<table>
<thead>
<tr>
<th><strong>Title</strong></th>
<th>Modulated photoconductivity study of electron drift mobility in amorphous silicon</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Author(s)</strong></td>
<td>Hattori, K.; Iida, M.; Hirao, T. et al.</td>
</tr>
<tr>
<td><strong>Citation</strong></td>
<td>Journal of Applied Physics. 2000, 87(6), p. 2901-2909</td>
</tr>
<tr>
<td><strong>Version Type</strong></td>
<td>VoR</td>
</tr>
<tr>
<td><strong>URL</strong></td>
<td><a href="https://hdl.handle.net/11094/2925">https://hdl.handle.net/11094/2925</a></td>
</tr>
</tbody>
</table>

_Osaka University Knowledge Archive : OUKA_

https://ir.library.osaka-u.ac.jp/  
Osaka University
Modulated photoconductivity study of electron drift mobility in amorphous silicon

K. Hattori, a) M. Iida, T. Hirao, and H. Okamoto
Department of Physical Science, Graduate School of Engineering Science, Osaka University, Toyonaka, Osaka 560-8531, Japan

(Received 2 August 1999; accepted for publication 14 December 1999)

The modulated photoconductivity technique, a convenient means of measuring the drift mobility of photocarriers, has been applied to investigate carrier transport in hydrogenated amorphous silicon. The frequency resolved spectra of drift mobility that can be obtained from the measurements were analyzed in accordance with a generalized transport model that included possible carrier interactions between localized states through tunneling transitions. Theory suggests that a tunneling-assisted thermalization of nonequilibrium carriers takes part in the transport process to an appreciable degree. The developed model accounts for the experimental results obtained for hydrogenated amorphous silicon (a-Si:H), yielding quantitative assessments of the transport properties of this material.

I. INTRODUCTION

A fundamental property of amorphous semiconductors is the presence of localized states. The interactions of excess carriers with localized states have a significant influence on the transport process as clearly manifested in transient photocurrent measurements with pulsed excitation, such as a time-of-flight (TOF) measurement in a sandwich configuration. The investigation of photocarrier transport has greatly contributed to the understanding of these materials. In the TOF experiment, a sheet of carriers is created near one surface by a brief flash of strongly absorbed light. A voltage applied across the sample causes the carriers to drift to the opposite surface. The propagation of carriers is monitored by the current induced in an external circuit. The TOF transport in amorphous semiconductors is frequently described by introducing the concept of drift mobility that is defined as an effective mobility averaged over all the carriers involved in transport. The drift mobility of experimental concern is that of carriers in a highly nonequilibrium distribution that relaxes as the carriers traverse the sample, and is in essence time dependent. The present prevailing theory for the transient drift mobility phenomena is the multiple trapping model, which considers that carriers move by repeatedly transitioning between extended and localized states, becoming trapped in localized states then releasing from localized states to extended states.

In this study, a frequency resolved technique based on modulated photoconductivity (MPC) in a coplanar geometry has been applied to investigate the drift mobility of photocarriers and their interactions with localized states. A detailed discussion is given for interpreting the frequency domain measurements of drift mobility in accord with a generalized transport model. The model takes into account possible carrier interactions between localized states through tunneling transitions in the context of a mean field approximation. The theoretical consideration suggests that a tunneling-assisted thermalization of nonequilibrium carriers takes part in the transport process to an appreciable degree. The developed model accounts for the experimental results obtained for hydrogenated amorphous silicon (a-Si:H), yielding quantitative assessments of the transport properties of this material.

II. THEORY AND ANALYSIS

A. Phenomenological formulation

We here consider an amorphous semiconductor layer in a coplanar configuration uniformly illuminated by a weakly absorbed band-gap light. The extended band states and the localized gap states are both populated with photogenerated excess carriers. The charge neutrality requirement imposes

\[ N = n + \sum_i n_i = p + \sum_k p_k, \]  

where \( N \) is the total concentration of charge carriers, \( n \) and \( p \) refer to the concentrations of electrons in the conduction band states and holes in the valence band states, respectively, \( n_i \) the concentration of electrons trapped at the localized states of energy \( \varepsilon_i \), and \( p_k \) the concentration of holes trapped at the localized states of energy \( \varepsilon_k \). With electron and hole currents being spatially uniform, the continuity equation is simply expressed by

\[ \frac{d}{dt} N = G - R, \]  

where \( G \) denotes the generation rate and \( R \) the recombination rate. For an excitation light sinusoidally varying in time such that

\[ G = G_0 + \Delta G \cos(\omega t), \]  

a first-order solution for carrier concentration is given by

\[ N = N_0 + \text{Re}[\Delta N \exp(i\omega t)], \]  

where \( i^2 = -1 \), \( N_0 = n_0 + \sum_i n_{i0} = p_0 + \sum_k p_{k0} \) is the steady-state concentration generated by \( G_0 \), and \( \Delta N = \Delta n + \sum_i \Delta n_i \).

