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# MAGNETIC STUDIES BY USING A COMBINED <sup>3</sup>HE AND MAGNETIC COOLING SYSTEM BELOW 1 K

by

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for

the Degree

of

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Part I

Technics for ESR and Magnetization Measurements below 1 K

## Synopsis

A new cryostat using a combined system of  ${}^{3}$ He and adiavatic demagnetization for ESR measurements below 1 K was developed as shown in A. ESR measurements can easily be done from 24 GHz to 47 GHz down to about 100 mK with good temperature stability around <sup>3</sup>He temperature region. In order to measure the sample temperature just on resonance, AFMR line shift in a typical antiferromagnet RbMnF, was measured and the temperature increase of the sample was estimated. Two kinds of <sup>3</sup>He cryostat using the fluxgate magnetometer for the magnetization measurements were constructed as shown in B. One of them can measure the temperature dependence of the magnetization in a constant field and another one can be used for measuring the magnetization curve by moving the sample in a various fixed field at a constant temperature. As these systems can detect the magnetization change of about  $10^{-3} \sim 10^3$  Gauss, they can be applied for almost all magnetization measurements of weak paramagnets as well as ferromagnets. A carbon resistance thermometer (50 mK  $\sim$  4.2 K) which is calibrated by measuring CMN susceptibility by Hartshorn mutual inductance bridge and a calibrated germanium thermometer (0.5 K  $\sim$  1 K) used for ESR and magnetization measurements are described in C.

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## A ESR Cryostat below 1 K Using A Combined <sup>3</sup>He and Adiabatic Demagnetization System

#### § 1 Introduction

Many low-dimensional antiferromagnets have their threedimensional magnetic ordering temperature  $T_N$  below 1 K, because of the weak exchange interaction between magnetic chains or layers. In the short range order region near  $T_N$ , the shift and broadening of the ESR line, which are characteristics of the low dimensional magnets, have been observed by previous ESR measurements.<sup>1)-5)</sup> In order to investigate the magnetism of these magnets at low temperatures, especially, the spin dynamics and cooperative excitations in the spin systems below  $T_N$ , it is necessary to construct the ESR cryostat which operates in wide frequency and temperature region below 1 K.

So far, all ESR work<sup>6)-12)</sup> below 1 K has been done by using either a <sup>3</sup>He refrigerator or an adiabatic demagnetization method at a single microwave frequency. The lowest ESR temperature obtained by Abe et al.<sup>12)</sup> using the adiabatic demagnetization method is about 40 mK while the lowest data for <sup>3</sup>He cryostat is 250 mK.<sup>10)</sup> In general, <sup>3</sup>He cryostat is simple and useful for ESR measurements down to near 0.3 K, and the temperature is easily controlled. On the other hand, a lower temperature can be obtained in the adiabatic demagnetization method. However, the temperature increase of this method in the <sup>3</sup>He temperature region (0.4 K ~ 1 K) is too fast to take ESR data because of the

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fact that the specific heat of the paramagnetic salt is small near 1 K. Desorption of <sup>4</sup>He gas adsorbed on the salt also promotes the heating of the specimen. The most favorable method is use of a dilution refrigerator but this method is too complicated in handling and needs a large quantity of liquid <sup>4</sup>He. So. we combined the <sup>3</sup>He refrigerator with the adiabatic demagnetization system to cover a wide ESR temperature region with desirable stability below 1 K. The ESR cryostat constructed is compact and includes two superconducting magnets for ESR and demagnetization. Liquid <sup>4</sup>He of only 2.5 litters is used for one cycle operation, as will be described in the next section. Α wide frequency range of  $24 \sim 47$  GHz is covered by changing the length of rectangular cavity in our ESR cryostat and it is useful especially for the antiferromagnetic resonance (AFMR). Detailed constructions of the cryostat and its operations are described in \$2 and \$3, respectively.

In the ESR measurements below 1 K, estimation of the sample temperature is an important problem. When the sample absorbs the microwave power on the resonance absorption, the temperature in the sample increases isolately from the sample holder. The presence of Kapitza thermal boundary resistance between the. sample and its holder is important in this case. As a new experimental method to estimate the sample temperature, the hyperfine shift of AFMR line in a cubic antiferromagnet RbMnF<sub>3</sub> was introduced in the present study. Detailed results and discussions on this method are given in §3.

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#### § 2 Apparatus

## (1) Cryostat

In our combined <sup>3</sup>He and adiabatic demagnetization refrigerator the <sup>3</sup>He system works in one-shot cycle. Outline of the cryostat is shown in Fig. 1. <sup>3</sup>He gas is pumped by a shaft-sealed rotary pump of 150 litters/min. through a stainless steel pipe J of 9.5 mm I.D. in the figure. The pumping speed is controlled by the valve B. The pipe E is a stainless steel tube of 12.5 mm I.D. for evacuating the vacuum can V. The symbol A in Fig. 1 is the valve for the evacuating line. A German silver waveguide WRJ-320 is passed through the pipe E and cut in two pieces separated by a few millimeters. These two pieces of german silver waveguide are connected with a slightly large rectangular sleeve, which is soldered to one piece of the waveguide, so as to absorb the difference in thermal expansion of the waveguide and that of the stainless steel tube E. The lower piece of German silver waveguide is soldered to copper waveguide. M which is inside the vacuum can V and thermally anchored on a copper rod L at 1.2 K. The radiation through the waveguide is shielded by bending the waveguide M. The vacuum seal for the waveguide is done by the quartz plate of 0.5 mm in thickness at the top of the pipe E at which the copper waveguide C coming from the ESR spectrometer is connected by a frange. The lead wires for the electrical resistance measurements in thermometers such as carbon resistors are also passed through the pipe E. These wires are thermally anchored on a copper rod L at 1.2 K, and they come out through

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a hermetic seal D at the top of the cryostat. Liquid <sup>4</sup>He is transferred through a pipe H. Two superconducting magnets N and U for the ESR measurements and the demagnetization, respectively, are suspended from the ring plate K. The symbol W in Fig. 1 shows the persistent current mode switch for the superconducting magnet U. The symbol G shows the liquid nitrogen pot. The inlet and outlet pipes to the pot are not drawn in the figure to avoid complication. This pot works effectively as the first thermal sink for the pipes E, J and H, and the lead wires F of the superconducting magnets. The spirally wound part Y of the leads works as the second heat exchanger with cold helium vapor so as to decrease the heat inflow.

Detailed constructions in the vacuum can V is shown in Fig. The vacuum can is made of SUS 304 stainless steel with 25 mm 2a. 0.D. and 0.5 mm wall thickness, and attached to the vacuum jacket O by Wood metal. A cylindrical <sup>3</sup>He evaporation pot P with a concentric hole of 5 mm in diameter is suspended by the <sup>3</sup>He pumping CuNi tube I of 3 mm I.D. × 80 mm in length. The upper end of tube I is connected to the pipe J in Fig. 1 through the radiation shield. The pot P is made of pure copper and has thin fins inside the inner wall as shown in Fig. 2a to increase the contact area with liquid <sup>3</sup>He. The capacity of the pot is about 3 cm<sup>3</sup>. The bottom of <sup>3</sup>He pot has a screw structure to support the salt pill for the demagnetization or to attach the constructions for any other purposes such as resistance or magnetization measurements. The salt pill S for adiabatic demagnetization is constructed from a Bakelite pipe (21 mm O.D., 20 mm I.D. and 130 mm in length) in which about 40 grams of ferric ammonium alum, FeNH4(SO4)2.12 H2O, and about

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2000 copper wires of 0.05 mm in diameter are stuffed with thermal contact agent Apiezon J oil. This salt pill S is suspended by the teflon supporter X from the <sup>3</sup>He evaporation pot with the screw construction as mentioned above. The fine copper wires out of the salt are bundled at the top of the pill and solidified by the epoxy resin. This strand of copper wires passes through the hole of the cylindrical <sup>3</sup>He pot without contact and serves as the thermal link Z between the salt pill and the cavity Q. The connection between the cavity Q and the thermal link Z is done by silver soldering or by tight screw connection. The cavity Q is made of a piece of copper waveguide and resonates on TE102 mode. For setting the sample the bottom wall is separated from the cavity at the position of a quarter wave length as schematically shown in Fig. 2b. The cavity Q is cut off about 2 mm from the waveguide M in order to avoid the heat inflow. This cut-off of the waveguide is one of the essential points in the ESR cryostat below 1 K. A wide ESR frequency range above the cut-off frequency of the waveguide WRJ-320, 24  $\sim$  47 GHz is covered by changing the cavity. The sample is grewed on to the bottom of the cavity by Apiezon N The temperatures of the cavity and  ${}^{3}$ He pot are measured grease. by carbon resistors R which are Matsushita ERC-18SG, 100  $\Omega$  at room The calibration of the carbon resistors was caretemperature. fully done by measuring ac susceptibility of CMN (Cerium Magnesium Nitrate,  $Ce_2Mg_3(NO_3)_{12} \cdot 24H_2O$ ). The electrical resistance of these carbon resistors was measured by ac bridge method using IT (Instruments for Technology Ltd. in Finland) automatic selfbalancing resistance bridge, and the power dissipation for the measurements

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is within  $10^{-11}$  Watt around 0.1 K. The temperature was measured within the error of 0.5 % in the temperature region 0.1 K  $\sim$  1 K. These carbon resistors are wound by a thin copper plate and attached onto the bottom of the cavity or the top of <sup>3</sup>He pot by a small screw as shown in Fig. 2. As the result, the thermal response time was sufficiently short. The temperature of the cavity can be changed by the heater T wound on the thermal link.

## (2) ESR Spectrometer

A conventional reflection type spectrometer was used in the present experiments. In the ESR measurements below 1 K, the following points should be noticed : a usual field modulation method is not applicable because of the eddy current heating on the cavity. Another problem is the sample heating due to the presence of Kapitza thermal boundary resistance between the sample and the cavity wall, so the input microwave power must be as low as to be  $10^{-7} \sim 10^{-9}$  Watt around 0.1 K as discussed in the next section. Considering these restrictions, the spectrometer as shown in Fig. 3 was used. Instead of the field modulation, the microwave power is modulated by superposing the rectangular pulse voltage with 1 kHz repetition to the dc repeller voltage. The klystron does not oscillate under the dc voltage and the pulse voltage is adjusted so as to obtain the maximum oscillation power with the best tuning condition of the whole cavity system<sup>12)</sup>. The microwave power is attenuated by two attenuators in series. After receiving by a crystal diode, 1N26, the ESR signal through the PAR-116 preamplifier and PAR-121A lock-in amplifier is displayed in a XY-recorder.

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A magnetic field for ESR measurements is supplied by the superconducting magnet which is 85 mm in length, 150 mm 0.D. and 25 mm bore-diameter, and its maximum field is about 30 kOe. The field values were calibrated by DPPH absorption signal at frequencies  $24 \sim 47$  GHz.

## § 3 Results and Discussions

### (1) Operation of The Cryostat

The time variation of the cavity temperature during the actual ESR measurements is shown in Fig. 4. After transferring liquid <sup>4</sup>He of 2.5 litters into the glass Dewar, adjustments of the apparatus such as the power balance in the magic-T of the spectrometer is done during the steps A and B in Fig. 4. Then, ESR measurements are performed from 4.2 K to 1.2 K with slowly pumping of liquid <sup>4</sup>He by Kenny type rotary pump of 3000 litters/min. (B  $\sim$  C in Fig. After the measurements at 1.2 K, <sup>3</sup>He gas is condensed in the 4). <sup>3</sup>He pot and the magnet for the adiabatic demagnetization is operated up to about 25 kOe with the persistent current mode (C  $\sim$  D). After the cavity temperature returns to 1.2 K the <sup>4</sup>He exchange gas is pumped out. The Kenny pumping line is closed until the temperature of liquid <sup>4</sup>He bath increases up to about 2 K so as the exchange gas to be quickly excluded as possible. In this process,  $D \sim E$  in Fig. 4, the cavity temperature increases slightly by the heat conduction through the remained exchange gas and solid construction supporting the cavity. When the vacuum gauge at the

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top of the cryostat shows about  $1 \sim 2 \times 10^{-6}$  Torr., the pumping line for liquid <sup>4</sup>He bath is again opened, and subsequently, the <sup>3</sup>He pot reaches at the lowest temperature of about 0.4 K, the magnetic field in the salt is slowly decreased at the rate of about 1 kOe/min. (F  $\sim$  G). After the demagnetization, ESR measurements start at G in Fig. 4. The ESR data are taken many times up to 1.2 K (G  $\sim$  H). The input microwave power is about 0.1  $\mu$ W in the present experiment.

