factor,  $\mu_B$  is Bohr magneton,  $\chi_f$  is the thermal averaged value of RE moments in external field,  $J_{sf}$  is the exchange interaction between the RE moment and the conduction electron and  $H_S$  is the atomic hyperfine field of  $^{11}\text{B}$ .  $J_{sf}$  means the exchange interaction with s-electron at RE site in uniform polarized model. However more precisely d-electron spin polarization at RE site also contributes to the conduction electron spin polarization which has s-symmetry at B site.

As shown in Fig.14,  $A_{iso}$  is well explained by

$$A_{iso} = \frac{g_J - 1}{g_J} \cdot 2 A_{iso}(\text{Gd}) \quad (13)$$

$$A_{iso}(\text{Gd}) = -550 \text{ Oe}/\mu_B$$

This means that  $J_{sf}N_s(E_F)$  is nearly same, or the conduction electron spin polarization which is induced by unit spin is nearly same for all  $\text{RERh}_4\text{B}_4$ .  $J_{sf}N_s(E_F)$  is obtained to be  $-2.4 \times 10^{-3}$  state/atom spin, where  $H_S = 1.0 \times 10^6$  Oe is assumed.<sup>16)</sup>

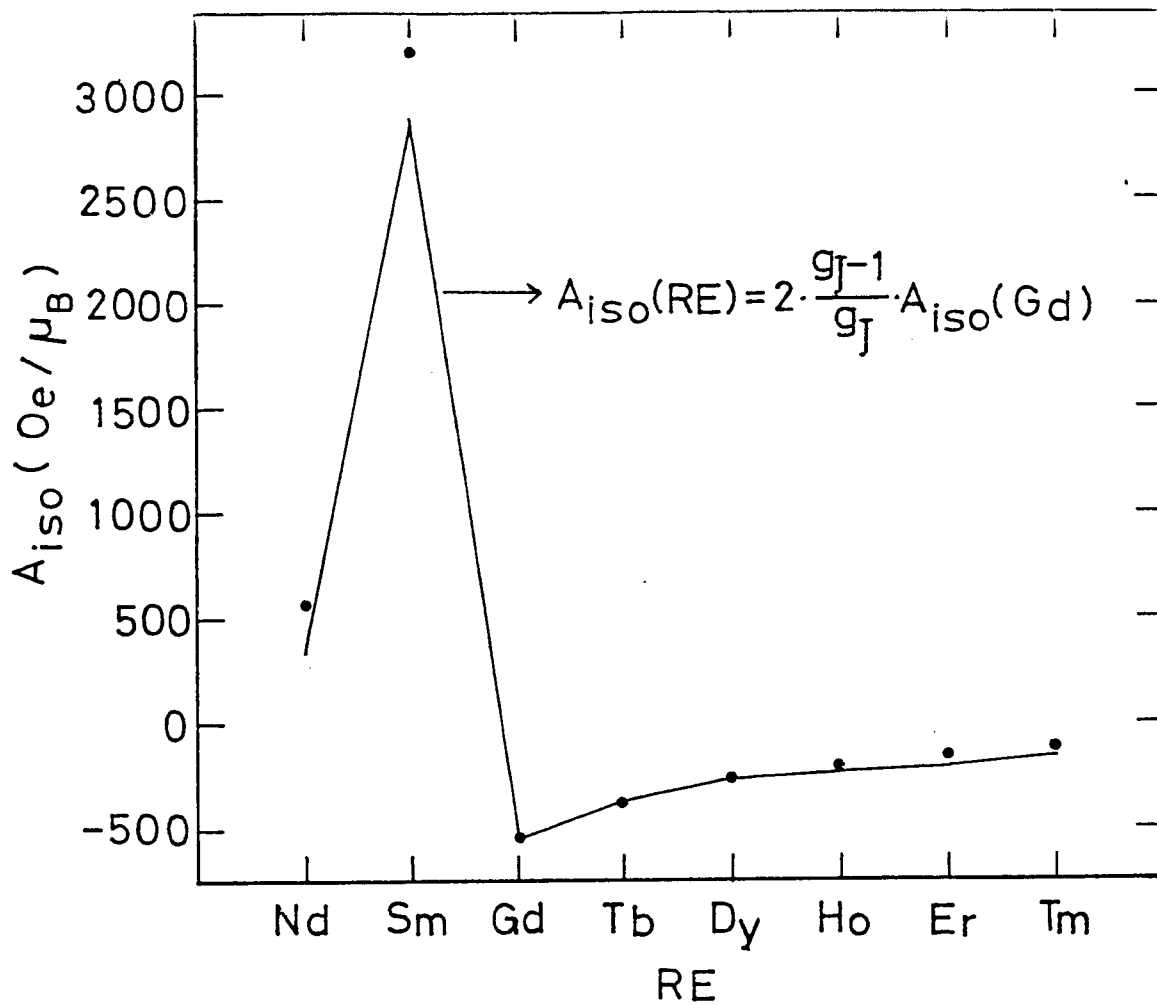


Fig. 14  $A_{iso}$  of  $^{11}\text{B}$  in  $\text{RERh}_4\text{B}_4$ . The solid line represents the isotropic hyperfine coupling const., which is normalized by the  $A_{iso}(\text{Gd})$

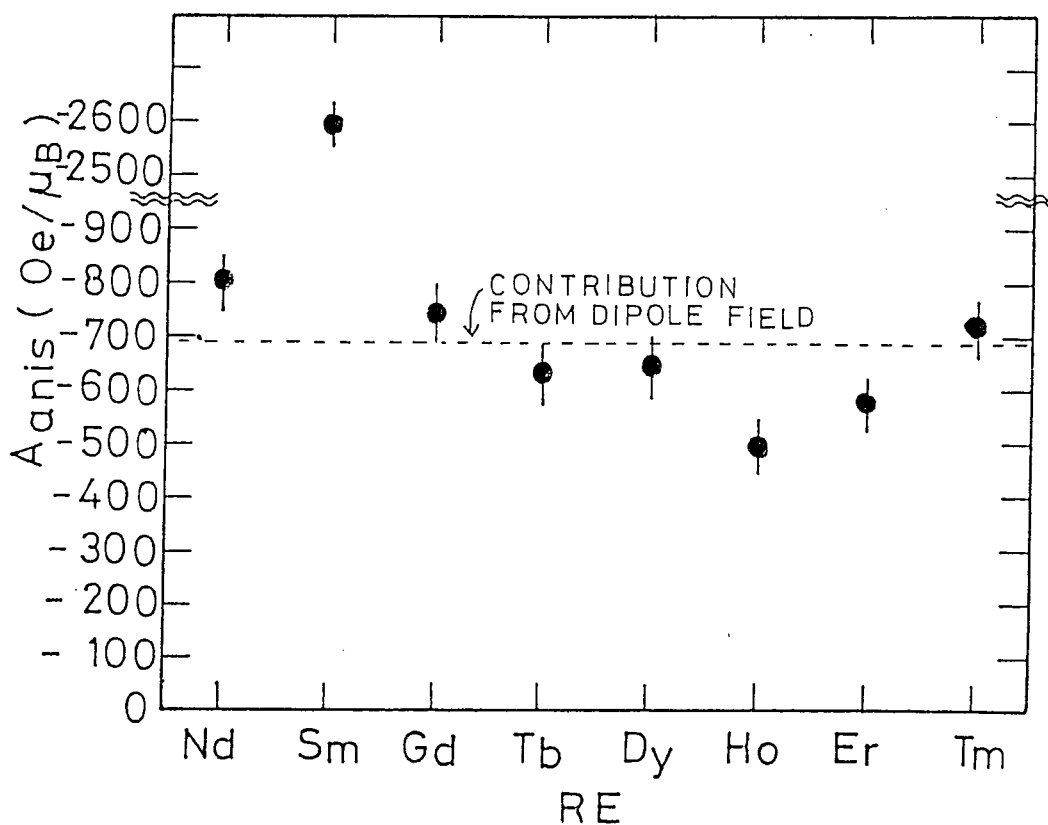


Fig. 15  $A_{anis}$  of  $^{11}\text{B}$  in  $\text{RERh}_4\text{B}_4$ . The dashed line represents the contribution from the dipole field.

If  $T_m$  is determined only by RKKY interaction,  $T_m$  should be proportional to the de Gennes factor  $G = (g_J - 1)^2 J(J+1)$ , where  $J$  is the total angular momentum. The de Gennes factor can be derived in the simplest of molecular field model.

$$\mathcal{H}_{\text{exch}} = -2 J' (g_j - 1)^2 J_z \langle J_z \rangle$$

where  $z$ -axis is the direction of the magnetic moment.  $J'$  is the effective exchange integral between RE ions. Then the magnetic transition temperature  $T_0$  is

$$T_0 = 2 J' (g_j - 1)^2 J(J+1)/3 \quad (14)$$

$$J = \frac{2z_0}{3k_B} J'$$

where  $z_0$  is the number of interacting RE ions.

As shown in Fig.8, however, Dy compound has the highest  $T_m$ . This means that  $T_m$  is determined not only by RKKY interaction but also by other contribution such as the crystal field effect (CFE). Indeed, recently, Shenoy has taken into account the CFE contribution. When the CFE splits the  $J_z$  state significantly with respect to  $k_B T_0$ , CFE terms should be added to the exchange Hamiltonian.

That is

$$\mathcal{H} = -2 J' (g_j - 1)^2 J_z \langle J_z \rangle + B_2^0 [3J_z^2 - J(J+1)] \quad (15)$$

When the ordering is along  $c$ -axis this leads to an ordering temperature  $T_m$

$$\text{given by } T_m = 2 J' (g_j - 1)^2 \cdot \frac{\sum_z J_z^2 \exp(-3B_2^0 J_z^2 / T_m)}{\sum_z \exp(-3B_2^0 J_z^2 / T_m)} \quad (16)$$

The transition temperature of the Gd compound can be used to fix a value for the exchange parameter,  $J'$ , because Gd, an  $L=0$  ion, is not affected by CFE. For the rest of the series, the RE dependent  $B_2^0$  parameter can be expressed for each RE.

$$B_2^0 = \alpha_2 A_2^0 \langle r^2 \rangle \quad (17)$$

where  $\alpha_2$  is the Stevens factor for each RE,  $\langle r^2 \rangle$  is the second moment of the 4-f radial wave function.  $A_2^0$  is a value related to the charge distribution. Shenoy et al measured the electronic field gradient at Gd nucleus by Mössbauer effect and determined  $A_2^0$ .  $B_2^0$  for each RE is estimated by using eq.17, and each  $T_m$  is also calculated by using eq.16. The result is shown in Fig.8. It is shown that the crystal field effect causes significant deviation from de-Gennes scaling. The calculated value becomes close to the experimental value.