a) Electronic mail: hattori@ee.es.osaka-u.ac.jp
\[ \Delta \sigma = q \Delta G \tilde{\mu} \bar{\tau}, \]  

(12)

in the low frequency regime where \( \omega|\bar{\tau}| \ll 1 \). Expected in this extreme limit is that the carrier system stays in quasithermal equilibrium during modulation and thereby the transport parameters \( \tilde{\mu} \) and \( \bar{\tau} \) become frequency independent. In Appendix A, the plausibility of MPC behavior suggested above is demonstrated by model calculations.

**B. Rate equations**

In this section, we will deal with drift mobility for the case in which electrons are the predominant type of carriers in photoconduction, so as to accommodate photocarrier transport in \( a \)-Si:H. This considerably reduces complications in the theoretical analysis and thereby makes the discussion more straightforward. It is also assumed that contributions due to hopping transport in the general formula (8) are minor. A justification of this neglect is given by means of numerical calculation in Appendix B. The drift mobility is then simply rewritten as

\[ \bar{\mu} = \frac{\Delta n}{\Delta N}. \]  

(13)

Even in such a simple case, contributions by tunneling processes cannot be completely excluded from consideration. There is a possibility that tunneling interactions between localized states may affect nonequilibrium occupation, on which the population ratio \( \Delta n/\Delta N \) and the drift mobility \( \bar{\mu} \) depend. We will address this point in the following.

The starting point for the analysis is the set of rate equations for a distribution of localized states with densities \( N_i \) and energies \( \varepsilon_i \).

\[ \frac{dn_i}{dt} = G - \sum_j \left[ nC(N_j - n_i) - e_i n_i \right] - \frac{n - n_i^{eq}}{\tau_i}. \]  

(14)

\[ \frac{dn}{dt} = nC(N_i - n_i) - e_i n_i - n_i \sum_j w_{ij} + \sum_{j=1}^{n_i} n_j w_{ji} - \frac{n_i - n_i^{eq}}{\tau_i}. \]  

(15)

All the localized states considered here have an identical efficiency of capturing a band electron, which is described by the coefficient \( C \). The thermal emission of electrons from the localized states of energy \( \varepsilon_i \) to the conduction band states above \( \varepsilon_i \) occurs at the rate \( e_i \) given by

\[ e_i = N_c C \exp \left[ - \frac{\varepsilon_i - \varepsilon}{kT} \right]. \]  

(16)

where \( kT \) is the thermal energy and \( N_c \) is the effective density of conduction band states. Equations (14) and (15) are written with monomolecular recombination terms containing lifetime parameters \( \tau \) and \( \tau_i \). They constitute the rate of charge recombination represented by

\[ R = \frac{n - n_i^{eq}}{\tau} + \sum_i n_i n_i^{eq} \frac{1}{\tau_i}. \]  

(17)
where the superscript eq refers to the value in thermal equilibrium. Considering a particular mechanism for recombination is not essential to the analysis of high frequency MPC or the drift mobility determined from it, but is necessitated for quantitative arguments on the low-frequency MPC and the steady-state photoconductivity. The tunneling rate of an electron from the state \(i\) to the state \(j\), separated by a distance \(r = |\mathbf{r}_j - \mathbf{r}_i|\) and an energy \(\epsilon_{ij} = \epsilon_j - \epsilon_i\), is expressed by\(^5\)

\[
w_{ij} = v \exp \left[ -\frac{2r}{\alpha} - \frac{\theta(\epsilon_{ij})\epsilon_{ij}}{kT} \right].
\]

where \(v\) is the frequency prefactor, \(\alpha\) the localization radius, and \(\theta(\epsilon)\) the unit step function. It is easily confirmed that Eqs. (14) and (15) are consistent with the continuity Eq. (2).