(2) Estimation of The Sample Temperature

In the ESR measurements below 1 K, it is verry difficult to determine the temperature of the sample which is on resonance, though the measurements of the cavity temperature are easily done by a thermometer as previously described. When the sample is just on resonance, the sample absorbs the microwave power and the produced heat does not decay because of the Kapitza thermal boundary resistance between the sample and the cavity wall. The heat flow  $\dot{Q}$  is proportional to the temperature difference  $\Delta T$  of the sample  $T_s$  and cavity wall  $T_c$  as

$$Q = \frac{A\Delta T}{R_{K}}$$
,

where A is the surface area between them and  $R_{K}$  represents the Kapitza resistance. In a single crystal of CrK-alum adhered on the copper foil by Apiezon N grease, for example, the Kapitza resistance is reported as 13,14)

(1)

$$R_{K} = 4 \times 10^{-6} \cdot T_{c}^{-3}$$
. (K·cm<sup>2</sup>·sec/erg) (2)

Therefore,  $\Delta T$  is given as

$$\Delta T = 4 \times 10^{-6} \cdot q/A \cdot T_c^3$$
. (K) (3)

We get  $\Delta T = 40$  mK for the condition that Q = 1 erg/sec,  $T_c = 0.1$  K and A = 0.1 cm<sup>2</sup>. This means that the sample temperature increases about 40 mK higher than the cavity temperature for the absorbed microwave power of 0.1  $\mu$ W. In the actual ESR measurements for various substances, however, the Kapitza resistance is not exactly known. Therefore, it becomes necessary to use another more direct method of the temperature measurement for specimens just under the resonance.

To estimate the exact temperature of the specimen, we measured the shift of AFMR line in a cubic antiferromagnet  $\text{RbMnF}_3^{15),16}$ . This shift comes from the temperature dependent nuclear anisotropy field in  $\text{AFMR}^{17)}$ . Below the Néel temperature of 82.6 K the manganese spins in this compound form the two sublattice antiparallel configuration and point in the body-diagonal direction in the absence of the applied field. When the field  $H_0$  is larger than the critical field  $H_c \approx 2.5$  kOe, the spin axes are perpendicular to  $H_0$ . In this state, AFMR ferquency is written as

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$$\left(\frac{\omega}{\gamma}\right)^2 = H_0^2 + 2H_E(H_A + H_N),$$
 (4)

where  $H_E$  and  $H_A$  are the exchange and anisotropy fields coming from the electronic origin, and they are usually constant at low temperatures below  $T_N$ .  $H_N$  is the hyperfine field coming from the Mn nucleus. This field is always parallel to the d-electron spin moment and acts as the dynamical anisotropy field perpendicular to the applied field in the state,  $H_0 > H_c$ . Then,  $H_N$  is written as<sup>17</sup>)

$$H_{N} = \frac{A^{2}I(I+1) < S >}{3kh\gamma_{e}} \cdot \frac{1}{T_{n}}, \qquad (0e) \qquad (5)$$

for AI<S>/kT<sub>n</sub><<1, where A is the hyperfine constant, I the nuclear spin, <S> the sublattice spin moment which is saturated at low temperatures below  $T_N$ ,  $\gamma_e$  the gyro-magnetic ratio of the electron spins, and  $T_n$  the nuclear spin temperature. In the AFMR measurements with a constant frequency  $\omega$ , it is expected from eqs. (4) and (5) that the square of resonance field  $H_0^2$  decreases in proportion to  $1/T_n$ . In these high concentrated manganese compounds, the nuclear spin lattice relaxation time is considered to be short enough<sup>18</sup>. Assuming  $T_n \approx T_s$ , one can estimate the sample temperature by using eqs. (4) and (5).

In our AFMR experiments in  $RbMnF_3$ , the external magnetic field was applied along the cubic axis and the sample of 1 mm × 1 mm × 0.5 mm was tightly grewed onto the bottom of the cavity

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wall by the thermal contact agent Apiezon N grease so as a large surface of the sample to be contact with the cavity wall. The incident microwave power to the cavity was attenuated by two attenuators inseries to be about 0.1  $\mu$ W. The typical AFMR lines observed for 32.44 GHz are shown in Fig. 5 for the cavity temperatures from 4.2 K to 0.14 K. The resonance field  $H_0$  shifts to lower field at lower temperatures. The square of observed field  ${\rm H_0}^2$  are plotted against the inverse of the cavity temperature  $1/T_c$  in Fig. It should be noted that the linear relation in  $H_0^2$  vs  $1/T_c$ 6. holds down to  $T_c \approx 0.25$  K and deviates from the linear line below about 0.25 K as is shown by a solid line in Fig. 6. As the condition AI<S>/kT<sub>n</sub><<1 should be satisfied down to about above 0.1  $K^{12}$ , the linear dependence should be satisfied down to this temperature. The observed deviation below 0.25 K in Fig. 6 is then attributed to the fact that the sample temperature increases due to the Kapitza resistance between the sample and the cavity wall. By extrapolating the linear relation above 0.25 K to lower temperatures, we can estimate the sample temperatures  $T_s$  from Fig. 6. The obtained  $T_s$  are plotted against the cavity temperature  $T_c$  in Fig. 7. The solid line (1) corresponds to the negligible microwave power. The other lines (2) and (3) are calculated for the absorbed microwave power of 0.02 and 0.1  $\mu W,$  respectively with  $R_{K}$  of CrK-alum. The open circles show the experimental results. As is seen from Fig. 7, the practical heat inflow in our experiment is about 0.6 erg/sec. In ESR measurements for various substances below 1 K, the present method seems to be effective for the determination of the sample temperature.

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## § 4 Concluding Remarks

Our combined <sup>3</sup>He-demagnetization system was proved to be practically useful for the ESR work in a frequency range of 24  $\sim$ 47 GHz at temperatures from 4.2 K to about 100 mK, and satisfactorily be applied to the ESR study in the low-dimensional magnets with T<sub>N</sub> below 1 K, such as Cu(NH<sub>3</sub>)<sub>4</sub>SO<sub>4</sub>·H<sub>2</sub>O<sup>19)</sup>, Rb<sub>2</sub>PbCu(NO<sub>2</sub>)<sub>6</sub><sup>20)</sup> and CuSO<sub>4</sub>·5H<sub>2</sub>O<sup>21)</sup>.

Now it may be necessarry to do a comparative discussion about the merits and demerits of various ESR techniques below 1 K. The simplest way to realize ESR below 1 K is to use <sup>3</sup>He cryostat or to use a demagnetization cryostat. The former is limited down to about 0.4 K but a precise temperature setting is available. The latter is effective down to 0.1  $\sim$  0.07 K but the temperature control above 0.5 K is very difficult. Our cryostat was designed to cover both merits and the results were satisfactory. However, one of the demerits in our system is the complexity because one must make two stages for refrigeration.

The next problem to be considered is the ESR sensitivity as a whole. As is well known the higher sensitivity can be expected if higher input microwave power is used. However, the high power increases the sample temperature. Our conclusion is summarized as follows : if one uses usual detecting systems such as the crystal video system, i.e., the crystal diode detection using the frequency or amplitude modulation, the microwave power level of the order of microwatt is necessary for the standard ESR measurements. In this case, the lowest temperature of the sample may be about 50 mK even if one uses the optimum experimental condition.

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Therefore, the use of the more sensitive detectors such as the superheterodyne detector or the SQUID detector may be necessary when one wishes to do ESR study in more low temperature region, i.e., around 10 mK or in the millikelyin temperature region. B Magnetization Measurement by Fluxgate Magnetometer below 1 K

#### § 1 Introduction

Since the re-entrant superconductivity was discovered in the ternary compounds (RE)Rh<sub> $\mu$ </sub>B<sub> $\mu$ </sub> by Fertig et al.<sup>22)</sup> and in the ternary Chevrel-phase compounds (RE)  $_{x}Mo_{6}S_{8}$  and (RE)  $_{x}Mo_{6}Se_{8}$  by Ishikawa et al.<sup>23)</sup>, where (RE) means a rare earth element and x = 1.0  $\sim$  1.2, there have been extensive studies about superconductivity and magnetic order in these compounds. One of the surprising features of these compounds is the coexistence of the magnetic order and the superconductivity. In the case of  $RE_{1,2}Mo_{6}S_{8}$  for RE = Tb, Dy and Gd, the coexistence of the superconductivity and antiferromagnetic order have been confirmed by neutron scattering experiments<sup>24),25),26)</sup>. In the case of ferromagnets such as  $ErRh_{ll}B_{ll}$ , however, the nature of the magnetic order coexisting with superconductivity is still controversial. Although the theoretical approachs by several authors 27)-30 have predicted the coexistence of superconductivity and the helical spin ordering in a narrow temperature region just above the ferromagnetic ordering temperature,  $T_{c2} \approx 0.8$  K in ErRh<sub>4</sub>B<sub>4</sub>, there have been found no experimental evidence for the helical spin phase except for the suggestive neutron scattering data<sup>31),32)</sup>. То check the possibility of the presence of the helical spin ordering, it is desired to investigate the magnetization profile around  ${
m T_{c2}}$ in ErRh<sub>4</sub>B<sub>4</sub>.

For the measurements of weak magnetization below 1 K, SQUID (Superconducting QUantum Interference Devices) is usually used.

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In the present case where the magnetization is large, however, this method is not adequate because of its too sensitive detecting abilities. For the present magnetization measurements in <sup>3</sup>He temperature region, the usual Faraday method is also not suitable because it is difficult to operate in such a low temperature region below 1 K. The magnetization curve can also be obtained by observing the induction signal of a pick up coil with scanning the magnetic field. However, the sensitivity of this method is not so high. In order to get higher sensitivity, the scanning speed must be increased. It is, however, undesirable for the present measurements because of the heating due to the eddy current loss. Considering these facts, we adopted the fluxgate magnetometer method<sup>33</sup>),<sup>34</sup>) using a superconducting transformer. This fluxgate magnetometer was set up by making use of Hewlet Packerd clip-on dc milliammeter (H.P. 428B) with an accessory (H.P. 3529A) for weak magnetic field measurement. This type of magnetometer, which was initially applied to the nuclear magnetization measurements in the millikelvin temperature region by Andres et al. (33), 34) is easy to handle compared with SQUID and has enough sensitivity for present measurement.

In this method, however, it is difficult to scan the magnetic field because the perfect balance of the superconducting transformer under the field scan is difficult. Therefore, the magnetization measurement can only be done by changing the temperature or by extracting and inserting the sample from the superconducting transformer. In the following section, the principle and construction of the fluxgate magnetometer will be shown in detail.

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The techniques of the practical operations and the estimation of the sensitivityare shown in §3. Applications to the magnetization measurement will be described in Part (III).

## § 2 Cryostat

<sup>5</sup>He refrigerator was used for magnetization measurement below 1 K. Two kinds of cryostat were constructed. One of them is the cryostat for the extracting method by which one can measure the magnetization process at a constant temperature. In another one, the sample is fixed and the magnetization change can be measured by changing temperature.

#### (1) The Cryostat and The Fluxgate Magnetometer

Outline of the magnetization measurements by the fluxgate magnetometer is shown in Fig. 8. The superconducting transformer consists of the astatic pick up coil (sample coil and compensation coil), the probe coil and the connecting leads. All wires are made of NbTi alloys. The astatic pick up coil is located in the vacuum can so as to set the sample just in the center of the sample coil. On the other hand, the field probe is inserted in the probe coil which is covered by the NbTi shield. The transformer system is directly immersed in liquid <sup>4</sup>He.

The principle of the fluxgate magnetometer is as follows. When the magnetization of the sample in the sample coil changes due to the temperature change under the constant magnetic field, for example, the supercurrent induced in the sample coil transforms to the probe coil so as to keep the total flux in whole of

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the transformer to be constant. This supercurrent produces the magnetic field in the probe coil which is proportional to the change of the flux in the sample coil. The produced field is detected by the field probe with aid of the clip-on dc milliammeter.

As the fluxgate magnetometer probe can detect the magnetic field in the range from 1 mGauss to 10 Gauss corresponding to the meter ranges from 1 mA to 10 A of the clip-on dc milliammeter, the effective measuring range of the magnetization covers from  $10^{-3}$  Gauss to about  $10^3$  Gauss by adjusting the sample volume. This means that one can measure the magnetization of weak paramagnets as well as usual ferromagnets. The magnetic field is supplied by the superconducting magnet in the persistent current mode, and its maximum field is about 30 kOe. A desired temperature is obtained by <sup>3</sup>He refrigerator and it is measured by a commercial germanium resistance thermometer using IT (Instruments for Technology Ltd.) automatic resistance bridge.

Two types of the sample holding system are designed and used. The model I in Fig. 9 is used for measuring the temperature dependence of the magnetization and the magnetization at a temperature is measured by extracting the sample using the model II system in Fig. 9. In the model II system, the sample position is fixed during the experiment while it is moved by the dc motor for extraction and insertion of the sample from the sample coil of the model II. The sample speed for extraction and insertion is about 4 cm/min. with the total stroke of about 6 cm. The sample and germanium thermometer in the model I are thermally

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linked with the <sup>3</sup>He pot by about 200 polyurethane coated copper wires of 0.05 mm in diameter which are tightly connected to the sample by Apiezon N grease. The sample in the type II system is immersed directly into liquid <sup>3</sup>He. In the both models, liquid <sup>3</sup>He of about 2 cm<sup>3</sup> is used. The temperature of the sample is controlled by controlling the vapor pressure of liquid <sup>3</sup>He below 1.2 K and by controlling the vapor pressure of liquid <sup>4</sup>He between 4.2 K and 1.2 K.