The anisotropic coupling constant is shown in Fig.15.  $K_{\text{anis}}$ , which is induced by the dipole field from RE magnetic moments, is expressed as <sup>19)</sup>

$$K_{\text{anis}} = - 11.1 \cdot \frac{\chi_f}{a^3} \quad (18)$$

where  $a$  is a lattice parameter. By using each  $\chi_f$  and lattice constant,  $K_{\text{anis}}$  is calculated and is shown in Fig.15.  $A_{\text{anis}}(\text{RE})$  is expressed by the dipolar contribution except RE=Sm. In  $\text{SmRh}_4\text{B}_4$ , Knight shift is measured at low temperature ( 1.2K ~ 10K ), where  $K_{\text{anis}}$  is about 4.6 times larger than the dipolar contribution. This suggests that the anisotropy of the static susceptibility also induces the anisotropic shift via the uniform spin polarization,

$$\begin{aligned} K_{\text{anis}} &= A_{\text{iso}} \cdot \chi_{\text{anis}} \\ \chi_{\text{anis}} &= 2/3 \cdot (\chi_{\parallel} - \chi_{\perp}) \end{aligned} \quad (19)$$

where  $\chi_{\parallel}$  and  $\chi_{\perp}$  are parallel and perpendicular component of  $\chi$  to the tetragonal c-axis respectively. In order to explain the anisotropy by the contribution from  $\chi_{\text{anis}}$ , we have to take  $\chi_{\perp} / \chi_{\parallel}$  to be 7.5. ( $\chi_{\perp}$  is much larger than  $\chi_{\parallel}$ ) As  $B_2^0$  for  $\text{Sm}^{3+}$  is negative in  $\text{SmRh}_4\text{B}_4$ , the easy axis of Sm moments may be in a-b plane and anisotropy of  $\chi$  appears. On the other hand in other  $\text{RERh}_4\text{B}_4$ , Knight shift is measured at 300K and nearly all the energy levels of  $J_2$  are thermally excited. Then  $K_{\text{anis}}$  may be explained only by the contribution from the dipole field.

( 2- 2 ) Knight shift of  $^{103}\text{Rh}$  in  $\text{SmRh}_4\text{B}_4$

In Sm compound, we observed  $^{103}\text{Rh}$  NMR in the paramagnetic state. The spin echo spectrum at 2.25 K is shown in Fig.16. The spectrum is broadened and the anisotropy of the spectrum is smeared by rf pulse. The shift is determined at the peak of the spectrum, and is shown in Fig.17 against the susceptibility data.  $^{23)} K_{\text{iso}}$  is linear in  $\chi_f(T)$  and the slope in  $K_{\text{iso}}$  vs  $\chi$  plot yields the hyperfine coupling constant of  $^{103}\text{Rh}$ ,  $[A_{\text{iso}}(\text{Sm})]_{\text{Rh}} = 1 \text{ kOe}$ . The observed hyperfine field is a sum of s- and d- part of contribution. We tentatively try to separate the conduction electron spin polarization. Assuming that the difference of  $(A_{\text{iso}})_{\text{Rh}}^s$  and  $[A_{\text{iso}}]_{\text{B}}^s$  is owing to the difference of the hyperfine coupling const. and the density of states, we estimate  $[A_{\text{iso}}(\text{Sm})]_{\text{Rh}}^s$  as

$$[A_{\text{iso}}(\text{Sm})]_{\text{Rh}}^s = [A_{\text{iso}}(\text{Sm})]_{\text{B}}^s \cdot \frac{[N_s(E_F)]_{\text{Rh}}^s}{[N_s(E_F)]_{\text{B}}^s} \cdot \frac{(H_{\text{Rh}}^s)_{\text{atom}}}{(H_{\text{B}}^s)_{\text{atom}}} \quad (20)$$

$$= 31 \text{ kOe}/\mu_B$$

where  $(H_{\text{Rh}}^s)_{\text{atom}} = 4.79 \times 10^6 \text{ Oe}$   $^{24)}$  and  $(H_{\text{B}}^s)_{\text{atom}} = 1.0 \times 10^6 \text{ Oe}$   $^{16)}$ . Then the contribution from d- electron is estimated as

$$[A_{\text{iso}}(\text{Sm})]_{\text{Rh}}^d = [A_{\text{iso}}(\text{Sm})]_{\text{Rh}} - [A_{\text{iso}}(\text{Sm})]_{\text{Rh}}^s \quad (21)$$

$$= - 30 \text{ kOe}/\mu_B$$

$[A_{\text{iso}}]_{\text{Rh}}^s$  and  $[A_{\text{iso}}]_{\text{Rh}}^d$  are much larger than the observed coupling constant and are nearly cancelled. In a uniform polarized model ( eq.12),  $J_{\text{df}} N_d(E_F)$  is estimated as

$$J_{\text{df}} N_d(E_F) = - 0.23 \text{ state/ atom spin} ,$$

where  $(H_{\text{Rh}}^d)_{\text{cp}} = - 0.12 \times 10^6$  is assumed.

This value is larger than  $JN(E_F) \approx 0.1$  state/atom spin at RE site obtained from Korringa fluctuation of RE moments. If  $(A_{iso})_{Rh}^s$  is smaller than the expected value,  $(A_{iso})_{Rh}^d$  and  $J_{df}N_d(E_F)$  at Rh site becomes smaller. However  $(A_{iso})_{Rh}^s$  has at least the same magnitude as  $(A_{iso})_{Rh}^d$ . Even then  $J_{df}N_d(E_F)$  at Rh site is an order of magnitude larger than that found in Chevrel phase compounds.

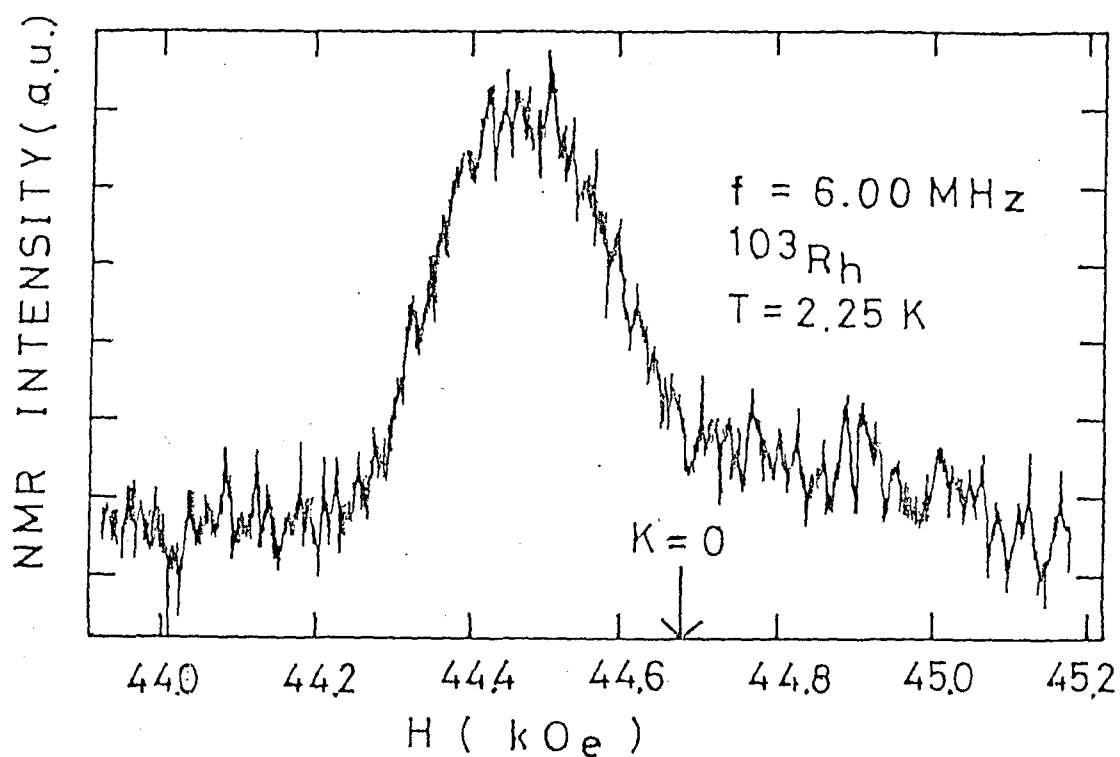


Fig.16 NMR spectrum of  $^{103}\text{Rh}$  in  $\text{SmRh}_4\text{B}_4$ . The positive shift appears.

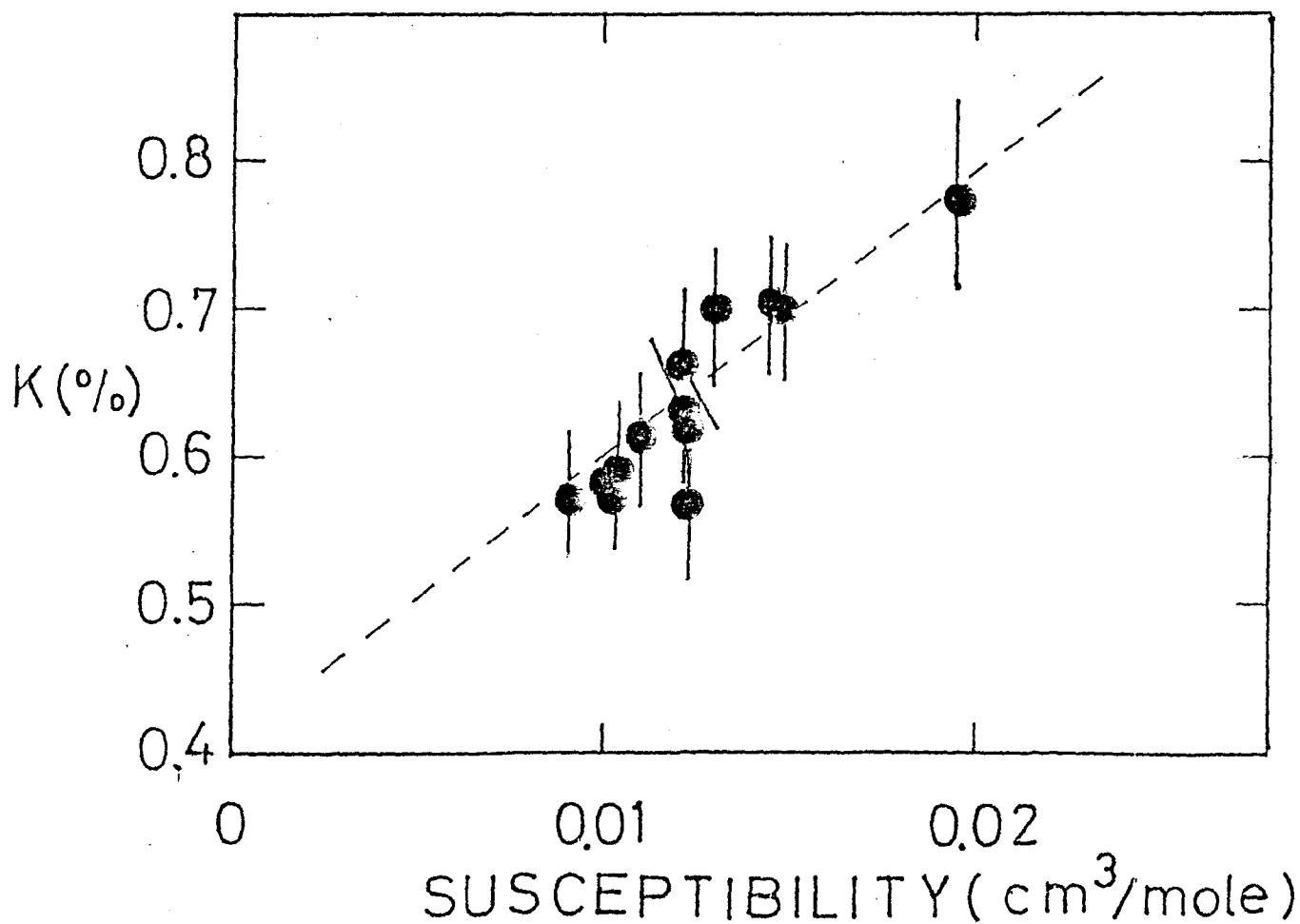


Fig.17 The isotropic shift of  $^{103}\text{Rh}$  in  $\text{SmRh}_4\text{B}_4$  vs susceptibility.