In order to make the rate equations given above tractable, we here use the average tunneling rate assessed in the framework of the mean field model that assumes each state is surrounded by the same average environment.\(^7\) The tunneling transitions preferentially take place between the nearest available neighbors. The distribution function of nearest neighbor separations \(r\) from a particular occupied state is given by

\[
P_j(r) = 4\pi r^2 (N_j - n_j) \exp \left[ -\frac{4\pi r^2 (N_j - n_j)}{3} \right],
\]

for a randomly distributed collection of unoccupied states with density \(N_j - n_j\). The configuration average is then

\[
\langle w_{ij} \rangle = \int w_{ij}(r) P_j(r) dr.
\]

An essential requirement for localization is that the localization radius \(\alpha\) is less than the mean distance \((3/4\pi N_j)^{1/3}\) between the states, leading to the approximation

\[
\langle w_{ij} \rangle = C_{ij}(N_j - n_j),
\]

with

\[
C_{ij} = v \pi \alpha^3 \exp \left[ -\frac{\theta(\epsilon_{ij})\epsilon_{ij}}{kT} \right].
\]

In the mean field approach, Eq. (15) is consequently rewritten by

\[
\frac{dn_{ij}}{dt} = nCN_j(N_j - n_j) - \epsilon_{ij} n_i n_j \sum_{j'\neq i} C_{ij'}(N_j - n_j)
\]

\[+ (N_j - n_j) \sum_{j'\neq i} n_j C_{ij'} - \frac{n_i - n_i^{eq}}{\tau_i}.
\]

A strong localization limit where \(\alpha = 0\) and equivalently \(C_{ij} = 0\) deals with the conventional multiple trapping model that ignores any carrier interactions between localized states. It might be worthwhile to mention that the average tunneling rate given above meets the detailed balance requirement in thermal equilibrium such that

\[f_i^{eq} C_{ij}(1 - f_j^{eq}) = f_j^{eq} C_{ji}(1 - f_i^{eq}).\]

where \(f_i^{eq} = \{1 + \exp[(\epsilon_i - \epsilon_F)/kT]\}^{-1}\) is the Fermi–Dirac distribution with Fermi level \(\epsilon_F\).

A linearization of Eqs. (14) and (23) for the modulated illumination Eq. (3) is easily achieved by collecting the first order terms in \(\Delta n\), \(\Delta n_i\), and \(\Delta G\) and replacing the derivative by \(i\omega\). The steady-state solutions \(n_0\) and \(n_i\) to be contained in the linearized equations should be considered carefully. Neglecting the recombination term \((n_i - n_i^{eq})/\tau_i\), the steady-state occupancy \(f_{i0} = n_0/n_i\) is given by

\[
f_{i0} = \frac{n_0 C}{n_0 C + \epsilon_i}.
\]

The occupation function \(f_{i0}\) is equivalent to the distribution \(f_i^{eq}\) with the Fermi level \(\epsilon_i\) replaced by the quasi-Fermi level \(\epsilon_i - kT \ln(n_i/n_0)\). The following equality:

\[
f_{i0} C_{ij}(1 - f_{j0}) = f_{j0} C_{ji}(1 - f_{i0}),
\]

then stands for tunneling transitions. This ensures that every tunneling term involved in the steady-state equation is canceled out and does not appear in the expression for \(f_{i0}\). For localized states lying in the vicinity of the band edge, like the conduction band tail in \(a\)-Si:H, we may expect that \(n_0 C \ll \epsilon_i\) and thereby \(f_{i0} \ll 1\) under a moderate excitation. It should be noted that the assumption of the empty states is valid even if the recombination events described by \(\tau_i\), which tend to reduce \(f_{i0}\), are taken into consideration.

On the basis of these arguments, we finally reach the equations that represent the high frequency MPC

\[
\Delta n \left( i\omega + \sum_i C N_i \right) - \sum_i \Delta n_i \epsilon_i = \Delta G,
\]

\[
\Delta n C N_i - \Delta n_i \left( i\omega + \epsilon_i + \sum_{j\neq i} C_{ij} N_j \right) + \sum_j \Delta n_j C_{ji} N_j = 0.
\]

The solutions for Eqs. (27) and (28), as well as the drift mobility determined from them, will be investigated in a later section.

C. Model calculation

We here introduce the quantities defined as

\[
\hat{N}_i = \frac{N_i}{N_c},
\]

\[
\hat{\Delta f}_i = \frac{N_i \Delta n_i}{N_c \Delta n}.
\]

The normalized occupancy \(\hat{\Delta f}_i\) is the ratio of occupancies \(\Delta n_i/N_i\) and \(\Delta n/N_c\) in the framework of the present rate equation analysis, where the distribution of extended states is equivalent to a single effective level with density \(N_c\) and energy \(\epsilon_c\). The drift mobility is formulated with these definitions as

\[
\tilde{\mu}_c = \frac{1}{1 + \hat{N}_i \hat{\Delta f}_i}.
\]

In this expression, a direct connection between the drift mobility and the normalized occupancy is evident.