(2) Design of The Transformer Coil

In this section, the optimum design for the superconducting transformer is considered. The total flux  $\phi_{\rm T}$  of the transformer coil, i.e., both the pick up and probe coils are constant and quantized. Therefore, the relation,

$$\phi_{\rm T} = i(L_1 + L_2 + L_3) = n\phi_0,$$
 (Gauss) (1)

is obtained where i is the supercurrent flow in the closed circuit.  $L_1$ ,  $L_2$  and  $L_3$  are self-inductances of the pick up and probe coils and interconnecting NbTi leads as shown in Fig. 10.  $\phi_0$  is the flux quantum (2.067 × 10<sup>-7</sup> Gauss·cm<sup>2</sup>) and n is an integer.

When the flux in the sample coil changes by  $\Delta\phi$  due to the change of the magnetization of the sample, the supercurrent must be modified by  $\Delta i$  so as to keep  $\phi_{\rm T}$  to be constant. Therefore, the relation,

$$\Delta \phi + \Delta i (L_1 + L_2 + L_3) = 0, \qquad (2)$$

holds. Ai is then obtained as

$$\Delta i = -\Delta \phi / (L_1 + L_2 + L_3).$$
 (emu.A) (3)

This current change induces the magnetic field change  $\Delta H$  in the long probe coil given by

$$\Delta H \approx 4\pi \left(\frac{n_2}{l_2}\right) \Delta i = -\left(\frac{4\pi n_2/l_2}{L_1 + L_2 + L_3}\right) \Delta \phi, \qquad (Oe) \qquad (4)$$

where  $l_2$  and  $n_2$  are the length and turn number of the probe coil. Now, we consider the case where the sample length is much longer than the coil length as is shown in Fig.li. The flux  $\Delta\phi$ due to the induced magnetization  $\Delta M$  is given by

$$\Delta \phi \simeq 4\pi n_1 A \Delta M = \pi^2 n_1 d^2 \Delta M, \qquad (Gauss \cdot cm^2) \qquad (5)$$

where A is the cross section of the sample in  $cm^2$ , d is the diameter of the cylindrical sample and  $n_1$  is the turn number of the sample coil. Thus, the induced magnetic field  $\Delta H$  in the probe coil is obtained by using eqs. (4) and (5) as

$$\Delta H = -p \Delta M, \qquad (0e) \qquad (6)$$

with

$$p = \frac{4\pi^{3}n_{1}n_{2}\bar{a}^{2}}{1_{2}(L_{1}+L_{2}+L_{3})}.$$
 (7)

To keep a high sensitivity of the transformer system, it is necessary to have a large  $\Delta H/\Delta M$  value. Therefore, the p-value in eq. (7) should be large. As d and  $l_2$  are substantially limited by the effective volume of the cryostat, the practical variable parameters are  $n_1$ ,  $n_2$ ,  $L_1$  and  $L_2$ .  $L_3$  is much smaller than  $L_1$  and  $L_2$  so that it is neglected. Thus, p is approximately written by

$$p \simeq \left(\frac{4\pi^{3}d^{2}}{l_{2}}\right) \times \frac{n_{1}n_{2}}{L_{1}+L_{2}}.$$
 (8)

Noticing the relations  $L_1 \propto n_1^2$  and  $L_2 \propto n_2^2$ , it is simply verified that the maximum p-value is obtained when the relation

 $L_1 = L_2, \tag{9}$ 

is satisfied. This is one of the important relations for designing the transformer system.

The sample and compensation coils are astatically wound. The inductances are nearly equal to each other with 12 turns and 1.2 cm in diameter. For the probe coil, the diameter of 0.7 cm, 62 turns and 2.5 cm in length are adopted.

The self-inductances of  $L_1$  and  $L_2$  are numerically evaluated by a standard formula and obtained 6.82 µH and 6.65 µH, respectively.  $L_3$  is also estimated and it was found to be about 0.15 µH.

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Using these estimations of  $L_1$ ,  $L_2$  and  $L_3$ , the magnetic field  $\Delta H$  induced in the probe coil is estimated as

$$\Delta H = -0.872 \cdot \pi d^2 \Delta M. \qquad (Oe) \qquad (10)$$

E31 Detailed Construction of The Transformer System

The field probe (H.P. 3529A) is the magnetic field sensor for detecting the magnetic field in the probe coil. Its plastic cover is stripped off. The field probe is drived by 20 kHz signal and the leakage flux becomes a serious noise for the transformer system. In order to shield the transformer system from 20 kHz rf field, the field probe is covered by the copper rf shield of 6 mm I.D., 7 mm O.D. and 35 mm in length as shown in Fig.12. The probe system is located inside the NbTi shield case in liquid <sup>4</sup>He bath.

The probe coil is wound around the copper tube. The bias coil for adjusting the detector level of the clip-on dc milliammeter is also wound on the probe coil. The bias adjustment can easily be done by feeding an additional dc current to the bias coil from an external current source of Keithley model 225.

The pick up coil was astatically wound around the Bakelite bobbin and it was tightly set in the vacuum can as shown in Fig. 12. All connections of the transformer are connected with spot welding.

A heater wire of about 100  $\Omega$  is wound around a part of the NbTi leads. It is used to destroy a residual supercurrent trapped in the transformer and to establish the scale of the clip-on dc

milliammeter to zero before measurements.

The transformer is made of 0.070 mm in core diameter copper coated (0.100 mm in diameter) formyal insulated (0.144 mm in diameter) NbTi wire manufactured by Vacuum Metallugical Co. Ltd.

As shown in Fig.12, the superconducting magnet is attached to the vacuum can with the fine adjustment system so as to set the magnet just in the center of the pick up coil.

The main part of the vacuum can is made of 24 mm I.D. and 25 mm O.D. stainless steel tube except the sample part. The central part of the can is made of copper in order to avoid the spurious magnetic effect to pick up coil system. The system given in Fig.12 is used both for the model I and II in common.

§ 3 Operation of The Cryostat

### (1) Model I cryostat

The temperature dependence of the magnetization can be observed as follows. After transferring liquid <sup>4</sup>He in the Dewar, a desired static magnetic field is supplied by the superconducting magnet in the persistent current mode with breaking the transformer circuit by the heater. Next, the detector level of the clip-on dc milliammeter is adjusted by the bias current so as to cover the desired range of the sample magnetization. The temperature dependence of the magnetization can be measured with decreasing temperature. A desired temperature between 4.2 K and 1.2 K can be obtained by pumping out <sup>4</sup>He gas by 3000 litters/min. Kenny type pump. Around 1.2 K, <sup>3</sup>He gas is liquified. The exchange gas

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is evacuated to about  $10^{-6}$  Torr. by diffusion pump and a required temperature down to 0.5 K can be obtained by pumping out <sup>3</sup>He gas. The temperature dependence of the magnetization is observed and recorded by looking at the change of the detector level of the clip-on dc milliammeter.

## (2) Model II cryostat

The magnetization measurement by the model II cryostat can be done in the following procedure. After obtaining a desired temperature by the similar method given in the previous subsection, the required field is supplied by a superconducting magnet with breaking the transformer circuit. The transformer circuit is operated after getting a desired constant field and the detector level of the clip-on dc milliammeter is adjusted as before. The sample is inserted into the pick up coil by driving the dc motor and the magnetization is measured. After the temperature measurement by the germanium thermometer, the sample is extracted and the magnetization is measured again. The difference between the maximum and the minimum values of the detector level should be proportional to the magnetization of the sample. Repeating this insertion and extraction in the various fixed magnetic field under the coustant temperature, the magnetization curve can be obtained between 0.5 K and 4.2 K.

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#### § 4 Characteristics of The Cryostats

The experimental test of the present cryostats for magnetization measurements was done by using a typical paramagnetic CMN There are two important parts for obtaining high sensisample. tivity of the magnetization measurements. One of them is the noise level of the transformer signal corresponding to the field fluctuation in the probe coil and the other is the long time drift in the coil. A typical experimental datum without sample is shown in Fig. 13. It shows an output of the fluxgate magnetometer showing the field fluctuation level in the probe coil. The result shows that both the fluctuation and drift are within 1.2  $\times$  10<sup>-4</sup> mA of the magnetometer which corresponds to the sensitivity of the magnetization change  $\Delta M$  in the sample coil as  $\Delta M \simeq 7 \times 10^{-5}$ Gauss. This may be enough for usual magnetization measurements except the nuclear paramagnetism.

It is difficult to determine the absolute value of the magmetization change by using the present equipment. Therefore, it is usually calibrated by the Faraday method in higher temperature region.

Typical magnetization data of CMN are shown in Fig. 14. The CMN powder is mixed with Apiezon N grease and is holded with a cylindrical shape of 3 mm in diameter. The output current (A) which is proportional to the susceptibility is proportional to 1/T, therefore, the accuracy of the equipment is garanteed.

An example of the output signal of the magnetometer due to the sample motion is shown in Fig. 15. Fig. 15a shows relative positions of the sample and coil and the corresponding signal is illus-

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trated in Fig. 15b. When the sample is far from the pick up coil, the signal level is zero as is shown in the position A and the level shows its maximum at B, i.e., the sample is just at the center of the sample coil. The level becomes negative around C because of the negative flux change due to the compensation coil. The level shows a similar change by extracting the sample as is easily seen in Fig. 15b. This magnetization measurement can easily be done by using the present fluxgate magnetometer.

#### C Thermometry below 1 K

### § 1 Introduction

There are several methods of measuring temperatures below 1 In the <sup>3</sup>He temperature region, i.e.  $1 \sim 0.3$  K, use of the K. germanium thermometer is most convenient because the commercial one has enough calibrations in the above temperature range. Therefore, the germanium thermometer was used both for the model I and II systems, as was described in the previous section. The used thermometer is GR-200A-100 calibrated by Lake Shore Cryotronics. Below 0.3 K, however, the thermometer has no reliable calibration. So, we must use other thermometers, especially for the ESR study around 0.1 K. Generally speaking, the magnetic susceptibility thermometer using typical paramagnets such as CMN may be the most reliable one around 0.1 K. However, it is not so convenient because the field sensor, i.e. the Hartshorn coil and the sample, is not so small. Moreover, it is sensitive for the magnetic field near by. Considering these facts, a carbon resistor was used for the ESR study and the CMN thermometer was used for the calibration of the carbon thermometer. The practical design and operation of the CMN thermometer is described in the next section and the calibration of the carbon resistor is shown in §2.

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§ 2 ac Susceptibility Measurement by Hartshorn Mutual Inductance Bridge and Calibration of The Carbon Resistor

The ac Hartshorn mutual inductance bridge has been constructed in our laboratory in order to measure the ac susceptibility of CMN for the calibration of the carbon resistor below 1 K.

A block diagram of the bridge is shown in Fig.16. A low frequency of about 100  $\sim$  200 Hz oscillating field of about 1 Oe is supplied into the primary coil A. PAR 124A lock-in amplifire is used as a detector in high sensitive ac voltmeter mode. Two mutual inductors  $M_1$  and  $M_2$  are used for the bridge balance.  $M_1$ is the type 4229 calibrated variable mutual inductor of H. Tinsley Co. Ltd. and  $M_2$  is the Brooks type variable mutual inductor of YEW (Yokogawa Electric Works).

Cut view of the cryostat for the ac susceptibility measurements is shown in Fig.17. <sup>3</sup>He and adiavatic demagnetization stage are similar to those of ESR measurements described in A in  $^{3}$ He gas is condensed in  $^{3}$ He pot C through the evacuation Part I. About 40 grams of Fe ammonium alum is packed in the pill pipe A. F with Apiezon J oil and about 1000, polyurethane insulated copper wires of 0.05 mm in diameter. The salt pill F is suspended by the teflon supporter E from the bottom of  ${}^{3}\!\mathrm{He}$  pot C. The manganin heater P of about 100  $\Omega$  is also immersed in the pill in order to control the temperature. The sample M, the germanium thermometer I and the carbon resistor H are immersed in the thermal link 0 made of about 300 polyurethane insulated copper wires of 0.05 mm in diameter. The coil set N (primary coil K and secondary coil L) for the susceptibility measurements is attached

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to the bottom of the adiayatic yacuum can B. The vacuum cell J for the coll set was made of STYCAST 2850-GT by Emerson & Cuming Japan K.K.. D is lead wires for the colls and thermometers. G is the superconducting magnet for the adiayatic demagnetization.

Operations of this cryostat is similar to that of ESR one.