( 3 ) NMR spectra of  $^{11}\text{B}$  in the magnetically ordered state

( ferromagnetic compounds )

In the magnetically ordered state, zero field NMR of  $^{11}\text{B}$  was observed<sup>25)</sup> in ferromagnetic compounds. We obtain information about the magnetic structure in these compounds using the hyperfine field data.

The hyperfine field of  $^{11}\text{B}$  in ferromagnetic compound may be expressed as a sum of the dipole field from the surrounding RE ions, the hyperfine field due to the conduction electron spin polarization and the Lorentz field due to the magnetization of RE moments .

$$H_{\text{hf}} = H_{\text{dip}} + H_{\text{cond}} + H_{\text{L}} \quad ( 22 )$$

Each contribution is calculated by the following procedure. The magnetic moments are directed to c-axis for  $\text{HoRh}_4\text{B}_4$  and ab plane for  $\text{ErRh}_4\text{B}_4$  according to the neutron diffraction measurement. Assuming that the magnetic moments in Gd, Tb and Dy compounds are aligned along c-axis, one can calculate the hyperfine fields. The values of the magnetic moments in Dy-, Ho and Gd- compound are found to be  $9.2\mu_{\text{B}}$  from Mössbauer effect by Shenoy et al.,<sup>26)</sup>  $8.7\mu_{\text{B}}$  from neutron diffraction by Mook et al<sup>27)</sup> and  $7\mu_{\text{B}}$  respectively. As for the classical dipole field at B site, one calculates the value from the first nearest-neighbor RE site in the distance of about  $70 \text{ \AA}$  around B.  $H_{\text{cond}}$  was calculated by using  $(g_{\text{J}}-1)J$  of RE and the hyperfine coupling constant for  $^{11}\text{B}$ , which was obtained from the Knight shift measurement. The Lorentz field  $4/3 \cdot \pi M$  was obtained by using the measured magnetic moment and the lattice constant. Each component contributing to  $H_{\text{hf}}$  is shown schematically with its direction in Fig.18. The measured  $H_{\text{hf}}$ , the total calculated  $H_{\text{hf}}$ , the dipole fields parallel and perpendicular to the magnetic moment  $H_{\text{dip}\parallel}$  and  $H_{\text{dip}\perp}$ ,  $H_{\text{L}}$  and  $H_{\text{cond}}$  are shown in Table 4. As shown in this table , the calculated  $H_{\text{hf}}$  of these compounds are in reasonable agreement with the measured values.

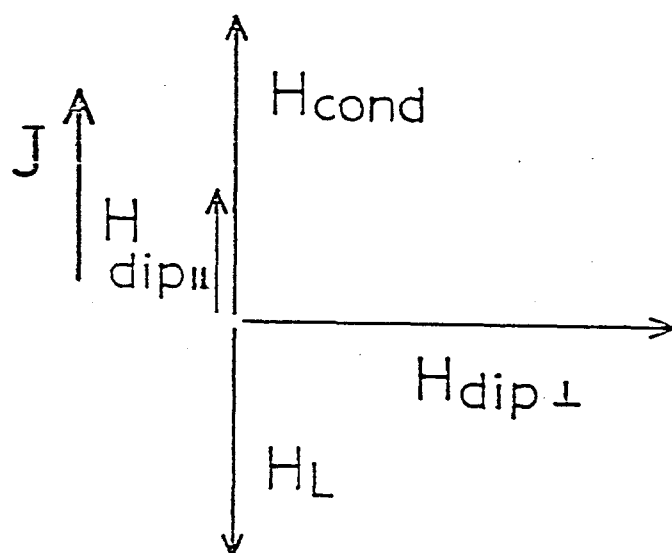


Fig. 18 The direction of each component of  $H_{hf}$  at B site relative to the total angular momentum  $J$ . The marks of  $H_{dip||}$  and  $H_{dip\perp}$  show the parallel and perpendicular component with respect to magnetization

Table 4

The measured  $H_{hf}$  and the calculated  $H_{hf}$  at B site.

$R_E$	$H_{hf}$ meas (kOe)	$H_{hf}$ calc (kOe)	$H_{dip\perp}$	$H_{dip  }$	$H_{cond}$	$H_L$
Gd	3.15	3.55	3.21	0.28	3.86	2.62
Dy	4.69	4.26	4.25	0.38	2.76	3.44
Ho	4.61	4.56	4.04	0.35	2.21	3.25
Tb	3.9					

( 4 ) Nuclear spin lattice relaxation rates of  $^{11}\text{B}$

The fluctuation of RE moments enhances  $T_1^{-1}$  of  $^{11}\text{B}$  through the RKKY coupling and the magnetic dipole coupling between RE spin and  $^{11}\text{B}$ . Then  $T_1$  of  $^{11}\text{B}$  provides informations about the origin of RE spin fluctuation; the s-f exchange interaction of RE spin and conduction electrons, the indirect coupling of the each RE spin and also the crystal field effect on the RE spin.

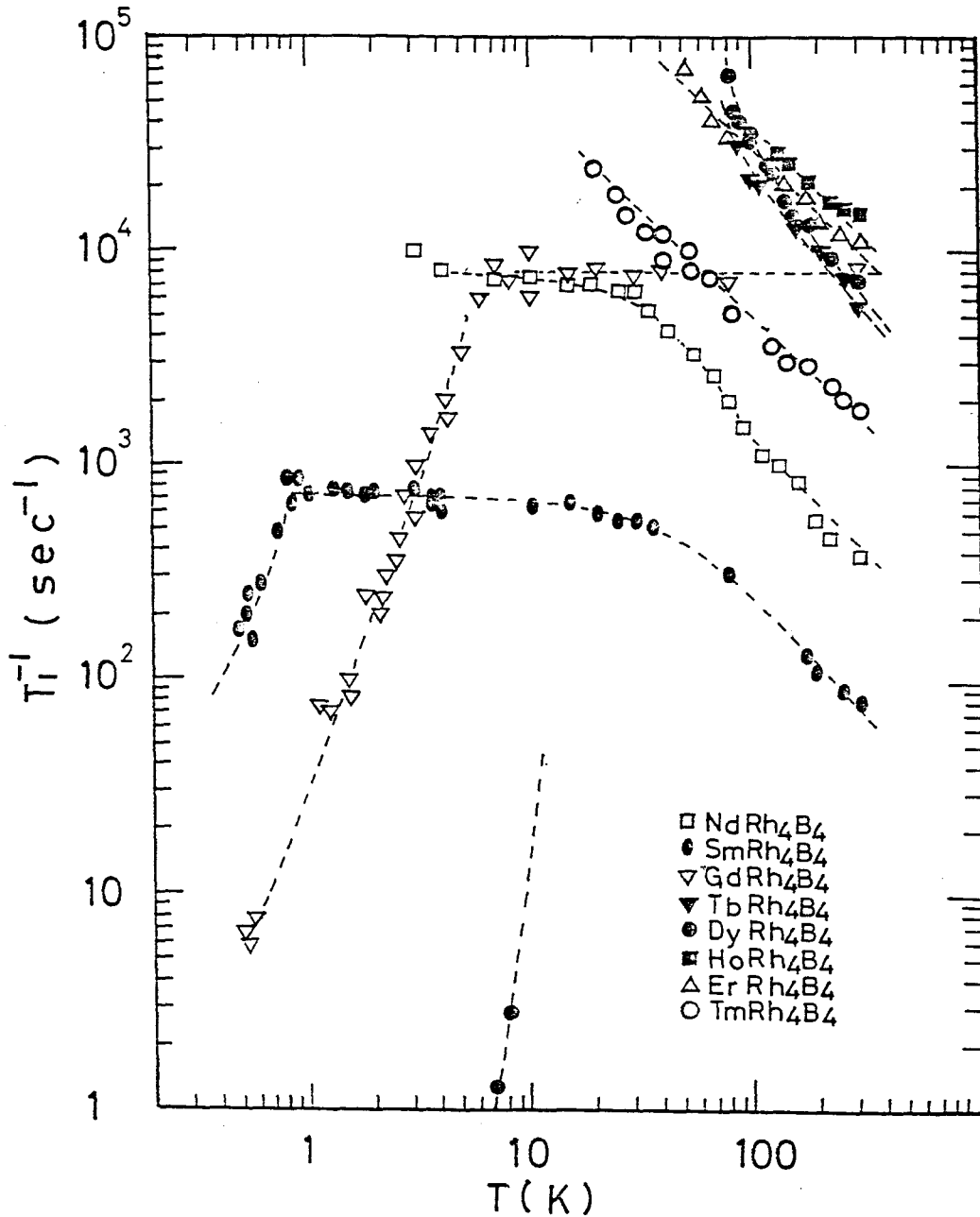


Fig.19 The temperature dependence of  $T_1^{-1}$  of  $^{11}\text{B}$  in  $\text{RERh}_4\text{B}_4$ .

$T_1$  is expressed as

$$T_1^{-1} \propto \gamma_n^2 \cdot H_{loc}^2 \cdot \frac{\tau}{1 + (\omega_n \tau)^2} \quad (23)$$

where  $\gamma_n$  is the gyromagnetic ratio of  $^{11}\text{B}$ ,  $H_{loc}$  is the coupling of B nucleus and RE spin (RKKY and/or dipole coupling),  $\omega_n$  is the nuclear Larmor frequency and  $\tau$  is the electronic spin correlation time, which is determined by the Korringa spin fluctuation of RE spin or RKKY indirect coupling of RE spin.

The temperature dependence of  $T_1$  of  $^{11}\text{B}$  in  $\text{RERh}_4\text{B}_4$  is shown in Fig.19. At high temperature  $T_1^{-1}$  decreases with increasing temperature (except  $\text{GdRh}_4\text{B}_4$ ).  $T_1$  is nearly proportional to  $T$  and field dependence is not observed. This behavior is widely seen in most of the compounds (except  $\text{GdRh}_4\text{B}_4$ ). In this case the Korringa relaxation of the electronic spins via the s-f exchange interaction governs the RE spin fluctuation.

The temperature dependence of  $T_1$  at low temperature depends on RE species. In Gd-, Nd-, and Sm- based compound  $T_1$  is temperature independent. This behavior suggests that the exchange interaction between Gd spins (RKKY coupling) is responsible for the electronic spin correlation time,  $\tau$ .

In Dy- based compound,  $T_1^{-1}$  increases with decreasing temperature and then decreases exponentially at low temperature,

$$T_1^{-1} \propto \exp(-\Delta/k_B T) \quad \text{with } \Delta \approx 130\text{K}$$

This means that  $\tau$  changes in proportional to  $\exp(-\Delta/k_B T)$  at low temperature.

As discussed in the previous section RE ion experiences the relatively large crystal field in  $\text{RERh}_4\text{B}_4$ . For example, the Schottky anomalies in specific heat indicate the crystal field effect on RE ions.  $T_1$  is also affected by the crystal field effect and is especially sensitive to the ground state at low temperature. In Dy-based compound, the RE spin fluctuation is suppressed by the crystal field.