## (1) Coil Design and Construction

There have been many studies<sup>35]</sup>, <sup>36]</sup> for the precise temperature measurement below 1 K using ac Hartshorn mutual inductance method. The present coils were also designed according to their results and its geometrical constructions are shown in Fig.18.

For the geometry in Fig.18, the mutual inductance  $\rm L_{M}$  due to the sample of CMN is given by  $^{35)}$ 

$$L_{M} = 16 \cdot \pi^{2} n_{s} n_{p} V \chi f_{s} f_{p}$$
 (x 10<sup>-9</sup>), (H) (1)

for a spherical sample where  $f_s$  and  $f_p$  are geometrical factors as

$$f_{s} = \frac{1}{(b_{s}^{2} + \tilde{1}^{2})^{1/2}} + \frac{1}{2} \frac{d_{1} + \tilde{1}}{[b_{s}^{2} + (d_{1} + \tilde{1})^{2}]^{1/2}} - \frac{1}{2} \frac{d_{1} + 3\tilde{1}}{[b_{s}^{2} + (d_{1} + 3\tilde{1})^{2}]^{1/2}}$$
(2)

and

$$f_{p} = \frac{1}{2} \left\{ \frac{d_{2} + \tilde{1}}{[b_{p}^{2} + (d_{2} + \tilde{1})^{2}]^{1/2}} + \frac{d_{1} + d_{2} + 3\tilde{1}}{[b_{p}^{2} + (d_{1} + d_{2} + 3\tilde{1})^{2}]^{1/2}} \right\}$$
(3)

In eq. (1),  $n_p$  and  $n_s$  are the number of turns per unit length on the primary and secondary windings, V is the volume of CMN,  $\chi$  is its susceptibility and  $\bar{b}_s$  and  $\bar{b}_p$  are effective radii for the secondary and primary coils. The dimensions of the present coil such as  $\tilde{l}$ ,  $d_1$  and  $d_2$  are shown in Fig.18. From these parameters,  $f_p$  and  $f_s$  are given to be 0.820 and 0.879.  $n_p$  and  $n_s$  are determined as 1683 turns/cm and 2041 turns/cm, respectively.

(2) Sensitivity and Calibration of The Carbon Resistor

The sensitivity of the present coil was calibrated by measuring the powdered susceptibility of about 1 gram CMN between 4.2 K and 1.2 K. As already described in (1) in this section, the parameters  $n_p$ ,  $n_s$ ,  $f_p$  and  $f_s$  are known. Then eq. (1) is written by

$$L_{M} = 0.391 \times \chi V.$$
 (H) (4)

In the present system, the minimum detectable change of the mutual inductance  $\Delta L_{M \text{ min.}}$  under the usual condition was obtained as

$$\Delta L_{\rm M,min} \simeq 3.3 \times 10^{-2}$$
. (µH) (5)

Then, the minimum detectable change of the susceptibility  $\Delta \chi_{min}$ . per unit volume for the present system was determined as

$$\Delta \chi_{min.} \simeq 8.4 \times 10^{-8}$$
 (emu) (6)

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This sensitivity is enough for the calibration of the carbon resistor below 4.2 K using CMN of about 1 gram. The accuracy of the temperature determination is about 0.1 % below 4.2 K.

In our ESR measurements, a commercial Matsushita carbon resistor ERC-GJ, 1/8 W,  $100 \ \Omega$  resistor was used as a thermometer down to  $100 \ \text{mK}$ . A famous carbon resistor made by Speer is also effective but the size of Matsushita carbon resistor is smaller than that of the Speer. So, we used the former one.

The calibration of the carbon resistor was done by simultaneously measuring the ac susceptivility of CMN and the resistance of the carbon resistor using the already mentioned cryostat as shown in Fig.17. The resistance was measured by the automatic resistance bridge of IT (Instruments for Technology Ltd). It can measure the resistance within  $10^{-11}$  W power dissipation with about 0.5 % precision even below 0.1 K.

The temperatures of the ESR measurements done in the present study was calibrated using Fig.19. The field dependence of the resistor is expected to be within a few percents up to 30 kOe. For the aging effect of the resistor, the similar CMN calibration was done after one week and tried again after about one year. The drift was found to be a few percents.

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### Figure Caption

- Fig. 1. Schematic view of the ESR cryostat. The symbols in the figure are explained in the text.
- Fig. 2a. Detailed constructions of <sup>3</sup>He and adiavatic demagnetization stages. The symbols in the figure are explained in the text.
- Fig. 2b. Schematic view of the cavity.
- Fig. 3. Block diagram of the ESR spectrometer with the microwave power modulation.
- Fig. 4. An example of the cavity temperature during the ESR measurements.
- Fig. 5. Recorder traces for the AFMR line in  $\text{RbMnF}_3$  at the cavity temperatures  $T_c = 4.2 \text{ K} \sim 0.14 \text{ K}$  for the frequency  $v_0 = 32.44 \text{ GHz}$ . The vertical spike-like lines are field marks.
- Fig. 6. The square of resonance field  $H_0^2$  versus the inverse of the cavity temperature  $1/T_c$ , for  $v_0 = 32.44$  GHz and  $H_0$ parallel to the cubic axis in RbMnF<sub>3</sub>. A solid line shows the linear relation  $H_0^2$  versus  $1/T_s$ .
- Fig. 7. The sample temperature  $T_s$  as a function of the cavity temperature  $T_c$ . The theoretical lines (1), (2) and (3) are given in the text.
- Fig. 8. Outline of the fluxgate magnetometer.
- Fig. 9. Cut views of the sample holders in the models I and II systems.
- Fig. 10. Schematic view of the transformer coil system.
- Fig. 11. Relation of the pick up coil and sample.

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- Fig. 12. Detailed structure of the vacuum can and transformer system.
- Fig. 13. An example of the recorder trace without the sample at the fixed field of 200 Oe.
- Fig. 14. Experimental results of the magnetization measurements in CMN.
- Fig. 15a. Schematic view of the sample motion.
- Fig. 15b. A recorder trace of the magnetometer output under the sample motion.
- Fig. 16. Block diagram of the low frequency ac susceptivility measurement system by Hartshorn mutual inductance bridge.
- Fig. 17. Cut view of the low temperature cryostat for low frequency ac susceptivility measurement by Hartshorn mutual inductance bridge.
- Fig. 18. Construction of Hartshorn coil. The coil length is given by mm unit.
- Fig. 19. Temperature dependence of the resistance in Matsushita ERC-18GJ, 1/8 W carbon resistor.

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Fig. 7



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Fig.12

	j			
1,200	K	•		
				•
	<u>        </u>			
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	1			
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Fig.13



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Fig. 15 b





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Fig.17

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II

Part

# Electron Spin Resonance in Copper Sulphate Pentahydrate

down to 100 mK

Synopsis

Copper sulphate pentahydrate  $CuSO_4 \cdot 5H_2O$  is investigated by electron spin resonance at 9, 17, 24, 35 and 45 GHz bands down to about 100 mK using a combined cryostat of <sup>3</sup>He and adiabatic demagnetization described in Part I. Above 70 K the temperature dependent exchange interaction between two inequivalent sites A and B in the crystal is found. Below 20 K the temperature dependent shifts of resonance lines are observed and it is analized by taking into account the H/T effect in the dissimilar spin sites using the molecular field theory.

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### § 1 Introduction

In recent years, there have been many intensive studies in magnetic properties of low dimensional ferro- or antiferromagnets. In contrust with usual three-dimensional magnets, these low dimensional magnets are characterized by the short-range ordering in a wide temperature range around its characteristic temperature  $zJ/k_{\rm p}$ , where J is the main exchange interaction in the chain or layer and z is the number of the nearest neighbor interacting In the short-range ordered region, many interasting spins. magnetic behavior such as a broad peak in magnetic susceptibility and specific heat, the shift of g-value and the characteristic temperature dependent line width of ESR line have been observed by many researchers. In our laboratory, so far, ESR studies have been done to investigate the spin dynamics in the short-range ordering region as well as below  $T_N$  in some low dimensional antiferromagnets such as  $Cu(NH_3)_4SO_4 \cdot H_2O^{1}$ ,  $KCuF_3^{2}$ ,  $Cu(HCOO)_2 \cdot 4H_2O^{3}$ ,  $TMMC^{4}$ ,  $Cu(C_6H_5COO)_2 \cdot 3H_2O^5)$ ,  $CuCl_2 \cdot 2NC_5H_5^6$ ,  $Rb_2PbCu(NO_2)_6^7$  and  $Cu(ND_3)_{\mu}SO_{\mu}\cdot D_2O^{8}$  etc.

The series of the low dimensional magnet studies in our laboratory are now extended to  $CuSO_4 \cdot 5H_2O$ . According to the proton NMR experiments by Poulis et al.<sup>9), 10)</sup>, this crystal consists of weakly coupled two spin systems A and B, where A and B spins belong to the inequivalent A and B sites, respectively. The A spin system shows a characteristic of Heisenberg antiferromagnetic linear chain and exibits a transition to a long-range ordered state at  $T_c \simeq 100 \text{ mK}^{11}$ , even though the B system is still paramagnetic at this temperature. This partial ordering<sup>12)</sup> of the A

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spin in addition to the one-dimensional spin dynamics is one of the attractive subjects of the present ESR study.

ESR measurements of this compound were performed by Arnold and Kip<sup>13)</sup>, Wheatley and Halliday<sup>14)</sup> and Bagguley and Griffiths<sup>15)</sup>. The exchange splitting of ESR lines was first observed in Q band region by Bagguley et al.<sup>15)</sup> and the exchange interaction between two crystallographic inequivalent spins was determined to be about 0.11 K at room temperature. The low temperature ESR measurement down to 1.2 K was performed by Abe et al.<sup>16)</sup> in the plane containing the two inequivalent copper spins. They found that one of the two well-split lines at room temperature was anomalously broadened below 20 K at Q band measurements and they concluded that the line broadening comes from the short range ordering effect in the A site linear chain.

We performed the ESR measurements in  $\text{CuSO}_4 \cdot 5\text{H}_20$  using a combined cryostat of <sup>3</sup>He and adiavatic demagnetization in a temperature range from room temperature down to about 100 mK at 9, 17, 24, 35 and 45 GHz bands. One of the remarkable results is that the temperature dependent exchange interaction between two inequivalent sites of copper spins was observed above 70 K and it increases with decreasing temperature. The similar phenomenon was first observed by Okuda and Date<sup>17)</sup> in K<sub>2</sub>CuCl<sub>4</sub>·2H<sub>2</sub>O and K<sub>2</sub>CuCl<sub>4</sub>·2D<sub>2</sub>O. Another interesting result is that the temperature dependent shift of the resonance lines in a low temperature region below about 20 K to 0.5 K was observed. These resonance line shifts are analyzed by taking into account the H/T effect between the dissimilar sites A and B using the molecular field theory as

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was done in some copper compounds by Kuroda et al.<sup>18)</sup> These results are summerized in §3 and are discussed in §4.

# § 2 Crystal and Magnetic Structure

The X-ray analysis of the crystal structure of  $CuSO_4 \cdot 5H_2O$ was performed by Beevers and Lipson<sup>19)</sup> and neutron scattering experiment for the determinations of more detailed and complete atomic positions was done by Bacon and Curry<sup>20)</sup>. According to their results,  $CuSO_4 \cdot 5H_2O$  has a triclinic structure with space group  $C_i^1$ . The dimension of the unit cell is a = 6.141 Å, b = 10.736 Å and c = 5.986 Å, and the interaxial angles  $\alpha$  = 82° 16',  $\beta = 107^{\circ} 26^{\circ}$  and  $\gamma = 102^{\circ} 40^{-20}$ . The projection of the crystal structure on the ab-plane is shown in Fig. 1. The unit cell has two inequivalent  $Cu^{2+}$  ions at (0, 0, 0) and (1/2, 1/2, 0) positions, which are abbriviated as A and B sites, respectively, as shown in Fig. 1. Each of the two cupric ions is surrounded by four water molecules and two oxygen atoms of  ${\rm SO}_{\mu}^{2-}$  group in a slightly distorted octahedral arrangement as shown in Fig. 2. The nomenclatures in Figs. 1 and 2 were quoted from the paper of Beevers and Lipson<sup>19)</sup>. The two remaining  $H_2^0$  molecules  $9(H_2^0)$ and 9<sup>( $H_2^{0}$ )</sup> are at a somewhat long distance from both Cu<sup>2+</sup> ions at A and B sites. Local electric fields acting on the two  $Cu^{2+}$ ions are nearly tetragonal. The angle  $\theta$  between the two tetragonal axes of A and B sites which are defined as the lines connecting two oxygens belonging to the  $SO_{\mu}^{2-}$  group, and are called  $L_2$ and  $L_{4}$  directions<sup>15)</sup>, respectively, is 94.7°. The calculated

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angular relations between the crystal and the two tetragonal directions using the data of Bacon and Curry<sup>20)</sup> are shown in Fig. 3 and they are slightly different from those of previous data.<sup>21)</sup>

Magnetic and thermal properties of this single crystal of  $CuSO_{1} \cdot 5H_{2}O$  were studied by many reserchers<sup>21)-29)</sup>. A broad maximum in the specific heat<sup>24)</sup> was found near 1 K and it was first believed that the B site copper ions make a one-dimensional chains along the c-axis. Recent proton NMR experiments 9),10),30), however, showed that the A site copper ions along the a-axis are coupled by the dominant exchange interaction  $J/k_{\rm B}$  = -1.45 K and compose the bundle of linear chains along the a-axis. Further NMR and specific heat investigations<sup>11)</sup> in lower temperatures showed the onset of antiferromagnetic long-range order in the A site copper ions at about 100 mK, even though the B site copper ions are still paramagnetic down to about 35 mK<sup>29)</sup>. The interchain exchange energy among the A site chains was estimated to be  $zJ^{/k_{R}} \approx -0.14 \pm 0.03 \text{ K}^{11}$ . These peculiar magnetic phase transition was also obtained in the similar isomorphous systems such as  $CuSeO_{\mu} \cdot 5H_{2}O^{12}$  and  $CuBeF_{\mu} \cdot 5H_{2}O^{31}, 32$ .

The g-tensors of A and B sites have the tetragonal symmetry corresponding to the symmetry of the crystal field acting on the  $Cu^{2+}$  ions and the values were determined by ESR measurements to be

$$\begin{cases} g_{\parallel} = 2.412 \pm 0.005 \\ g_{\perp} = 2.102 \pm 0.005 \end{cases}$$

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(1)

where  $g_{\parallel}$  and  $g_{\perp}$  mean the principal g-values parallel and perpendicular to the tetragonal axis, respectively. These values are consistent with the results of previous work <sup>15)</sup>, <sup>16)</sup>. Though the local environment of two Cu<sup>2+</sup> ions belonging to the A and B sites is different, the principal g-tensors are almost the same. If the exchange interaction  $J_{AB}$  between two inequivalent sites A and B is sufficiently weak compared with the difference of the Zeeman energy between them, two well-split ESR lines should be observed. If the condition is opposite, two lines should be amalgamated. Considering the simplest exchange coupled two spin system, the splitting criterion is given as

 $\Delta g \mu_B H \simeq 2 J_{AB}$ 

where  $\Delta g = g_A - g_B$ , and  $g_A$  and  $g_B$  are g-tensors corresponding to two inequivalent copper spins. This exchange splitting phenomenon was first observed by Bagguley and Griffiths<sup>15)</sup> in the Q-band ESR at room temperature in CuSO<sub>4</sub>·5H<sub>2</sub>O. According to above criterion, the exchange constant  $J_{AB}$  was determined by them to be  $2J_{AB}/k_B \simeq$ 0.11 K at room temperature.

(2)

The linear chain mechanism of the exchange interaction may be understood by considering the configuration of the wave function of  $Cu^{2+}$  ions as follows: The  $Cu^{2+}$  ion in a tetragonal local environment has the ground state wave function of  $d(x^2-y^2)$ , which spreads in the plane of four  $H_2O$  molecules as shown in Fig. 2. This is confirmed by looking at the g-tensor symmetry. Thus, the exchange interaction through the path (I) of A site ions along the

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a-axis as shown in Fig. 4 is considered to be dominant, compared with the other exchange path (II) along the c-axis. Other exchange interactions, i.e., the A-B and intra-B site interactions may be small compared with the path (I) exchange.

### § 3 Experimental and Results

(1) Experimental

Electron spin resonance was performed in the temperature range from room temperature down to about 100 mK at 35 and 45 GHz bands. Above 1.2 K the conventional transmission type of cryostat with 100 kHz field modulation was also used at the frequency 9, 17, 24, 35 and 45 GHz. The temperature was measured by using  $AuCo_{2.1\%}$ -Cu thermocouple. Below 1.2 K the combined <sup>3</sup>He and adiavatic demagnetization cryostat was used. The detailed construction and operation of this cryostat are described in A in Part I.

The crystal was grown from saturated aqueous solution by slow evaporation at room temperature and it has a well-developed [0,0,1]-zone plane.

In every experiments the sample was checked by taking the angular dependence of ESR lines at 35 GHz at room temperature in order to ascertain the desired direction of the crystal and to avoid the twin crystal. The setting error of the crystal direction is less than about  $\pm$  5° in the all present ESR measurements.

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- (2) Summary of The Experimental Results
- (a) Temperature, Frequency and Angular Dependences of The Exchange Splitting

Most of the measurements were done in the plane including two tetragonal axes  $L_2$  and  $L_4$ . Only one exchange narrowed line was observed at the 9 GHz band in all temperature region. Its angular dependences of the resonance line and line widths at the 9.385 GHz at various temperatures are shown in Fig. 5.

At the 35 GHz band, the exchange splitting phenomena were observed around the  $L_2$  and  $L_{ll}$  axes as shown in Figs. 6 and 7. In Fig. 6, it is noticed that there exist two angles for the maximum separation corresponding to the  $L_2$  and  $L_{\parallel}$  axes and the angle between the both axes is about 90°. The separated lines amalgamate to one line at about 29°  $\pm$  2° from the L<sub>2</sub> or L<sub>4</sub> axes. The observed exchange splitting is satisfactorily explained by the model that the local tetragonal axis of the A site points in the L, direction while the tetragonal axis of the B site is parallel to the  $L_4$  axis as is pointed out by Bagguley and Griffiths<sup>15)</sup>. A new information given in Figs. 6 and 7 is the temperature dependence of the exchange splitting. If the exchange constant  $J_{AB}$  were temperature independent, the splitting pattern should not depend on temperature. However, a clear temperature dependence is observed in Figs. 6 and 7. This means that the exchange constant becomes large as temperature decreases. The detailed discussions will be shown in §4.

At the 45 GHz band, the similar exchange splitting pattern was obtained as shown in Figs. 8 and 9. At the 35.758 GHz the

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two split lines amalgamate to one line below about 70 K, while at the 45.35 GHz two separated lines can be observed.

The frequency dependence of the exchange splitting at room temperature is summalized in Fig. 10.

### (b) Resonance Shifts

Temperature dependences of the resonance line from room temperature to 1.2 K at the 9.385 GHz in the field parallel to the  $L_2$  and  $L_4$  axes are shown in Fig. 11. The resonance lines shift with decreasing temperature to lower and higher field sides when an external field H is applied to the  $L_2$  and  $L_4$  directions, respectively.

The temperature dependences of the exchange splitting lines above about 70 K at the 35.640 GHz are shown in Figs. 12 and 13, when the external field H is applied parallel to the  $L_2$  and  $L_4$ axes, respectively. The magnitude of the exchange splitting becomes small with decreasing temperature as was explained in (a) in this section. This means that the exchange constant  $J_{AB}$ clearly depends on temperature. With decreasing temperature below about 70 K, the temperature dependent shifts of the amalgamated line were observed at the 35.640 GHz. When the external field H is applied parallel to the  $L_2$  axis, the line shifts to higher field side between about 70 K and 0.5 K as shown in Fig. 12. When the field H is applied parallel to the  $L_4$  axis, the shift is opposite as shown in Fig. 13.

In the 45 GHz band, similar temperature dependence of the exchange splitting was observed above 70 K. However, the amalgama-

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tion does not occur even in the low temperatures and the lower field lines always shift to lower field side below about 20 K as shown in Figs. 14 and 15. The intensities of the lower field lines become weaker and weaker with decreasing temperature below some tens Kelvin. When the external field H is applied parallel to the  $L_2$  axis, the intensity of lower field line diminishes and the resonance line disapperas below about 3 K while the higher field line slightly shifts to higher field as shown in Fig. 14. When the field H is parallel to the  $L_4$  axis, both resonance lines shift to lower field side and they become constant below about 0.5 K as shown in Fig. 15.

### (c) Line Width

Angular dependences of the maximum slope width at 9 GHz band are shown in Fig. 5. The widths increase with increasing temperature above about 100 K in both  $L_2$  and  $L_4$  directions from about 80 Gauss to 150 Gauss. The temperature dependences of the line width are shown in Fig. 16.

The line widths in the 45 GHz band become sharper and sharper with decreasing temperature down to about 0.5 K and it becomes constant below about 0.5 K. Above 100 K the line widths rapidly decrease with decreasing temperature. The temperature dependences of the line widths at 45.388 GHz with the field H parallel to  $L_2$  and  $L_4$  axes are shown in Figs. 17 and 18, respectively. The widths in Figs. 17 and 18 are given by the full-half width.

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### § 4 Discussions

(1) Temperature Dependence of Exchange Interaction

The temperature dependent exchange constant  $J_{AB}$  is estimated by using the data in Figs. 6, 8, 12, 13, 14 and 15, as is shown in Fig. 19. The experimental results shows that the exchange interaction  $2J_{AB}/k_B$  between  $Cu^{2+}$  ions increases with decreasing temperature up to 0.24 K. Below about 70 K,  $J_{AB}$  becomes constant and it is about two times larger than that at room temperature. Our data of  $J_{AB}$  at room temperature is slightly larger than that of Bagguley and Griffiths<sup>15)</sup> as shown in Fig. 19.

There are two possible mechanisms for explaining the temperature dependence. One of the mechanisms is expressed in the following way: if there are two competing ferro- and antiferromagnetic interactions between the A and B sites and a small difference in temperature coefficients between the ferro- and antiferromagnetic interaction exists, the temperature dependence of the resultant exchange interaction will occur. The other one is that the exchange path between copper ions is modifyed by the rotational motion of  $H_20$  molecules connecting the A and B sites ions. It is known from the NMR experiment<sup>33)</sup> that the rotational vibration is strongly temperature dependent. Anyway, however, there is no definite evidence for explaining the large temperature dependence in  $J_{AB}$ .

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### (2) Paramagnetic Resonance Shift at Low Temperature

The shift of the resonance lines between about 20 K and 0.5 K as is shown in Figs. 14 and 15 can be explained in the following way.  $CuSO_4 \cdot 5H_2 \dot{Q}$  has two inequivalent sites A and B with different g-tensors and the both sites are coupled with a relatively weak exchange interaction compared with the difference of the Zeeman energy. When the one site spins in  $CuSO_4 \cdot 5H_2 O$  is just on resonance, the other site spins is at rest. The spins at rest give the molecular field due to the weak exchange coupling to the other site spins. As this molecular field should be proportional to the polarization of the spins at rest, the shift depends on both the temperature and magnetic field. The mechanism of the shift considered here different from the shift introduced by Nagata et al.<sup>34</sup>, <sup>35</sup> for explaining the shift in low dimensional magnets.

The shift discussed here was first presented by McMillan and Opechowski<sup>36)</sup>, <sup>37)</sup> using the technique of the moment expansion method. They calculated the first moment by using the trancation method of the total Hamiltonian taking into account the dissimilarity of the A and B spins under the condition that  $\Delta g\mu_B H >> 2J_{AB}$ . One of the experimental example to this theory was done by Svare and Seidel<sup>38)</sup> in K<sub>2</sub>Cu(SO<sub>4</sub>)<sub>2</sub>.6H<sub>2</sub>O. However, it is not suitable to apply above theory to the shift in the present case of CuSO<sub>4</sub>.5H<sub>2</sub>O because the exact calculation of the first moment is difficult and the condition is not always well satisfied.

Recently, the molecular field approach to the shift of the resonance lines was done by Kuroda et al.<sup>18)</sup> taking into account the H/T effect in order to analize the exchange splitting in some

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copper compounds such as  $(NH_4)_2CuCl_4 \cdot 2H_2O$ ,  $(NH_4)_2CuBr_4 \cdot 2H_2O$  and  $Cu(NH_3)_4SO_4 \cdot H_2O$  in submillimater ESR experiments at liquid <sup>4</sup>He temperature using pulse high magnetic field at Osaka University. This treatment is based on the classical molecular field theory of ferrimagnetic materials developed by Wangsness<sup>39</sup>.

The essential point of the theory is as follows. When there are two inequivalent spins with different g-tensors  $g_A$  and  $g_B$  in crystal, the system can be regarded as a two sublattice system of  $M_A$  and  $M_B$  with different g-tensors  $g_A$  and  $g_B$ , respectively. The treatment is not appropriate at high temperature region but it is applicable at low temperature because the polarizations of the sublattice magnetizations become large. The two sublattices are connected to each other by the molecular field coming from the exchange interaction between inequivalent sites A and B. The temperature dependence of the sublattice moments and it can be easily be calculated.