( 4-1 )  $T_1$  of  $^{11}\text{B}$  in  $\text{GdRh}_4\text{B}_4$

First we consider  $T_1$  in  $\text{GdRh}_4\text{B}_4$ . As Gd, an  $L=0$  ion, is not affected by the crystal field effect, the behavior of  $T_1$  is simplest in  $\text{RERh}_4\text{B}_4$ . In the paramagnetic state  $T_1$  is nearly temperature independent between 8K and 300K, being 125 $\mu\text{sec}$  which is smaller by about four orders of magnitude compared with that in non-magnetic  $\text{LuRh}_4\text{B}_4$ . ( $T_1 T = 55\text{secK}$  in  $\text{LuRh}_4\text{B}_4$ . This value is due to the direct relaxation to the conduction electron at B site.) This means that the exchange interaction between Gd spins to be responsible for the fluctuation of the Gd spins.  $T_1$  of  $^{11}\text{B}$  due to the magnetic dipole interaction between  $\text{Gd}^{3+}$  spin and  $^{11}\text{B}$  nuclear spin is expressed as <sup>28)</sup>

$$T_1^{-1} = \frac{\sqrt{2\pi} \gamma_e^2 \gamma_n^2 \hbar^2}{6 \omega_e} \cdot S(S+1) \cdot \sum_1 r_1^{-6} [F_1(\alpha \beta \gamma) + F_1'(\alpha \beta \gamma)] \quad (24)$$

where  $\omega_e$  is the exchange frequency,  $\gamma_e$  is the gyromagnetic ratio of the electrons,  $r_1$  is the distance between  $^{11}\text{B}$  and Gd ion and  $S$  is the spin number.  $F_1$  and  $F_1'$  are the functions of the direction cosine of the local magnetic field of the nucleus,  $\alpha, \beta, \gamma$ . We replace  $F_1$  and  $F_1'$  by their directional average,  $\langle F_1 \rangle$  and  $\langle F_1' \rangle$ , as they are not so sensitive to the direction. Then eq. 24 is expressed as

$$T_1^{-1} = \frac{2 \sqrt{2\pi} \gamma_e^2 \gamma_n^2 \hbar^2}{3 \omega_e} S(S+1) \sum_1 r_1^{-6} \quad (25)$$

We estimate  $\omega_e$  from the Curie temperature  $T_c$ . Gd spin is in s-state, not affected by the crystal field effect. The contribution to  $T_c$  from the dipole coupling is order of 0.25K ( $M = 7\mu_B, r = 5\text{\AA}$ ), which is smaller than the experimental value. Then  $T_c$  is determined mainly by RKKY exchange coupling.

$$(\hbar \omega_e)^2 = \frac{1}{6z} \cdot \frac{(3k_B T_c)^2}{S(S+1)} \quad (26)$$

Putting eq.26 into eq.25,  $T_1$  is estimated to be 25 $\mu$ sec.

In addition to the dipole coupling, the coupling between  $^{11}\text{B}$  and Gd spin via the conduction electron spin polarization also contributes to  $T_1^{-1}$ . This value may be estimated by the relation <sup>29)</sup>

$$T_1^{-1} = \sqrt{2\pi} \sum_i \left( \frac{A_i}{\hbar} \right)^2 \frac{S(S+1)}{3\omega_e} \quad (27)$$

where  $A_i$  is a hyperfine coupling constant between  $^{11}\text{B}$  and  $i$ -th Gd spin via the conduction electron spin polarization. Although we have no knowledge about  $A_i$ , we tentatively try to estimate  $A_i$  from the isotropic Knight shift. Assuming roughly that  $T_1$  is caused by nearest neighbor 3 Gd moments,  $A_i$  is estimated as  $3.3 \times 10^{-21}$  erg and  $T_1$  is calculated to be 167 $\mu$ sec, which is longer than the value due to the dipole interaction. Thus in  $\text{GdRh}_4\text{B}_4$   $T_1$  seems to be governed by the fluctuations of the dipole field from the Gd spins.

When the system sets into ferromagnetic state,  $T_1^{-1}$  decreases rapidly with decreasing temperature, as the spin fluctuations are suppressed.

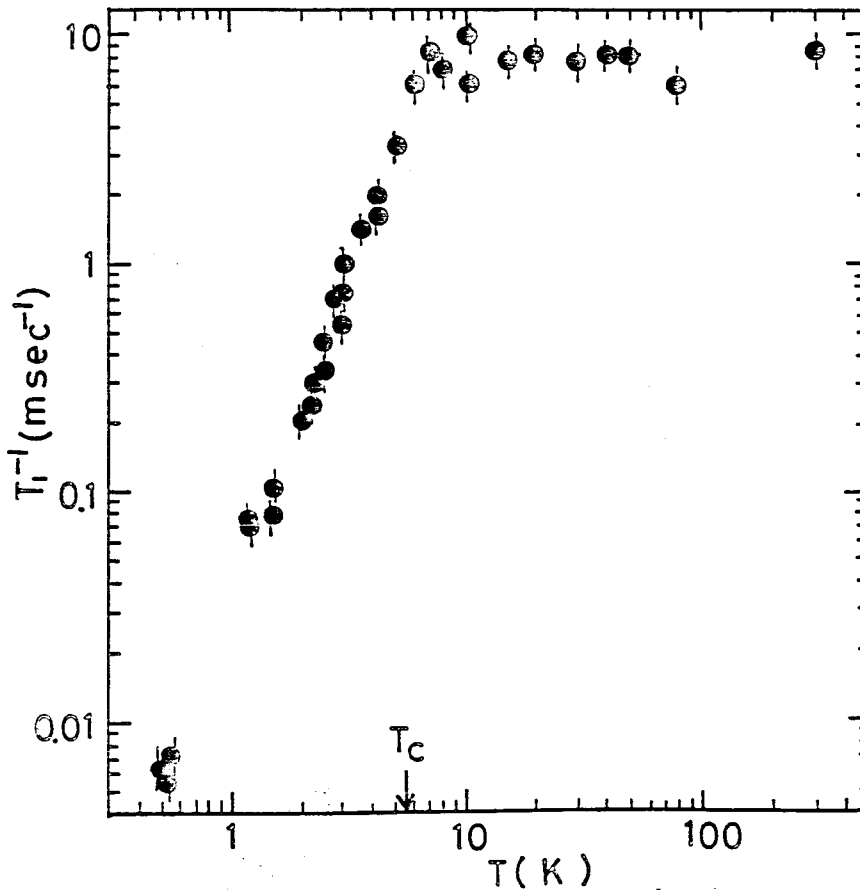


Fig. 20 Temperature dependence of  $T_1^{-1}$  of  $^{11}\text{B}$  in  $\text{GdRh}_4\text{B}_4$ .

( 4-2 )  $T_1$  of  $^{11}\text{B}$  in  $\text{RERh}_4\text{B}_4$  — high temperature

As shown in Fig.19  $T_1$  is nearly proportional to  $T$  at high temperature in most of the compounds. In this case the Korringa relaxation of the electronic spins via the s-f exchange interaction is responsible for the fluctuation of RE moment. The relaxation rate  $W$  is expressed as <sup>30)</sup>

$$W = \frac{2\pi}{\hbar} \cdot (g_j - 1)^2 [J N(E_F)]^2 k_B T \quad (28)$$

where  $J$  is the s-f and/or d-f exchange interaction, and  $N(E_F)$  is the density of state at RE site.

In this region  $T_1$  due to the dipole coupling between RE and  $^{11}\text{B}$  is expressed as

$$T_1^{-1} = \frac{2\gamma_e^2 \gamma_n^2 \hbar^2}{3W} g_j^2 J(J+1) \sum_1 r_1^{-6}, \quad (29)$$

$$\propto \frac{g_j^2 J(J+1)}{(g_j - 1)^2},$$

while that due to RKKY coupling is expressed as

$$T_1^{-1} = \frac{S(S+1)}{3W} \cdot \sum_1 \left( \frac{A_1}{\hbar} \right)^2, \quad (30)$$

$$\propto J(J+1),$$

The RE dependence of the observed relaxation rate is shown in Fig.21. The RE dependence of  $(T_1)_{\text{dipole}}$  and  $(T_1)_{\text{RKKY}}$  is also shown in Fig.21, where  $J N(E_F)$  is assumed to be independent of RE species. The strong RE dependence is observed in  $(T_1)_{\text{dipole}}$ , which is similar to the observed  $T_1$ , while the RE dependence of  $(T_1)_{\text{RKKY}}$  is weak. If one assumes that the hyperfine field  $A_1$  arises from 3 neighboring RE moment,  $[T_1(\text{Sm})]_{\text{RKKY}}$  is 2 times shorter than  $[T_1(\text{Sm})]_{\text{dipole}}$ , while  $(T_1)_{\text{dipole}}$  is shorter than  $(T_1)_{\text{RKKY}}$  in other RE based compounds.

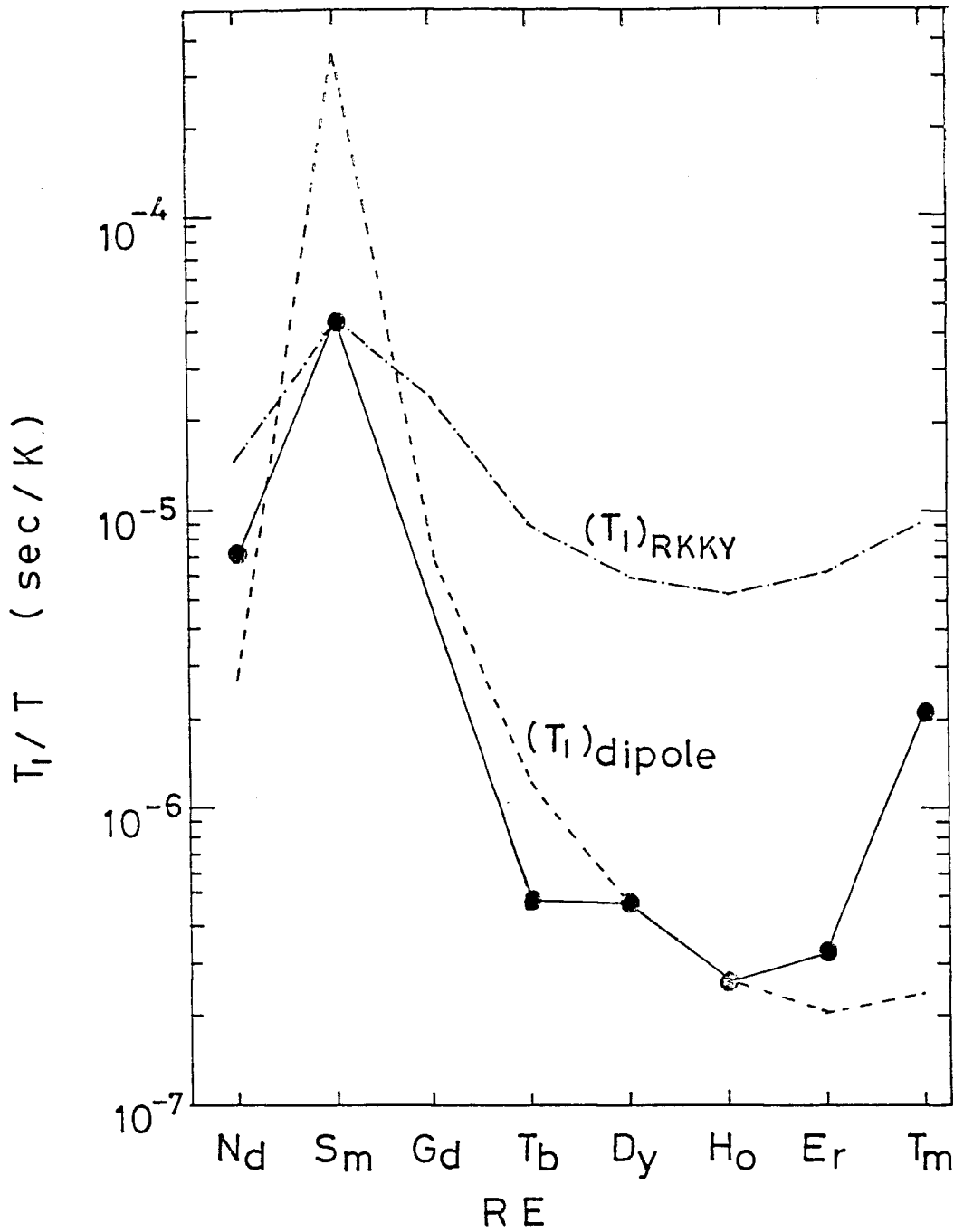


Fig.21 The RE dependence of  $T_1$  at high temperature.

(  $T_1$  is determined by Korringa relaxation of the RE spins.)

$T_1$  due to dipole coupling and RKKY coupling are also shown on the assumption of  $JN(E_F)$  being independent of RE.  $T_1$  due to dipole coupling is normalized by RE = Dy.  $T_1$  due to RKKY coupling is normalized by RE = Sm. This value corresponds to the maximum RKKY coupling constant.



So it seems natural to conclude as following.

Even if  $T_1(\text{Sm})$  is determined by RKKY interaction, which gives the maximum RKKY coupling constant,  $T_1$  in other RE based compounds is governed by the dipole coupling. Then we obtain  $J N(E_F)$  at RE site from the experimental relaxation rate by using eq.28 , eq.29 and  $\gamma_e^2 h^2 S(S+1) = \mu_{\text{eff}}^2 \times \mu_B^2$ . The obtained  $J N(E_F)$  is shown in Table 5.

Table 5 Value of  $J N(E_F)$  in  $\text{RERh}_4\text{B}_4$

Compound	$J N(E_F)$ [ state/atom-spin ]
$\text{NdRh}_4\text{B}_4$	0.16
$\text{TbRh}_4\text{B}_4$	0.064
$\text{DyRh}_4\text{B}_4$	0.10
$\text{HoRh}_4\text{B}_4$	0.10
$\text{ErRh}_4\text{B}_4$	0.13
$\text{TmRh}_4\text{B}_4$	0.30

These values obtained in  $\text{RERh}_4\text{B}_4$  are compared with those in Chevrel compounds. <sup>34)</sup>

Table 6 Value of  $J N(E_F)$  in Chevrel compound

Compound	$J N(E_F)$ [ state/atom-spin ]
$\text{Eu}_{0.25}\text{Sn}_{0.75}\text{Mo}_6\text{S}_8$	0.0033
$\text{GdMo}_6\text{S}_8$	0.0047
1% Gd in $\text{SnMo}_6\text{S}_8$	0.0061
0.91% Gd in $\text{SnMo}_6\text{S}_8$	0.0050

The conduction electron spin polarization in  $\text{RERh}_4\text{B}_4$  is about 20 times larger than that in Chevrel compounds.

( 4-3 )  $T_1$  of  $^{11}\text{B}$  in  $\text{RERh}_4\text{B}_4$  ——— low temperature

Non-S RE ions experiences a relatively large crystal field in  $\text{RERh}_4\text{B}_4$ . For example, the Schottky anomalies in specific heat indicate the crystal field effect on RE ions. Recently, Dunlap and Niarchos studied the crystal field effect in  $\text{RERh}_4\text{B}_4$  by analysis of a large amount of available data. Their result is shown in appendix. ( In their paper the energy spacing of  $|J_z\rangle$  is not published, as it has still ambiguity.)

$T_1$  is affected by the crystal field effect and is especially sensitive to the ground state at low temperature. For Dy- based rhodium boride the ground state consists of  $|\pm 15/2\rangle$  and the first excited state is  $|\pm 13/2\rangle$  located by about 130 K above the ground state:  $|\Delta m_J|=1$  transitions are forbidden at low temperature. Then the spin fluctuations associated with the spin-spin interaction (RKKY interaction) and/or s-f exchange interaction are suppressed at low temperature. The spin correlation time  $\tau$  changes as follows.

1) When  $\tau$  is determined by RKKY coupling

$$\tau^{-1} \propto \langle |m_f| J_{\pm} |m_i\rangle^2 \propto \exp(-\Delta'/k_B T) \quad (31)$$

2) When  $\tau$  is determined by Korringa mechanism

$$\begin{aligned} \tau^{-1} &\propto W_{\pm} \propto \langle f | J_{\pm} | i \rangle^2 \cdot \int f(E_i) \cdot [1 - f(E_i \mp \Delta')] \cdot dE_i \\ &\propto \Delta' \cdot \frac{\exp(\mp \Delta'/k_B T)}{\exp(\mp \Delta'/k_B T) - 1} \end{aligned}$$

which gives

$$\begin{cases} W_{\pm} \propto k_B T & \text{for } \Delta' \ll k_B T \\ \tau^{-1} \propto T & \end{cases} \quad (32)$$

while

$$\begin{cases} W_{+} \propto \exp(-\Delta'/k_B T) \\ W_{-} \propto \Delta' \\ \tau^{-1} \propto \exp(-\Delta'/k_B T) \end{cases} \quad \text{for } \Delta' \gg k_B T$$

Thus

$$T_1 \propto H_{\text{loc}}^2 \cdot \frac{\tau}{1 + (\omega_n \tau)^2} \quad (33)$$

$$\propto H_{\text{loc}}^2 \cdot \tau \quad \text{for } \omega_n \tau \ll 1 \quad (\text{fast limit})$$

$$\text{while } \propto H_{\text{loc}}^2 / (\omega_n^2 \tau) \quad \text{for } \omega_n \tau \gg 1 \quad (\text{slow limit})$$

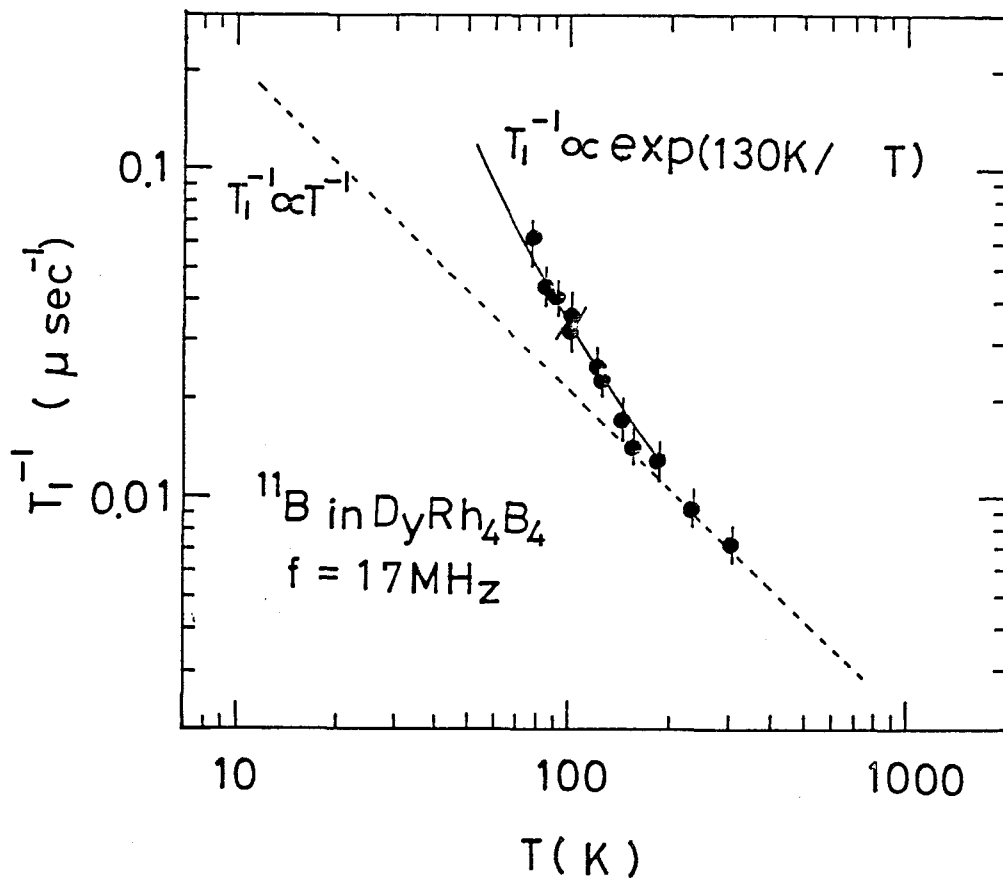


Fig. 22 The temperature dependence of  $T_1^{-1}$  of  $^{11}\text{B}$  in  $\text{DyRh}_4\text{B}_4$ . The system is in fast limit region. The external magnetic field is 12.4 kOe.

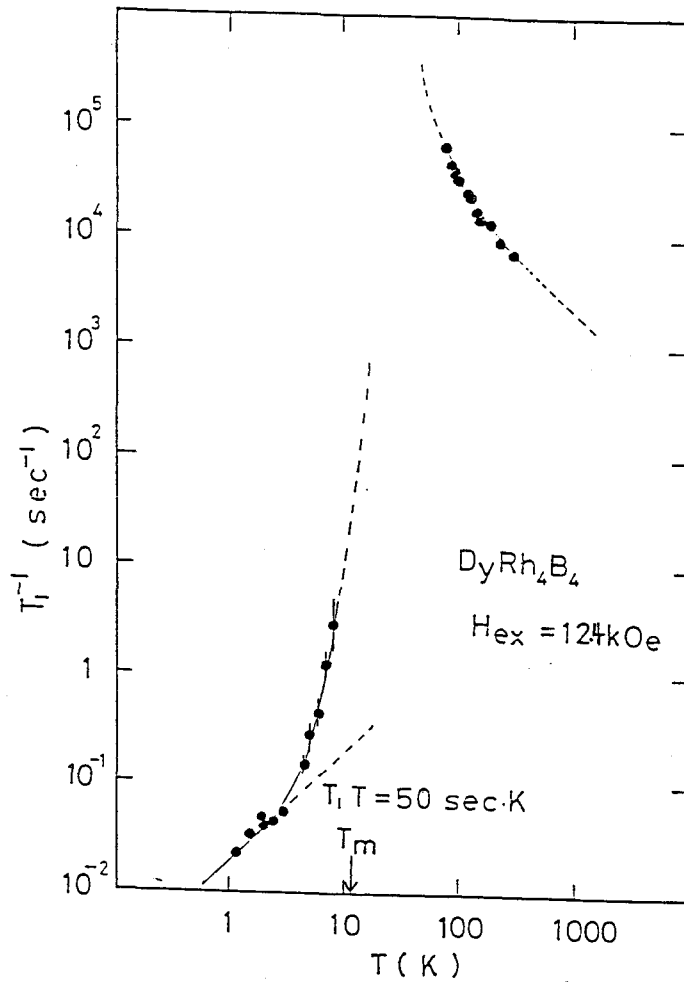


Fig.23 The temperature dependence of  $T_1^{-1}$  in  $\text{DyRh}_4\text{B}_4$ . At 1.2K  $T_1$  becomes about  $10^6$  times longer than  $T_1$  at 80K.

Then  $T_1$  of  $^{11}\text{B}$  changes exponentially in fast region as shown in Fig.22.

$$T_1 \propto \exp(-\Delta'/k_B T)$$

where  $\Delta'$  means the energy separation between the ground state  $|\pm 15/2\rangle$  and the first excited state  $|\pm 13/2\rangle$ . The energy gap obtained experimentally is  $\Delta' = 130\text{K}$ . With further decreasing temperature,  $\tau$  becomes long and  $\omega_n \tau$  becomes larger than 1. (slow limit) Then  $T_1$  increases as  $\tau$  increases at low temperature. At 12K the system sets into ferromagnetically ordered state. Near  $T_C$   $T_1$  increases rapidly with decreasing temperature. Below 4K  $T_1$  is nearly proportional to  $T^{-1}$ ;  $T_1 T = 50 \text{ secK}$ , which is just the same as in non-magnetic  $\text{LuRh}_4\text{B}_4$ . In this temperature region the nuclear spin energy relaxes to the conduction electron at B site directly and the contribution from RE spin is negligible. At 1.2K  $T_1$  becomes about  $10^6$  times longer than  $T_1$  at 80K.