The resonance frequencies  $\omega^+$  and  $\omega^-$  given by Wangsness<sup>39)</sup> in a spherical and isotropic ferrimagnet can be written by

$$b^{\pm} = \{\gamma H - \frac{A}{2}(\gamma_{A}M_{Bz} + \gamma_{B}M_{Az})\}$$
  
$$\pm \frac{1}{2}[\{\Delta\gamma H - A(\gamma_{A}M_{Bz} - \gamma_{B}M_{Az})\}^{2} + 4\gamma_{A}\gamma_{B}A^{2}M_{Az}M_{Bz}]^{1/2}$$
(3)

where  $\gamma_A$  and  $\gamma_B$  are the gyromagnetic ratios of the two sublattices  $M_A$  and  $M_B$ , respectively.  $\gamma$  and  $\Delta \gamma$  are defined as  $\gamma = (\gamma_A + \gamma_B)/2$ and  $\Delta \gamma = \gamma_A - \gamma_B$ . The molecular field constant A is given by

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A =  $2zJ_{AB}/N\gamma_A\gamma_Bh^2$ , where N is the number of the spins in a sublattice, z is the number of interacting spins.  $M_{Az}$  and  $M_{Bz}$  are the magnetic moments along the field for A and B sublattices, respectively. The transverse components of them are assumed to be small. The shifts  $\Delta H^+$  and  $\Delta H^-$  corresponding to  $\omega^+$  and  $\omega^-$ , respectively, are written as

$$\Delta H^{+} = -\frac{1}{2} \{\delta H + A(M_{Az} + M_{Bz})\} + \frac{1}{2} [\{\delta H + A(M_{Bz} - M_{Az})\}^{2} + 4A^{2}M_{Az}M_{Bz}]^{1/2}$$
(4)

and

$$\Delta H^{-} = \frac{1}{2} \{ \delta H - A(M_{Az} + M_{Bz}) \}$$
$$- \frac{1}{2} [ \{ \delta H + A(M_{Bz} - M_{Az}) \}^{2} + 4A^{2}M_{Az}M_{Bz} ]^{1/2}, \qquad (5)$$

Where &H is the difference of the resonance fields at sufficiently high temperatures.

Temperature dependence of the resonance field was calculated as follows. As the exchange interaction  $J_{AB}$  between A and B sites was obtained by ESR measurements around 70 K to be  $2|J_{AB}|/k_B =$ 0.236 K, the molecular field constant A is calculated with z = 2assuming  $J_{AB}$  to be ferromagnetic. The temperature dependence of  $M_{Az}$  is obtained by using the experimental results of NMR<sup>10</sup>. On the other hand, the temperature dependence of  $M_{Bz}$  is obtained by a simple Brillouin function because the B site is paramagnetic.

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Hence, the shifts of the resonance fields  $\Delta H^+$  and  $\Delta H^-$  can be calculated by using eqs. (4) and (5), respectively.

The calculated  $\Delta H^+$  and  $\Delta H^-$  for the 45 GHz region are shown in Figs. 20 and 21, where the experimental results are also given. Satisfactory agreement between the theory and experiments is obtained for the B site, while a considerable deviation is found for the A site shift. The deviation in the A site may be explained by considering the short-range ordering effect<sup>34)</sup>. However, the numerical estimation is difficult because the calculation of the correlation function in our case is not so simple.

When the exchange interaction is ferromagnetic, the intensity of the lower field resonance should be weak<sup>18)</sup> and the experimental results support it. This result means that our assumption of the ferromagnetic  $J_{AB}$  is correct.

In 9 GHz region, a relation  $\Delta g\mu_B H \leq 2J_{AB}$  holds so that the resonance lines belonging to two different Cu<sup>2+</sup> ions are amalgamated by the exchange interaction. The molecular field theory can also be applicable for this condition. The resonance formula for the low frequency mode is written as<sup>39)</sup>

$$\omega = \gamma_{\text{eff}}^{\text{H}}, \qquad (6)$$

(7)

where

$$\gamma_{eff} = \frac{M_{Az} + M_{Bz}}{M_{Az} / \gamma_A + M_{Bz} / \gamma_B} .$$

The experimental results of the shift in  $CuSO_4 \cdot 5H_2O$  can satisfact-

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orily be described by the theory as shown in Fig. 22.

As shown in Figs. 17 and 18, the line widths decrease with decreasing temperature and they become constant below 0.5 K. If the A site is antiferromagnetic below about 100 mK<sup>11)</sup>, the short-range order broadening may occur near  $T_N$  but it is not observed. This may be understood by the model that the external field surpresses the spin fluctuation and the broadening effect is reduced.

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### Figure Caption

Fig. 1. Crystal structure of  $CuSO_4 \cdot 5H_2O$  projected on the ac plane. Unit cell consists of two inequivalent  $Cu^{2+}$  ions at A (0,0,0) and B (1/2,1/2,0) positions with different tetragonal axes  $L_2$  and  $L_4$ , respectively. Lattice constants and interaxial angles are also shown. The nomenclatures were quoted from Beevers and Lipson<sup>19)</sup>.

- Fig. 2. Local octahedral atomic arrangement around two inequivalent Cu<sup>2+</sup> ions A (0,0,0) and B (1/2,1/2,0). Atomic distances are also shown.
- Fig. 3. Angular relation between two tetragonal axes  $L_2$  and  $L_4$ , and crystal axes a, b and c. Interaxial angle  $\theta$  between two tetragonal axes  $L_2$  and  $L_4$  is 94.7°.
- Fig. 4. Probable exchange linkages about  $Cu^{2+}$  ion at A (0,0,0).
- Fig. 5. Angular dependence of the amalgamated line and its width at 9.385 GHz at various temperature.
- Fig. 6. Angular dependence of the exchange splitting in  $L_2L_4$ plane at 35.758 GHz above 70 K. Two exchange split lines were observed around  $L_2$  and  $L_4$  axes forming two circles in the plane and they shrink with decreasing temperature.
- Fig. 7. Angular dependence of the amalgamated line in  $L_2L_4$  plane at 35.758 GHz in low temperature region. Only one line is observed in all directions. Angular dependence of the exchange splitting at room temperature is also given in the figure.
- Fig. 8. Angular dependence of the exchange splitting in  $L_2L_4$ plane at 45.35 GHz above 70 K. Two exchange split lines

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are observed around  $L_2$  and  $L_4$  axes.

- Fig. 9. Angular dependence of the exchange splitting in  $L_2L_4$ plane at 45.515 GHz in low temperature region. Angular dependence of the exchange splitting at room temperature is also given in the figure.
- Fig. 10. Frequency dependence of the exchange splitting at room temperature when the external field H is parallel to  $L_2$  axis. Exchange splitting occurs at 18 GHz and the estimated exchange constant  $2|J_{AB}|/k_B$  is about 0.12 K.
- Fig. 11. Temperature dependent shifts of the amalgamated line at 9.411 GHz when the external field H is parallel to  $L_2$  and  $L_{\mu}$  axes.
- Fig. 12. Temperature dependence of the exchange splitting at 35.640 GHz from room temperature down to about 100 mK when external field H is parallel to L<sub>2</sub> axis. The temperature dependent exchange splitting is observed above 70 K.
- Fig. 13. Temperature dependence of the exchange splitting at 35.640 GHz from room temperature down to about 100 mK when the external field H is parallel to  $L_4$  axis. The temperature dependent exchange splitting is observed above 70 K.
- Fig. 14. Temperature dependence of the exchange splitting at 45.388 GHz from room temperature down to about 100 mK when the external field H is parallel to L<sub>2</sub> axis. Below about 3 K, the lower field resonance line diminishes and disappears.

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- Fig. 15. Temperature dependence of the exchange splitting at 45.388 GHz from room temperature down to about 100 mK when the external field H is parallel to  $L_4$  axis.
- Fig. 16. Temperature dependence of the amalgamated lines at 9.411 GHz when the external field H is parallel to  $L_2$  and  $L_h$  axes, respectively.
- Fig. 17. Temperature dependence of the resonance line widths at 45.388 GHz when the external field H is parallel to  $L_2$  axis.
- Fig. 18. Temperature dependence of the resonance line widths at 45.388 GHz when the external field H is parallel to  $L_4$  axis.
- Fig. 19. Temperature dependence of the exchange interaction J<sub>AB</sub> between A and B sites Cu<sup>2+</sup> ions. Exchange constants obtained by Bagguley et al.<sup>15)</sup> at room temperature are also given by open circles, respectively.
- Fig. 20. Comparison between experimental results and molecular field theory at 45.388 GHz when the external field H is parallel to L<sub>2</sub> axis.
- Fig. 21. Comparison between experimental results and molecular field theory at 45.388 GHz when the external field H is parallel to  $L_{h}$  axis.
- Fig. 22. Comparison between experimental results and molecular field theory at 9.411 GHz when the external field H is parallel to  $L_2$  and  $L_{ll}$  axes, respectively.

-78-



-79-



-80-



# Fig. 3





total 7.29 Å



total 7.73 Å



-82-



Fig. 5

-83-



Fig.6

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-87-



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### Part III

Magnetic and Superconducting Phase Transitions in  $\text{Er}_{c} \text{Y}_{1-c} \text{Rh}_{4} \text{B}_{4}$ 

#### Synopsis

In magnetoresistance measurements in  $\mathrm{Er_{c}Y_{1-c}Rh_{4}B_{4}}$  from its superconducting transition temperature  $\mathrm{T_{c1}}$  to 80 mK, the  $\mathrm{T_{c1}}$  and the reentering temperature  $\mathrm{T_{c2}}$  were determined as a function of the concentration of Er. Comparing our results with the recent theory of Maekawa et al., the exchange interaction J' among local spins and I between local spins and superconducting electrons were estimated as J'  $\simeq$  0.3 K and  $\mathrm{I}^{2}\mathrm{N}(0) \simeq 0.046$  K, where N(0) is the density of state. A sudden decrease of  $\mathrm{H_{c2}}$  at  $\mathrm{T_{c2}}$  suggesting the first order transition was observed in a high concentration region.

In magnetization measurements from 4.2 K to 0.5 K up to 29 kOe, an anomalous temperature dependence of magnetization suggesting the presence of a new phase predicted by the theory was found in  $\text{ErRh}_4\text{B}_4$  in narrow temperature region between 1.0 K and about 1.4 K in low fields H  $\simeq$  0  $\sim$  400 Oe.

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## § 1 Introduction

Since the discovery of the re-entrant superconductivity in the ternary compounds (RE)Rh<sub>4</sub>B<sub>4</sub> by Fertig et al.<sup>1)</sup> and in the ternary Chevrel-phase compounds (RE)  $Mo_6S_8$  and (RE)  $Mo_6Se_8$  (x = 1.0  $\sim$  1.2) by Ishikawa et al.<sup>2)</sup>, where (RE) means a rare earth element, there have been growing interest on superconductivity and magnetic properties in these compounds containing a rare earth ion with localized moment. Generally speaking, in the case of impurity spins in superconductors the fluctuation of local spins inside a superconductor acts on a Cooper pair as a pair-breaker, therefore, weakens the BCS coupling. So the T usually strongly depends on the concentration of impurity spins. However, one of the surprising features of our superconductors is an extreemly weak depression of T<sub>cl</sub> in spite of the presence of localized magnetic moment. Recently, the theoretical formulations of these problems for superconducting and magnetic transition temperatures in the rare earth ternary superconductors were presented by Maekawa and tachiki<sup>3)</sup> as functions of the intra- and interatomic exchange interactions and the concentration of local spins. То verify their theory, it is desired to investigate the dependence of  ${\rm T}_{_{\rm M}}$  and  ${\rm T}_{_{\rm M}}$  on the concentration of local spins.

Another surprising feature in these ternary compounds is the coexistence of superconductivity and magnetic long range order. Up to the present, the coexistence of superconductivity and antiferromagnetic order on Chevrel-phase compounds  $(\text{RE})_{1.2}\text{Mo}_6\text{S}_8$  for RE = Gd, Dy and Tb was comfirmed by neutron scattering experiments. 4),5),6) In addition to these compounds, the coexistence have

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been inferred in  $\operatorname{Er}_{1.2}\operatorname{Mo}_6\operatorname{S}_8^{7)}$ , and the same kinds of selenide compounds<sup>8),9)</sup>. However, no clear experimental evidence have been found for the coexistence of superconductivity and long-range ferromagnetic order. Actually, in a ferromagnetic superconductor  $ErRh_4B_4$  which becomes superconducting at  $T_{c1} = 8.7$  K and returns to normal state at  $T_{c2} \approx 0.8 \text{ K}^{(1),10)}$ , heat capacity (1),11),12and neutron diffraction experiments 13),14) have shown that the destruction of superconductivity at  $T_{c2}$  is accompanied by the development of long-range ferromagnetic order of magnetic ions. Quite recently, the appearence of helical spin order in ferromagnetic superconductor  $\text{ErRh}_{\underline{l}}B_{\underline{l}}$  in the superconducting state just above the ferromagnetic ordering temperature is theoretically expected<sup>15),16),17),18)</sup>. However, this possibility is still controversial. There is no obvious experimental result for verifying the coexistence of the superconductivity and helical spin ordering near  $T_{c2}$  except for the suggestive neutron scattering data<sup>13),14).19)</sup>. To investigate this possibility we have precisely measured the magnetization of  $ErRh_{4}B_{4}$  around  $T_{c2}$  by using newly developed fluxgate magnetometer. The concentration dependence of  $T_{c1}$  and  $T_{c2}$  and the temperature and concentration dependence of the upper critical field  $H_{c2}$  in  $Er_{c}Y_{1-c}Rh_{4}B_{4}$  are also measured.