For Sm-based compound the ground state consists of  $|\pm 1/2\rangle$ , for Er-based compound the ground state consists of the linear combination of  $J_z$  wave functions of  $|\pm 5/2\rangle$ ,  $|\pm 3/2\rangle$  and  $|\pm 11/2\rangle$  and for Nd-based compound the ground state is the linear combination of  $|\pm 9/2\rangle$  and  $|\pm 1/2\rangle$ . These RE based compounds possess degenerate CFE ground states which are connected by  $|\Delta m_J| = 1$  transitions. The RE spin fluctuation associated with RKKY interaction and/or s-f exchange interaction is not suppressed in these RE based compounds.

Figure 19 and 24 show the temperature dependence of  $T_1^{-1}$ .

$T_1$  is temperature independent at low temperature (in paramagnetic state) for Sm and Nd based compound. The spin fluctuation associated with RKKY interaction is responsible for the temperature dependence, and their behavior is similar to that in  $\text{GdRh}_4\text{B}_4$ .

In  $\text{SmRh}_4\text{B}_4$   $T_1$  becomes long as the spin fluctuation of the Sm spin is quenched in magnetically ordered state, as shown in Fig.24. Below 0.3K  $T_1$  is

proportional to  $T^{-1}$  ( $T_1 T = 5 \text{ msecK}$ ) in the normal state. This value is very short compared with that in nonmagnetic  $\text{LuRh}_4\text{B}_4$  ( $T_1 T = 55 \text{ secK}$ ). Therefore, the indirect mechanism including the fluctuation of the Sm spin is considered to contribute to  $T_1$ : the indirect coupling between  $^{11}\text{B}$  and conduction electron (virtual excitation of) through the spin waves (Weger mechanism) contributes to  $T_1$  at sufficiently low temperature<sup>32)</sup>. In this mechanism  $T_1$  is proportional to  $T^{-1}$ . As the ground state is the degenerate  $|\pm 1/2\rangle$  the CFE does not yield the energy gap in spin wave dispersion in  $\text{SmRh}_4\text{B}_4$ . The anisotropy from the dipole coupling of nearest neighbor Sm is also small as Sm has small magnetic moment. Then the Weger mechanism is considered to contribute significantly to  $T_1$ .

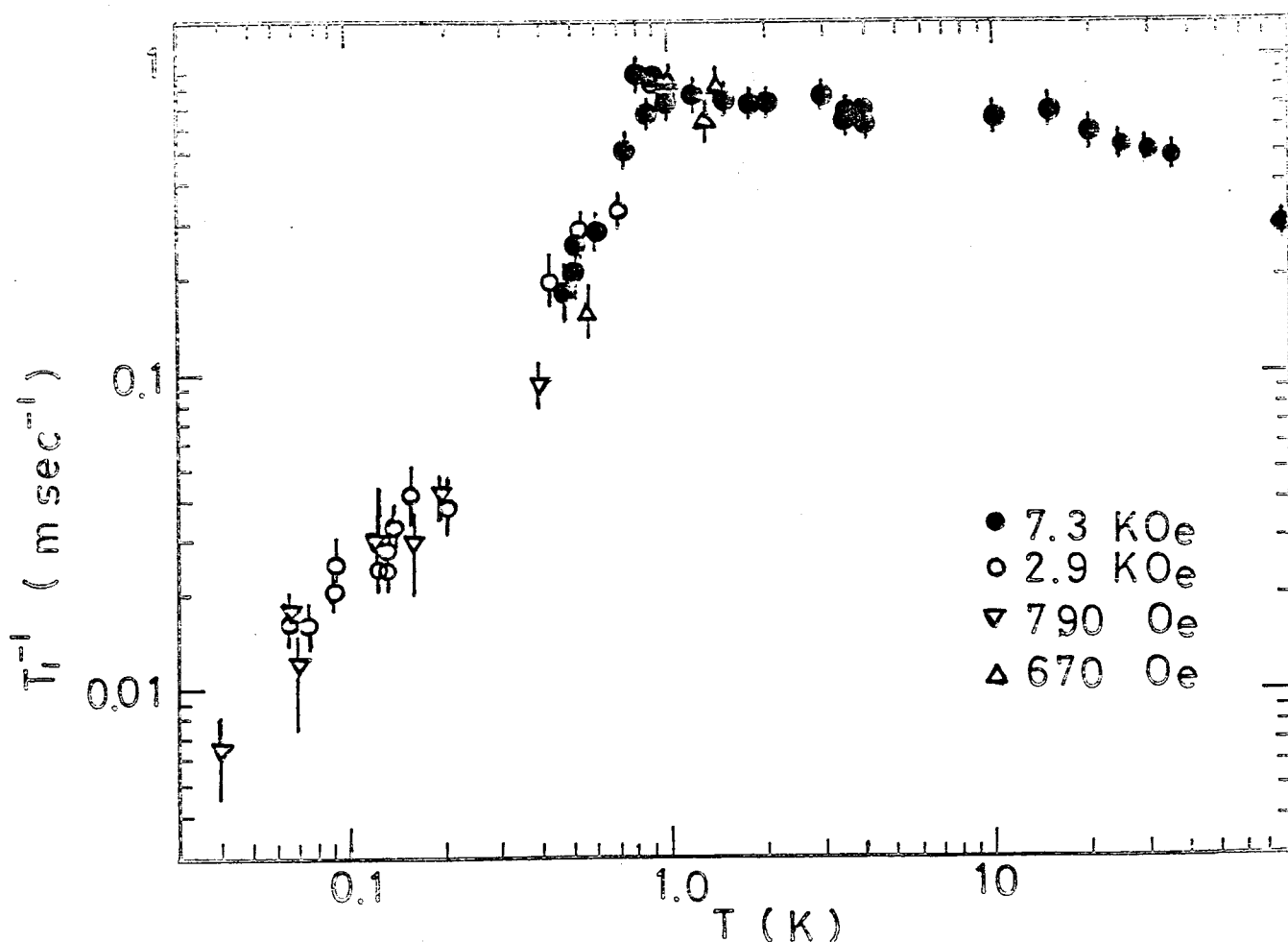


Fig. 24 Temperature dependence of  $T_1^{-1}$  of  $^{11}\text{B}$  in  $\text{SmRh}_4\text{B}_4$  below 80K.

## ( 5 ) Antiferromagnetic superconductor

The coexistence of the superconductivity and the antiferromagnetic order is proposed in  $\text{RERh}_4\text{B}_4$  ( RE = Nd, Sm and Tm ),  $\text{Ho}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$  and  $\text{Dy}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$ . We have obtained NMR spectra of  $^{11}\text{B}$  in magnetically ordered state in  $\text{SmRh}_4\text{B}_4$ ,  $\text{Ho}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$  and  $\text{Dy}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$ .

### ( 5-1 ) $\text{SmRh}_4\text{B}_4$

NMR spectra in  $\text{SmRh}_4\text{B}_4$  are shown in Fig.25 and Fig.10-2. Figure25 shows the spectrum in antiferromagnetic and superconducting mixed state.

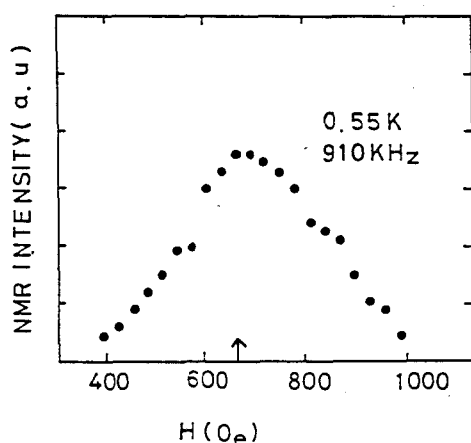


Fig.25 NMR spectrum of  $^{11}\text{B}$  in  $\text{SmRh}_4\text{B}_4$  at  $T = 0.5 \text{ K}$  and  $f = 910 \text{ kHz}$ . The system is in antiferromagnetic and superconducting state.

Figure 10-2 shows the spectrum in antiferromagnetic and normal state. There is no appreciable difference between the line width in superconducting mixed state and normal state. The line width due to the inhomogeneity of the internal field caused by the spatial distribution of vortices is negligibly small compared with the width due to the magnetic origin.

Figure 24 shows the temperature dependence of  $T_1$  in  $\text{SmRh}_4\text{B}_4$ . At 790 Oe and 670 Oe the system is in superconducting mixed state. Hence  $T_1$  is expected to increase exponentially in superconducting mixed state, when superconducting energy gap appears in the conduction electron band at Sm site. However, there is

no difference between  $T_1$  in the normal and superconducting mixed state as shown in Fig.24. In the present experimental condition,  $\text{SmRh}_4\text{B}_4$  seems to be gapless superconductor.

Comparing  $T_s$  of  $\text{LaRh}_4\text{B}_4$  and  $\text{LuRh}_4\text{B}_4$ , we may expect for  $T_s$  of  $\text{SmRh}_4\text{B}_4$  to be about 9 K.<sup>33)</sup> The actual  $T_s$  of  $\text{SmRh}_4\text{B}_4$  is 2.7 K. According to the theory of Abrikosov and Gor'kov on the depression of  $T_s$  by the magnetic impurity, the ratio  $T_s/T_{s0}$  of 0.3 corresponds to a normalized impurity concentration of  $n_i/n_{\text{crit}} = 0.85$ , where  $n_{\text{crit}}$  is a critical concentration for the occurrence of the superconductivity. In the theory, the depression of  $T_s$  by magnetic impurity is accompanied by a change in the excitation spectrum of the superconductor and always leads to a temperature region below  $T_s$  where gapless superconductivity occurs. In the case of  $T_s/T_{s0} = 0.3$  the gap is expected to appear below  $T/T_{s0} = 0.2$ ,  $T = 1.8$  K. Now external field also reduces the energy gap.  $\text{SmRh}_4\text{B}_4$  is considered to be a gapless superconductor above 700 Oe. If we perform the measurement in lower field, we may detect the appearance of the energy gap, although it is difficult to perform NMR study in lower field.

(5-2)  $\text{Ho}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$  and  $\text{Dy}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$

In  $\text{Ho}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$  and in  $\text{Dy}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$  the long range magnetic order and the superconductivity coexist at low temperature. In these compounds the magnetic ordering temperature is higher than the superconducting transition temperature. For Ho-based compound  $T_M = 2.7$  K and  $T_s = 1.4$  K and for Dy-based compound  $T_M = 4$  K and  $T_s = 1.2$  K. The magnetic structure of Ho-based compound is studied by neutron scattering and the result is shown in Fig.28,<sup>30)</sup> while the magnetic structure of Dy-based compound is not yet clear.

We observed the zero field NMR in these compounds. Figure 26 and 27 show  $^{11}\text{B}$  NMR in Dy-based compound at 1.5 K and Ho-based compound at 0.55 K, respectively.

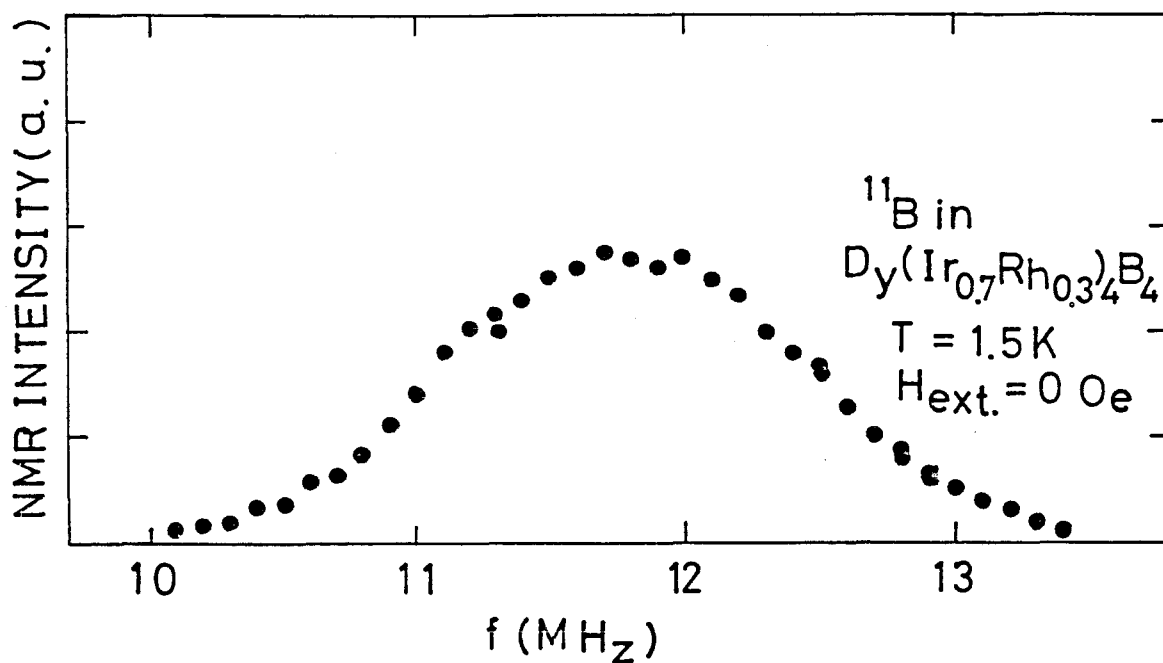


Fig. 26 The zero field NMR spectrum of  $^{11}\text{B}$  in  $\text{Dy}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$  at  $T = 1.5\text{ K}$ .  
The system is in antiferromagnetic and normal state.

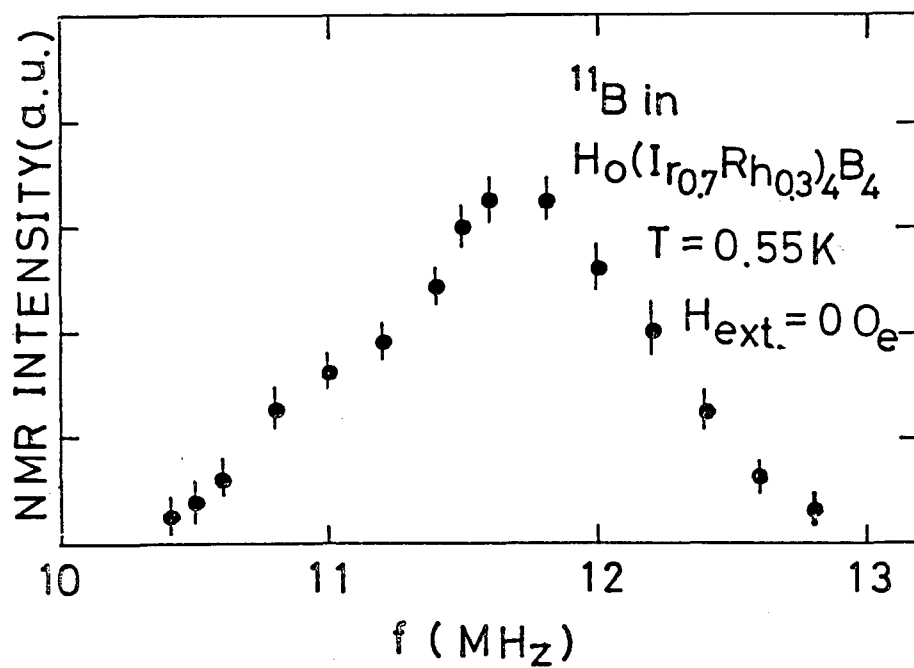


Fig.27 The zero field NMR spectrum of  $^{11}\text{B}$  in  $\text{Ho}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$  at  $T = 0.55\text{ K}$   
The system is in antiferromagnetic and superconducting state.



The internal field is 8.6 kOe for the compounds. In the antiferromagnetic compounds the contribution from RKKY coupling becomes small, hence the hyperfine field is determined by the dipole coupling. In Ho-based compound the contribution from the dipole field is 8.6 kOe, which is just the same value as the observed internal field. As the internal field in Dy-based compound is nearly equal to that in Ho-based compound, the magnetic structure in Dy-based compound is considered to be the same as in Ho-based compound.

As  $T_S$  and  $T_M$  in these compounds are higher than  $\text{SmRh}_4\text{B}_4$ , these compounds are good candidate for the study of energy gap, which is not definite in  $\text{SmRh}_4\text{B}_4$ .

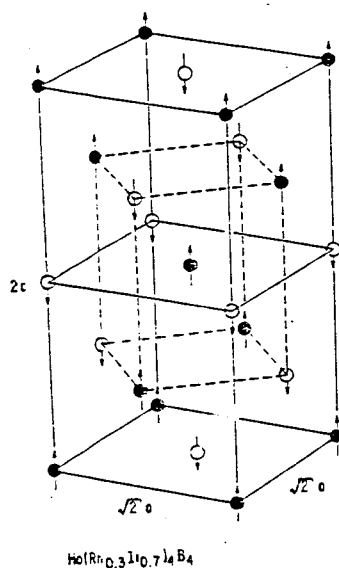


Fig.28 Proposed magnetic structure for  $\text{Ho}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$ . The crystallographic unit cell is outlined in dashed lines and the Rh, Ir and B atoms have been removed for clarity.

## §5 Conclusion

1) We have measured  $T_1^{-1}$  of  $^{89}\text{Y}$  (RE site),  $^{103}\text{Rh}$  and  $^{11}\text{B}$  in  $\text{YRh}_4\text{B}_4$  and  $\text{LuRh}_4\text{B}_4$  in order to investigate DOS at each atomic site in  $\text{RERh}_4\text{B}_4$ .

The observed  $T_1^{-1}$ 's are compared with the values, which are obtained by using the calculated DOS for  $\text{RERh}_4\text{B}_4$ .

The agreement of the experimental results with the band calculation is satisfactory for Y (RE) and Rh site.

Considerable reduction of DOS at RE site (Y site) in  $\text{RERh}_4\text{B}_4$  compared with pure RE metal has been observed, which is responsible for the weak coupling of RE spin and the superconducting electron at Rh site.  $T_1^{-1}$  of

$^{103}\text{Rh}$  shows a large DOS of d electron at Rh site, which means that Rh is responsible for the superconductivity.

2) We measured the isotropic and anisotropic Knight shift,  $K_{\text{iso}}$  and  $K_{\text{anis}}$ , of  $^{11}\text{B}$ .  $K_{\text{iso}}$  of  $^{11}\text{B}$  is proportional to the conduction electron spin polarization at B site. We found that it is proportional to  $(g_J - 1)J$  of each RE. Hence it is concluded that the conduction electron spin polarization induced by unit spin is nearly the same for all  $\text{RERh}_4\text{B}_4$ .  $K_{\text{anis}}$  of  $^{11}\text{B}$  is well explained by the dipole coupling between RE moments and  $^{11}\text{B}$  nucleus except in  $\text{SmRh}_4\text{B}_4$ . In  $\text{SmRh}_4\text{B}_4$ , the anisotropy of the susceptibility seems also to contribute to  $K_{\text{anis}}$  of  $^{11}\text{B}$ .

3) In order to estimate the exchange field on the superconducting electron, we have measured  $K_{\text{iso}}$  of  $^{103}\text{Rh}$ . The isotropic Knight shift arises from s- and d- part of the conduction electron spin polarization. We estimate s-part of the spin polarization at Rh site by assuming that the difference of s-part between B and Rh site is owing to the difference of the hyperfine coupling constant and DOS. Then d- part of the spin polarization is estimated by subtracting s-part from the observed value.

The s-f exchange effect on Rh is one order of magnitude larger than that in Chevrel compound.

4) The fluctuation of RE moments enhances  $T_1^{-1}$  of  $^{11}\text{B}$  through the magnetic dipole coupling and the RKKY coupling between RE spin and  $^{11}\text{B}$  nucleus. We obtained informations about the origin of RE spin fluctuations, the s-f exchange interaction of RE spin and the conduction electrons at RE site, the indirect coupling of each RE spin through RKKY interaction and also the CFE on the RE spin.

4-1) The s-f and/or d-f exchange interaction at RE site have been obtained from the Korringa spin fluctuation of RE spin. The obtained values are one order of magnitude larger than those found in Chevrel phase compound. This means that s-f exchange interaction play an important role in  $\text{RERh}_4\text{B}_4$  than in Chevrel phase compound.

4-2) Non-S RE ion experiences a relatively large CFE in  $\text{RERh}_4\text{B}_4$ , then the energy level of  $|J_z\rangle$  is lifted by the CFE. For Dy based compound, the first excited state  $|13/2\rangle$  has been found to be located by 130 K above the ground state  $|15/2\rangle$ . This energy spacing is much larger than the exchange interaction between RE ions, then the magnetic properties are much affected by the CFE. This circumstance is also same for all RE in  $\text{RERh}_4\text{B}_4$ .

5) We performed  $^{11}\text{B}$  NMR study of non-magnetic superconductor  $\text{LuRh}_4\text{B}_4$  in the superconducting mixed state.  $\text{LuRh}_4\text{B}_4$  is appropriate for the study of superconductivity in the compound without the influence of magnetic interaction or phase transitions. The obtained ratio of the energy gap to the superconducting critical temperature was found to be that of a weak coupling superconductor  $2\Delta(0)/k_B T_c = 3.5$ .

6) The superconductivity coexists with the antiferromagnetic long range order in  $\text{RERh}_4\text{B}_4$  ( RE = Nd, Sm and Tm ),  $\text{Ho}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$  and  $\text{Dy}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$ . We have obtained NMR spectra of  $^{11}\text{B}$  in magnetically ordered state in  $\text{SmRh}_4\text{B}_4$ ,  $\text{Ho}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$  and  $\text{Dy}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$ .

#### 6-1) $\text{SmRh}_4\text{B}_4$

Below 0.3 K,  $T_1$  is proportional to  $T^{-1}$  (  $T_1 T = 5 \text{ m sec K}$  ) in the normal state. This means that the Weger mechanism governs  $T_1$  at sufficiently low temperature. Thus the nuclear Zeeman energy of  $^{11}\text{B}$  relaxes to the conduction electron at RE site. Hence  $T_1$  is expected to increase exponentially in superconducting mixed state, when superconducting energy gap appears in the conduction electron band at Sm site. However, there is no difference between  $T_1$  in the normal state and superconducting mixed state above 790 Oe.  $\text{SmRh}_4\text{B}_4$  is considered to be a gapless or nearly gapless superconductor in the magnetic field of 790 Oe.

#### 6-2) $\text{Ho}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$ and $\text{Dy}(\text{Ir}_{0.7}\text{Rh}_{0.3})_4\text{B}_4$

We have observed the zero field  $^{11}\text{B}$  NMR in these compounds. This means the occurrence of the magnetic order in these compounds. For Ho-based compound, the antiferromagnetic order was found by neutron scattering, while the magnetism of Dy-based compound was not clear. From the hyperfine field analysis, we conclude that the magnetic structure in Dy-based compound is the same as in Ho-based compound.