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## § 2 Crystal and Electronic Structure

X-ray diffraction experiment of (RE) $Rh_{\mu}B_{\mu}$  was performed by Vandenberg et al.<sup>20)</sup> as a series of investigation of crystal structures of ternary rhodium borides. The compounds (RE)Rh<sub>ll</sub>B<sub>ll</sub> with RE = Y, Nd, Sm, Gd, Tb, Dy, Ho, Er, Tm, Lu and Th have the same crystal structure with body-centered tetragonal lattice and space group P42/nmc which is shown in Fig. 1. However, some elements such as Sc, La, Ce, Pr, Eu and Yb do not form (RE)Rh $_4B_4$ compounds. Th, Y, Nd, Sm, Er, Tm and Lu form superconducting compounds while Gd, Tb, Dy and Ho yield ferromagnetic phase with no superconductivity. Their superconducting transition temperatures are by far the highest yet observed for any borides. This superconducting behavior is in sharp contrast to that previously found for the ternary Chevrel-phase compounds (RE)  $Mo_6 S_8^{21}$  and (RE)Mo<sub>6</sub>Se<sub>8</sub><sup>22)</sup>, where x = 1.0  $\sim$  1.2. Every rare earth compound has been to form a Chevrel-phase sulphide and selenide with the exception of the Ce and Eu compounds, and they are all superconducting.

A comparison of electronic and magnetic properties in the series of these ternary rhodium boride compounds in particularly interesting. Though any obvious differences in the crystal and magnetic structures can not be found in the series of these compounds, quite different electronic and magnetic properties appears. The a/c ratio is almost constant in all these compounds and the value of the effective moment  $\mu_{eff}$  does not show any anomalous behavior. The series of these compounds can be clearly divided to two groups, i. e., Gd, Tb, Dy and Ho group with ferromagnetic

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and no superconducting phase, and Er, Tm and Lu group with superconducting phase. Especially, there exist a clear difference between the neighboring rare earth ions Ho and Er. HoRh<sub> $\mu$ </sub>B<sub> $\mu$ </sub><sup>23)</sup> is ferromagnetic below 6.5 K while  $\text{ErRh}_{\mu}\text{B}_{\mu}$  shows the superconducting transition at 8.7 K. However, the effective magnetic moments of both rare earth ions are close to each other. It is 10.6  $\mu_{\rm R}$ for Ho and 9.6  $\mu_{\rm R}$  for Er and the difference is only 10 %. This fact suggests that the electronic and magnetic properties of these ternary rhodium boride compounds may strongly be modified by delicate changes in the electronic structure, magnetic interactions and so on. In Chevrel-phase compounds it is experimentally concluded that the superconducting properties are mainly determined by the  $Mo_6^{-}$  clusters and their relative positions<sup>24</sup>. The exchange interactions among 4f local spins are mainly produced by 6s conduction electrons and the contribution coming from 4d electrons, i.e., the superconducting electrons due to Mo<sub>6</sub> is negligibly small. It is believed that the electronic and magnetic interaction mechanisms of (RE)Rh $_{\mu}B_{\mu}$  are similar to those of the Chevrel-phase compounds. This picture in ternary rhodium boride compounds (RE)Rh $_4B_4$ was supported by the selfconsistent energy band calculations<sup>25),26)</sup> 27) and was also adopted to the theory of Maekawa and Tachiki<sup>3)</sup>.

The relatively weak magnetic interaction between the 4f localized moments by 5d and 6s electron bands of Er atoms leads to a magnetic ordering at  $T_M$ . However, once the superconducting state has been realized, the exchange interaction is reduced because of disappearence of polarization of conduction electrons due to the superconductivity.

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## § 3 Experimental

(1) Sample Preparation

The sample of  $\operatorname{Er}_{c} \operatorname{Y}_{1-c} \operatorname{Rh}_{4} \operatorname{B}_{4}$  was synthesized from high purity oxide  $\operatorname{Er}_{2} \operatorname{O}_{3}$  (99.9 %) and elements Rh (99.9 %), B (99.8 %) and Y (99.9 %) from Shinetsu Chemical Co. Ltd.. In order to get a high stoichometry, considerable care was taken as follows. The first step is the synthesis of binary compounds MB<sub>4</sub>, where M means Er or Y. Generally speaking, the hexaboride MB<sub>6</sub> is more stable compared with MB<sub>2</sub>, MB<sub>4</sub> and MB<sub>12</sub>. In ErB<sub>6</sub>, however, it is exceptionally unstable<sup>28)</sup>. ErB<sub>4</sub> was made from  $\operatorname{Er}_{2} \operatorname{O}_{3}$  by using the induction heating method according to the reaction given by

$$Er_2O_3 + 10 B \longrightarrow 2 ErB_4 + B_2O_3$$
 (gas). (1)

The procedure is as follows. Powdered  $\operatorname{Er}_{2}O_3$ , which is of pale pink, is mixed with powdered boron. The mixture was pressed by 100 kg/cm<sup>2</sup> in the form of disk (13 mm in diameter and 3  $\sim$  5 mm in thickness). The disk was heated by induction furnace in a graphite crucible at about 2000 °C for one hour. The excess boron get off as a gas of  $B_2O_3$  during the chemical reaction. Other compounds,  $\operatorname{ErB}_2$  and  $\operatorname{ErB}_{12}$  were not found in our disk. Synthesized  $\operatorname{ErB}_4$  is gray. YB<sub>4</sub> was made by conventional arc-melting method. When induction method was used, it was difficult to make a single phase of YB<sub>4</sub>. The reason is not yet clear. Probably the cooling speed in the arc-melting method is faster than that of the induction method and YB<sub>2</sub> or YB<sub>6</sub> can not be produced under the rapid cooling procedure. The reaction is thus simply explained according to the following as

$$Y + 4 B \longrightarrow YB_{\mu}$$

(2)

This tetraboride is gray. and can easily distinguish from hexaboride which is blue. As the second step, the ternary compounds  $MRh_4B_4$  were prepared by induction or arc-melting of two constituents  $MB_4$  and Rh under 1/3 atmospheric pressure of Ar according to the following reaction formula as

$$MB_{\mu} + 4 Rh \longrightarrow MRh_{\mu}B_{\mu} \qquad (M = Er \text{ or } Y) \qquad (3)$$

The synthesized sample of  $MRh_4B_4$  was confirmed by X-ray diffraction. In the final step,  $Er_cY_{1-c}Rh_4B_4$  and  $YRh_4B_4$  were synthesized by arc-melting with appropriate mixture of  $ErRh_4B_4$  and  $YRh_4B_4$ .

The annealing were done at 1050 °C for one week and an X-ray analysis was done to check the crystal structure. The X-ray analysis also shows that a weak trace of RhB phase remaines in addition to the tetragonal  $\mathrm{Er_{c}Y_{1-c}Rh_{4}B_{4}}$  phase. The impurity phase is almost independent of the heat treatments and the concentration of Er.

The concentration of Er was determined by X-ray flourescence method. As the results, the concentration c of 13 kinds of ternary borides were produced with c = 0.00, 0.13, 0.17, 0.26, 0.29, 0.44, 0.53, 0.65, 0.71, 0.72, 0.82, 0.88 and 1.00.

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# (2) Experimental Procedure

The measurements of dc electrical resistance of  $\mathrm{Er_{c}Y_{1-c}Rh_{4}B_{4}}$ was done using adiabatic demagnetization refrigerator combined to <sup>3</sup>He stage from 4.2 K down to 80 mK. Above 4.2 K the conventional cryostat was used. Superconducting transition temperature  $T_{c1}$ and the reentrant temperature  $T_{c2}$  were determined by measuring the magnetoresistance using conventional four-probe method. The sample was cut by spark cutter in the form of about 0.5 mm  $\times$  0.5 mm  $\times$  1 cm and copper wires of 0.05 mm in diameter were spot welded on to the sample. The data below 1 K were taken with increasing temperature only. The current used in the present resistance measurements was 1 mA for all cases. The fluxflow resistance which usually appears in large current measurements was negligible in the present small current measurement.

Two kinds of magnetization measurements were done by the fluxgate magnetometer method using two kinds of  ${}^{3}$ He cryostats down to about 0.5 K. One of the measurements is due to the extracting sample method and the other one is the temperature variation method under a fixed magnetic field. The magnetic field is always supplied parallel to the long dimension of the sample. Absolute value of the magnetization was calibrated by comparing with the static measurements with the same sample by the Faraday method. The characteristics of these apparatus are described in B in Part (I) in detail.

#### § 4 Results and Discussions

### (1) Magnetoresistance Measurements

The magnetoresistance curves were taken in the temperature range from 80 mK up to  $T_{c1}$  for a whole concentration region in  $Er_{c}Y_{1-c}Rh_{4}B_{4}$ . Typical examples at 80 mK are shown for c = 1.00, 0.44 and 0.17 in Fig. 2. The virgin curve for c = 0.44 rises abruptly at a threshold field  ${\rm H}_{\rm s}$  of about 2 kOe, and reaches a normal resistance at about 4 kOe. For decreasing field the curve does not follow the virgin curve but gives a finite resistance value at zero field. After that, the magnetoresistance curve follows the initial decreasing field curve with field up and down as shown by double arrows in Fig. 2. Similar virgin behavior was observed in a concentration region  $c = 0.44 \sim 0.65$ , where the threshold field H decreased with increasing the concentration. No such virgin curve was observed in high (c = 0.70  $\sim$  1.00) and low (c =  $0.00 \sim 0.40$ ) concentration regions. Instead, only a reversible curve was observed for the field up and down as is shown in Fig. 2. The cause for the peculiar virgin behavior in the region c = 0.44  $\sim$  0.65 might be that below  $T_{M}$  an inhomogeneous superconducting phase remains, because of the closeness to the critical concentration  $C_c = 0.43$  for long-range magnetic order as is shown below. This inhomogeneous superconducting phase disappears after the initial increasing field. The temperature dependence of the magnetoresistance curve was taken for all concentrations and an example for c = 0.44 is shown in Fig. 3. The resistance value at zero field falls to zero at 0.11 K and a hysteresis curve was observed up to about 0.5 K. Hereafter, we define the

temperature at which the zero field resistance in non-yirgin state falls to zero as the lower critical temperature  $T_{c2}$ , and the temperature at which it returns to the normal value at high temperature as  $T_{c1}$ . The hysteresis curves were observed in a narrow temperature region above  $T_{c2}$  for the concentrations  $c = 0.44 \sim 1.00$ .

The temperature dependences of electrical resistance at various magnetic fields are also shown in Fig. 4 for c = 1.00, 0.44 and 0.17 as the typical examples. The destruction of superconductivity at  $T_{c2}$  at zero field for c = 1.00 is relatively sharp with appreciable hysteresis. Fertig et al<sup>1)</sup>. found a small peak mar  $T_{c2}$  but it was not observed in our data.

The obtained concentration dependences of  $T_{cl}$  and  $T_{c2}$  are shown in Fig. 5. Open and black circles denote  $T_{cl}$  and  $T_{c2}$ , respectively. The present results of  $T_{cl} = 8.7$  K and  $T_{c2} = 0.79$ K in  $\text{ErRh}_4B_4$  are in agreement with the results of Matthias et al.<sup>1)</sup>, <sup>10)</sup>. They showed that the transition at  $T_{c2}$  in  $\text{ErRh}_4B_4$ found from the magnetoresistance coincides with the onset of longrange magnetic order of Er sublattice. So we assume that the temperature  $T_{c2}$  coincides with the magnetic ordering temperature  $T_M$  in a whole concentration region in  $\text{Er}_c Y_{1-c} \text{Rh}_4 B_4$ . The concentration dependence of  $T_M$  in the present system is given by Oguchi's theory<sup>29)</sup> in a magnetically diluted system as<sup>3)</sup>

$$T_M/J^2 = 2/\ln \{z^2/(z^4)\},$$
 (4)

where J' is the nearest neighbor exchange interaction among Er spins and z' is the reduced concentration defined by z' = 1 +

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 $7c\{1-(1-c)^8\}$ . By best fitting eq. (4) with the observed concentration dependence in  $T_{c2}$ , the value of J' was estimated as J'  $\approx$  0.30 K, and the theoretical line was calculated as shown by the dashed line in Fig. 5. The observed  $T_{c2}$  shows good agreement with the theoretical line of  $T_{M}$  and suggests a critical concentration of  $C_c \approx 0.43$  for the long range magnetic order. The concentration dependence of  $T_{c1}$  reduced by the transition temperature  $T_{c0}$  without magnetic spins is given by Maekawa and Tachiki<sup>3)</sup> as

$$T_{cl}/T_{c0} = \exp[1/g_{BCS}N(0) - 1/\{g_{BCS}N(0) - \frac{6I^2N(0)Co}{T_{cl}} \frac{1}{f_2}\ln(1+\frac{f_2}{f_1})\}],$$
(5)

where  $g_{BCS}$  and I are the BCS interaction parameter and the exchange interaction between local spins and superconducting electrons, respectively. N(0) is the density of state and Co<sup>-</sup> is the reduced concentration defined by Co<sup>-</sup> = cfl-(1-c)<sup>8</sup>} $\frac{1}{3}$ S(S+1). f<sub>1</sub> and f<sub>2</sub> are functions of T<sub>c1</sub>, J<sup>-</sup> and concentration c<sup>3)</sup>. These parameters are given by Maekawa and Tachiki<sup>3)</sup>. Their theory is applicable in high concentration region. So we tried a quantitative comparison of eq. (5) with our experimental results in high concentration regions. The parameter I<sup>2</sup>N(0) in eq. (5) is the most decisive factor for determining the increaseing rate in T<sub>c1</sub> when the concentration c decreases from c = 1. By best fitting eq. (5) with our results in a high concentration region, the value of I<sup>2</sup>N(0) was determined as 0.046 K. The other parameters were taken as T<sub>c0</sub> = 10 K and  $g_{BCS}N(0) = 0.3^{3}$ . The theoretical line for T<sub>c1</sub> is given

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### by a solid line in Fig. 5.