As the superconducting temperature and the magnetic transition temperature in these compounds are higher than  $\text{SmRh}_4\text{B}_4$ , these compounds are good candidate for the study of the superconducting energy gap, which is not definite in  $\text{SmRh}_4\text{B}_4$ .

## Appendix

In  $\text{RERh}_4\text{B}_4$  compounds, the  $\overline{4}2m$  point symmetry for the rare-earth ion requires a crystal field Hamiltonian of the form

$$H_{\text{CF}} = B_2^0 O_2^0 + B_4^0 O_4^0 + B_4^4 O_4^4 + B_6^0 O_6^0 + B_6^4 O_6^4 \quad (\text{A-1})$$

where  $B_n^m$ 's are parameters to be determined empirically and  $O_n^m$ 's are Stevens operators. Customarily one writes

$$B_n^m = \alpha_n \langle r^n \rangle A_n^m, \quad (\text{A-2})$$

where  $\alpha_n$  is a Stevens factor whose value is known but dependent on the individual rare-earth ion under consideration and  $\langle r^n \rangle$  is a 4f radial integral obtained from Hartree-Fock atomic calculations. In this form,  $A_n^m$ 's are determined by the charge distribution in the lattice and are presumed to be approximately independent of the particular rare-earth ion in an isostructural series of compounds. Because of the presence of five unknown parameters in eq.A-1, two of which are multiplied by non-diagonal operators it is difficult to obtain reliable experimental parameters without extensive data and without a priori information on the parameters. Fortunately, in the present case both are available. A Mössbauer measurement of the electric field gradient at the Gd site in  $\text{GdRh}_4\text{B}_4$  has been interpreted to provide a value of  $A_2^0$  which, by use of eq A-2, gives  $B_2^0$  in  $\text{RERh}_4\text{B}_4$ . This is an important piece of data since the term in  $B_2^0$  is the largest term in the Hamiltonian.

In addition, single crystal magnetization data has recently been obtained for  $\text{ErRh}_4\text{B}_4$  both parallel and perpendicular to the tetragonal c-axis at various temperatures and fields. In polycrystalline sample, Schottky specific heat datum is available in  $\text{ErRh}_4\text{B}_4$ . All the data have been used in non-linear least-square fitting routine to eq.A-1 to obtain the crystal field

parameters, with the  $B_2^0$  value given above as a starting parameter. The results so obtained for  $\text{ErRh}_4\text{B}_4$  are  $B_2^0 = 0.769\text{K}$ ,  $B_4^0 = 0.13 \times 10^{-2}\text{K}$ ,  $B_4^4 = 0.619 \times 10^{-2}\text{K}$ ,  $B_6^0 = -0.139 \times 10^{-5}\text{K}$ , and  $B_6^4 = 0.352 \times 10^{-5}\text{K}$ . The signs of  $B_4^4$  and  $B_6^4$  are indeterminate due to the symmetry of the material. Also using the Er parameter given above in conjunction with eq.A-1 and eq.A-2, wavefunctions and eigenvalues have been computed for a number of rare-earth ions in  $\text{RERh}_4\text{B}_4$  compounds. The results are shown in Table A-1.

Table A-1 Crystal field schemes for (RE)Rh<sub>4</sub>B<sub>4</sub>

Nd<sup>3+</sup> in NdRh<sub>4</sub>B<sub>4</sub>

204.6  $\equiv$   $\psi_9 \psi_{10}$

180.3  $\equiv$   $\psi_7 \psi_8$

158.7  $\equiv$   $\psi_5 \psi_6$

119.6  $\equiv$   $\psi_3 \psi_4$

0  $\equiv$   $\psi_1 \psi_2$

Sm<sup>3+</sup> in SmRh<sub>4</sub>B<sub>4</sub>

291.9  $\equiv$   $\psi_5 \psi_6$

61.4  $\equiv$   $\psi_3 \psi_4$

0  $\equiv$   $\psi_1 \psi_2$

Dy<sup>3+</sup> in DyRh<sub>4</sub>B<sub>4</sub>

373.2  $\equiv$   $\psi_{15} \psi_{16}$

372.8  $\equiv$   $\psi_{13} \psi_{14}$

333.2  $\equiv$   $\psi_{11} \psi_{12}$

316.2  $\equiv$   $\psi_9 \psi_{10}$

281.0  $\equiv$   $\psi_7 \psi_8$

222.9  $\equiv$   $\psi_5 \psi_6$

131.4  $\equiv$   $\psi_3 \psi_4$

0  $\equiv$   $\psi_1 \psi_2$

$$\psi_1, \psi_2 = 0.997|\mp 9/2\rangle + 0.076|\mp 1/2\rangle$$

$$\psi_3, \psi_4 = -0.04|\mp 9/2\rangle + 0.34|\mp 1/2\rangle - 0.94|\pm 7/2\rangle$$

$$\psi_5, \psi_6 = 0.68|\mp 5/2\rangle + 0.73|\pm 3/2\rangle$$

$$\psi_7, \psi_8 = -0.07|\mp 9/2\rangle + 0.94|\mp 1/2\rangle - 0.34|\pm 7/2\rangle$$

$$\psi_9, \psi_{10} = -0.73|\mp 5/2\rangle + 0.68|\pm 3/2\rangle$$

$$\psi_1, \psi_2 = |\pm 1/2\rangle$$

$$\psi_3, \psi_4 = |\pm 3/2\rangle + 0.07|\mp 5/2\rangle$$

$$\psi_5, \psi_6 = |\mp 5/2\rangle + 0.07|\mp 3/2\rangle$$

$$\psi_1, \psi_2 = |\pm 15/2\rangle$$

$$\psi_3, \psi_4 = |\pm 13/2\rangle$$

$$\psi_5, \psi_6 = |\pm 11/2\rangle$$

$$\psi_7, \psi_8 = 0.98|\pm 9/2\rangle + 0.20|\pm 1/2\rangle$$

$$\psi_9, \psi_{10} = 0.94|\mp 7/2\rangle + 0.30|\pm 1/2\rangle - 0.14|\pm 9/2\rangle$$

$$\psi_{11}, \psi_{12} = 0.80|\mp 5/2\rangle + 0.59|\pm 3/2\rangle - 0.06|\pm 11/2\rangle$$

$$\psi_{13}, \psi_{14} = 0.93|\pm 1/2\rangle - 0.33|\mp 7/2\rangle - 0.16|\pm 9/2\rangle$$

$$\psi_{15}, \psi_{16} = 0.80|\pm 3/2\rangle - 0.59|\mp 5/2\rangle$$

Ho<sup>5+</sup> in HoRh<sub>4</sub>B<sub>4</sub>

		$\psi_1 = 0.70 8\rangle + 0.02 -4\rangle + 0.71 -8\rangle$
		$\psi_2 = 0.70 -8\rangle - 0.71 8\rangle$
155	$\psi_{17}$	
	$\psi_{15} \psi_{16}$	$\psi_3 \psi_4 =  ^+_{-7}\rangle$
	$\psi_{14}$	$\psi_5 = 0.70 -6\rangle - 0.70 6\rangle + 0.10 -2\rangle$
135.4	$\psi_{13}$	$\psi_6 = 0.69 -6\rangle + 0.16 -2\rangle + 0.16 2\rangle + 0.69 6\rangle$
132.1	$\psi_{11} \psi_{12}$	$\psi_7 \psi_8 = 0.84 \pm 5\rangle + 0.48 \pm 1\rangle + 0.24 \mp 3\rangle$
130.2	$\psi_{10}$	
121.3	$\psi_9$	$\psi_9 = 0.67 0\rangle + 0.53 4\rangle + 0.53 -4\rangle - 0.01 8\rangle - 0.01 -8\rangle$
116.6	$\psi_7 \psi_8$	$\psi_{10} = 0.69 2\rangle + 0.69 -2\rangle - 0.16 6\rangle - 0.16 -6\rangle$
96.0	$\psi_5 \psi_6$	$\psi_{11} \psi_{12} = 0.50 \pm 1\rangle + 0.71 \mp 3\rangle + 0.49 \pm 5\rangle$
		$\psi_{13} = 0.71 4\rangle - 0.71 -4\rangle$
56.5	$\psi_3 \psi_4$	$\psi_{14} = -0.47 4\rangle - 0.47 -4\rangle + 0.75 0\rangle$
		$\psi_{15} \psi_{16} = 0.66 \mp 3\rangle - 0.72 \pm 1\rangle + 0.22 \pm 5\rangle$
0	$\psi_1 \psi_2$	$\psi_{17} = 0.70 2\rangle - 0.70 -2\rangle$

Er<sup>5+</sup> in ErRh<sub>4</sub>B<sub>4</sub>

		$\psi_1 \psi_2 = 0.69 \mp 5/2\rangle - 0.71 \pm 3/2\rangle + 0.11 \pm 11/2\rangle$
146.9	$\psi_{15} \psi_{16}$	$\psi_3 \psi_4 = -0.61 \mp 7/2\rangle + 0.75 \pm 1/2\rangle - 0.24 \pm 9/2\rangle$
90.1	$\psi_{13} \psi_{14}$	$\psi_5 \psi_6 = 0.71 \mp 7/2\rangle + 0.39 \mp 1/2\rangle - 0.59 \pm 9/2\rangle$
		$\psi_7 \psi_8 = 0.71 \mp 5/2\rangle + 0.67 \pm 3/2\rangle - 0.20 \pm 11/2\rangle$
52.1	$\psi_{11} \psi_{12}$	$\psi_9 \psi_{10} = 0.35 \mp 7/2\rangle + 0.54 \pm 1/2\rangle + 0.77 \pm 9/2\rangle$
32.5	$\psi_9 \psi_{10}$	$\psi_{11} \psi_{12} = 0.22 \pm 3/2\rangle + 0.97 \pm 11/2\rangle$
22.8	$\psi_7 \psi_8$	$\psi_{13} \psi_{14} =  ^+_{-13/2}\rangle$
21.7	$\psi_5 \psi_6$	$\psi_{15} \psi_{16} =  ^+_{-15/2}\rangle$
2.1	$\psi_3 \psi_4$	
0	$\psi_1 \psi_2$	



$\text{Tm}^{3+}$ in $\text{TmRh}_4\text{B}_4$			
330.3	=====	$\psi_{12} \psi_{13}$	$\psi_1 = 0.98 0\rangle - 0.14 4\rangle - 0.14 -4\rangle$
			$\psi_2 \psi_3 = 0.94 \pm 1\rangle - 0.34 \mp 3\rangle$
186.1	=====	$\psi_{10} \psi_{11}$	$\psi_4 = -0.71 2\rangle + 0.71 -2\rangle$
103.2	—————	$\psi_9$	$\psi_5 = 0.71 2\rangle + 0.71 -2\rangle$
99.0	—————	$\psi_8$	$\psi_6 \psi_7 = 0.94 \mp 3\rangle + 0.34 \pm 1\rangle$
55.3	=====	$\psi_6 \psi_7$	$\psi_8 = -0.71 4\rangle + 0.71 -4\rangle$
40.0	—————	$\psi_5$	$\psi_9 = 0.70 4\rangle + 0.70 -4\rangle$
3.2	—————	$\psi_4$	$\psi_{10} \psi_{11} =  \pm 5\rangle$
1.3	=====	$\psi_2 \psi_3$	$\psi_{12} \psi_{13} =  \pm 6\rangle$
0	—————	$\psi_1$	

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