In this paper we define the upper critical field  $H_{c2}$  as the field at which the electrical resistance begins to rise from zero with increasing magnetic field. The anisotropy of  $H_{c2}^{31}$  is expected in the present crystal which has a tetragonal symmetry, and the anisotropy may induce a broad transition at the upper critical field in the polycrystalline specimen as seen in Figs. 2 and 3. Thus, our defined  $H_{c2}$  may correspond to a minimum value in the anisotropic H2. The temperature dependence of H22 was measured in a whole concentration region and the results are shown in Fig. 6.  $H_{c2}$  in the Er doped compounds has a broad peak near 4 K and decreases with decreasing temperature. The decrease in H22 at low temperatures is explained as follows<sup>32)</sup>: in the mixed state the persistent current of vortices induces a magnetic field and this field polarizes the Er spin moments. Along the vortex current, the spin magnetization contributes to the magnetic flux. The total flux which is the sum of the spin and current contributions is quantized. Then this flux quantization leads to the following facts: the vortex current is drastically affected by the spin polarization of Er at low temperatures and the current inversion occurs in some part of the vortex. The current inversion causes the attractive force between the vortices. As the result, when the spin magnetization increases at low temperatures, the superconducting state becomes unstable and  $H_{c2}$  decreases. The sample with low concentrations of Er ions (c =  $0.3 \sim 0.17$ ) showed a clear small minimum of  $H_{c2}$  near 0.2 K as is shown in Fig. 6. It was noted in Fig. 6 that  $H_{c2}$ , in high concentration specimens with

c = 1.0  $\sim$  0.8, decreases suddenly at  $T_{c2}$ . This sudden decrease in  $H_{c2}$  suggests the first order transition at  $T_{c2}^{15}$ . It was also noted that the zero field resistance below  $T_{c2}$  is about 60 % of normal values and the positive magnetoresistance was observed as shown in Fig. 2. The origin of the reduced resistance below  $T_{c2}$ may be due to partially remained superconducting phase in polycrystalline sample. The reduction disappears by applying a magnetic field.

### (2) Magnetization Measurements

Precise temperature dependences of magnetization in  ${\rm ErRh}_{ll} B_{ll}$ were measured between 0.5 K and about 2.0 K up to 29 kOe as shown in Figs. 7 and 8. In the case of H = 215 Oe, for example, the magnetization is negative and constant down to about 1.1 K due to the Meissner effect. Then the magnetization increases crossing the zero line and becomes constant below about 0.8 K. As the electrical resistance appears at 0.83 K with decreasing temperature in the same field, the induced magnetization may be due to the onset of the ferromagnetic transition. The transition temperature determined from the magnetoresistance is shown by open circles on the magnetization curve. When the temperature increases from about 0.5 K to about 2 K, a large hysteresis is observed. Generally speaking the magnetic moment persists even above T<sub>c2</sub> determined from the magnetoresistance. The main part of the excess large magnetic moment observed under the increasing temperature may come from the residual vortecies persisted in the sample. However, the magnetization at H = 215 Oe shows a curious plateau

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between 1 K and 1.4 K and this might reflect the existence of the melical spin ordering. The hysteresis decreases as the field increases and it is not observed above about 2 kOe. The magnetization curve under a strong field is shown in Fig. 8. The value of the induced magnetization at 0.5 K is about 6.5  $\mu_{\rm B}$ /Er ion even at about 29 kOe and it is considerably smaller than that of 9.0  $\mu_{\rm B}$ /Er expected from the ground state  ${}^{4}{\rm I}_{15/2}$  of Er $^{3+}$ . We also tried to observe the high field magnetization curve by using the D-1 Magnet of The High Magnetic Field Laboratory, Osaka University and the results is given in Fig. 9.

The magnetization curves in  $\text{ErRh}_{\mu}\text{B}_{\mu}$  at various temperature around  $T_{c2}$  were also measured by extracting sample method only in low field regions up to 3 kOe as shown in Fig. 10. The magnetic field in Fig. 10 means a measured field under the increasing field In the low field region above 0.8 K, i.e., higher than  $T_{r2}$ scan. the negative magnetization due to the Meissner effect is observed and the magnitude is  $-H/4\pi$  up to  $H_{cl}$ . Above  $H_{cl}$  the Meissner state is destroyed and the magnetization begins to increase as shown in Fig. 10. Therefore, the magnetization curve shows the minimum at the critical field H<sub>cl</sub>. The temperature dependence of H<sub>cl</sub> is shown in Fig. 11. The determination of H<sub>cl</sub> in these material is usually very difficult. However, we can find it because the fluxgate magnetometer is very sensitive even at low field In Fig. 11, H<sub>c2</sub> obtained by the magnetoresistance measurregion. ments is also given. It is noticed that all magnetization curves below T<sub>c2</sub> does not show the temperature dependence. Simply speaking, the magnetization curve looks like a paramagnetic magneti-

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zation. There is no hysteresis loop. If the crystal has the domain structure such as usual ferromagnets, a large hysteresis should be expected in the magnetization curve. The reason is not clear yet.

The hysteresis curve in  $\mathrm{ErRh}_{4}\mathrm{B}_{4}$  above  $\mathrm{T}_{\mathrm{c2}}$  at 1.33 K, where the hysteresis is largest, is shown in Fig. 12. In the virgin state, the magnetization is diamagnetic below  $\mathrm{H}_{\mathrm{c1}}$  due to the Meissner effect. Above  $\mathrm{H}_{\mathrm{c1}}$  the vortex state is stabilized between  $\mathrm{H}_{\mathrm{c1}}$  and  $\mathrm{H}_{\mathrm{c2}}$ . As seen in the usual type II superconductors the vortex state is irreversible to magnetic field. Therefore, once the vortex state is stabilized, the vortices are trapped and remain in the specimen after removing the magnetic field. The hysteresis curve in Fig. 12 may be explained by the vortex trapping. The hysteresis decreases as temperature, increases and diminishes at  $\mathrm{T}_{\mathrm{c2}}$ .

# § 5 Concluding Discussions

Electrical and magnetic properties of  $\text{ErRh}_4\text{B}_4$  and the mixed crystal with  $\text{YRh}_4\text{B}_4$  are studied and many informations are obtained as are summerized below. The first aim of the present paper is to find the concentration dependences of  $\text{T}_{c1}$ ,  $\text{T}_{c2}$  and  $\text{H}_{c2}$  in the mixed crystals and to check the recent theory of Maekawa and Tachiki<sup>3)</sup>. The agreement with the theory is satisfactory except the dilute region of Er.  $I^2N(0)$  was obtained to be 0.046 K from the concentration dependence of  $\text{T}_{c1}$ . This value means that the exchange coupling between localized 4f electron of  $\text{Er}^{3+}$  and super-

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conducting 4d electrons of Rh is very weak. This means that the localized magnetic moment does not give a strong influence upon the superconducting electrons. However, the magnetic coupling between 4f electrons via 6s band is not so weak and the ferromagnetic order below  $T_{c2}$  may occur due to the indirect coupling and the superconducting state may be destroyed by this magnetization. This model was proposed by Maekawa and Tachiki<sup>3)</sup> and our experimental results does not contradict to their theory. In pure  $ErRh_4B_4$ , the temperature dependence of  $H_{c2}$  suggests the first order transition near 0.8 K. However, the confirmation is difficult by looking at  $H_{c2}$  only.

The temperature dependence of  $H_{cl}$  is obtained in pure  $ErRh_{4}B_{4}$ down to its ferromagnetic critical temperature  $T_{c2}$ . This can be obtained by using the fluxgate magnetometer which is very effective even in a very weak field.

As predicted by the theory  $^{15),16),17),18}$  and suggested by neutron scattering data  $^{13),14),19}$ , some anomalous behaviors in magnetoresistance, magnetization curve etc. should be expected if the helical spin order appears near  $T_{c2}$ . We found an anomalous large hysteresis and a curious plateau in the magnetization curve between 1.0 K and 1.4 K. This may suggest the coexistence of the helical spin order in the superconducting state. However, the low field magnetization curve around this temperature region does not show any anomalies. It is also curious that the anomalous magnetization plateau in decreasing temperature can not be found. In the ferromagnetic state, the magnetization curve does not show the hysteresis. This means that the remanence is negligibly small.

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It is also interesting that the magnetization curve does not show a steep increase but show a gradual, say a paramagnetic, magnetization. The high field magnetization up to 360 kOe was also measured but a large increase in magnetization was not found.

Finally, one must say about the necessity of the single crystal experiment. We now have no informations about the magnetic anisotropy of the ferromagnetic state, the domain structure and the electrical conductivity tensor. These are very important for investigating the further details of the magnetic and electrical properties of these compounds. We once tried to make a single crystal with aid of Professor T. Komatsubara in Tohoku University. However, no good single crystals were obtained. It is still doubtful whether one can make a good single crystal in the series of the mixed  $\operatorname{Er}_{c}Y_{1-c}\operatorname{Rh}_{4}B_{4}$  compound or not.

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#### Figure Caption

- Fig. 1. Crystal structure of  $(RE)Rh_{\parallel}B_{\parallel}$ .
- Fig. 2. Magnetoresistance curves of  $\text{Er}_{c}Y_{1-c}\text{Rh}_{4}B_{4}$  with c = 0.17, 0.44 and 1.00 at 80 mK.  $R_{max}$  means the resistance in the normal state at high fields.
- Fig. 3. Magnetoresistance curves of  $\text{Er}_{0.44}\text{Y}_{0.56}\text{Rh}_4\text{B}_4$  as a parameter of temperature.
- Fig. 4. Temperature dependences of the magnetoresistance in various fields in  $\text{Er}_{c}Y_{1-c}\text{Rh}_{4}B_{4}$  with c = 1.00, 0.44 and 0.17.
- Fig. 5. Concentration dependences of  $T_{cl}$  and  $T_{c2}$  in  $Er_c Y_{l-c} Rh_4 B_4$ . Open and black circles denote  $T_{cl}$  and  $T_{c2}$ , respectively.
- Fig. 6. Temperature dependence of  $H_{c2}$  in  $Er_c Y_{1-c} Rh_4 B_4$  as a parameter of Er concentration.
- Fig. 7. Temperature dependence of magnetization around  $T_{c2}$  in ErRh<sub>4</sub>B<sub>4</sub> in low magnetic field region. The phase boundaries between paramagnetic and superconducting phase, and ferromagnetic and normal phase are shown by the solid lines (open circles mean the ferromagnetic transition temperatures with decreasing temperatures and squares mean that with increasing temperatures).
- Fig. 8. Temperature dependence of magnetization around  $T_{c2}$  in ErRh<sub>4</sub>B<sub>4</sub> in high magnetic field region up to 29 kOe.
- Fig. 9. Magnetization curves in  $\text{ErRh}_4\text{B}_4$  under the high magnetic field up to 360 kOe at 4.2 K and 1.3 K.
- Fig. 10. Low field magnetization curves of  $\text{ErRh}_4\text{B}_4$  at various temperatures obtained by extracting sample method.

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Fig. 11. Temperature dependences of  $H_{cl}$  and  $H_{c2}$  in  $ErRh_4B_4$ . Fig. 12. Hysteresis curve in  $ErRh_4B_4$  at 1.33 K.







Rh • B

space group P42/nmc

RE = Y, Nd, Sm, Gd, Tb, Dy, Ho Er, Tm, Lu, Th

# Fig.1

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Fig. 2

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Fig.4

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ErRh<sub>4</sub>B<sub>4</sub>

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