It is instructive to outline the analytic properties of the multiple trapping model assuming \(\alpha = 0\) before proceeding to
more general cases. A simple analytical solution for the normalized occupancy is easily achieved in the strong localization limit to be

$$\Delta f_i = \frac{N_c C}{i \omega + e_i}.$$  (32)

Readily understood is that a specific energy level given by

$$\epsilon_{th} = \epsilon_e - kT \ln \left( \frac{N_c C}{\omega} \right),$$  (33)

plays an important role. 8–11 Two energy regions separated by the thermalization energy $\epsilon_{th}$ are defined in conjunction with given frequency and temperature. In the shallower energy region where $\epsilon_e > \epsilon_{th}$, the normalized occupancy obeys a Boltzmann distribution

$$\Delta f_i = \exp \left( \frac{\epsilon_e - \epsilon_i}{kT} \right),$$  (34)

indicating that a quasithermal equilibrium is established partially between electrons in the extended states and the associated localized states. On the other hand, for the deep localized states with energies $\epsilon_e < \epsilon_{th}$, the nonequilibrium occupation represented by

$$\Delta f_i = \frac{N_c C}{i \omega},$$  (35)

occurs. A deeper thermalization energy appears for a lower frequency at a fixed temperature. The frequency-domain thermalization event corresponds to the progressively deeper trapping of carriers that causes dispersive transport observed in the time domain. The thermalization process in the presence of tunneling transitions between localized states will be examined in the following part of this section by means of numerical calculation.

The calculations are based on the density of states (DOS), which has been introduced to describe the conduction band tail, 12,13

$$D(\epsilon) = \begin{cases} D_c \left( 1 - \frac{\epsilon_e - \epsilon}{\epsilon_0} \right), & \epsilon > \epsilon_e - \epsilon_0 + kT_c, \\ D_c kT_c \frac{\epsilon_0}{\epsilon_0} \exp \left[ - \left( 1 + \frac{\epsilon_e - \epsilon - \epsilon_0}{kT_c} \right) \right], & \epsilon < \epsilon_e - \epsilon_0 + kT_c. \end{cases}$$  (36)

This distribution is composed of a linearly decreasing part from the conduction band edge $\epsilon_e$, followed by an exponentially decreasing part into the gap. A linear distribution extended above $\epsilon_e$ gives the effective density of states $N_c = D_c kT_c (1 + kT_c / \epsilon_0)$. In the calculation, the continuous DOS was replaced by a set of discrete levels with a spacing $\delta$, normally set at 10 meV, for which the simultaneous linear Eqs. (27) and (28) are solved numerically. It has been confirmed that the calculated result is not altered by using $\delta$ less than 10 meV. Parameters used in the calculations are $D_c = 2 \times 10^{21}$ cm$^{-3}$ eV$^{-1}$, $\epsilon_0 = 100$ meV, $C = 10^{-8}$ cm$^3$ s$^{-1}$, and $\alpha = 10$ Å. The value of localization radius is compatible with the previous estimates. 6,14 The same frequency prefactor $\nu$ is $N_c C$ for tunneling transitions and thermal emissions was assumed for simplicity, which would be reasonable so far as nonradiative tunneling transitions 6 are concerned.

Figure 1 displays the absolute values of normalized occupancy $|\Delta f_i|$ calculated as a function of energy for various frequencies. The occupation function for $\alpha = 0$, plotted by dotted line as a reference, exhibits a sharp step at the thermalization energy, as interpreted previously on the basis of the analytical consideration. In the shallow energy region, the function behaves as an exponential, whereas uniform occupancy appears in the deep energy region. The thermalization energy shifts downward in the gap with decreasing frequency. Simultaneously, the deep nonequilibrium part becomes more prominent. Similar qualitative features can be found for the results obtained by assuming $\alpha = 10$ Å, shown by solid lines. It can be seen in the figure that tunneling interactions between localized states bring about a deep thermalization energy as well as an increased deep nonequilibrium occupancy. In this case, the energy at which the total escape rate described by $e_i + \sum_j C_{ij} N_j$ coincides with the frequency $\omega$ is a good approximation to the thermalization energy that divides the exponential occupancy from the uniform occupancy. Figure 2 shows the normalized occupation functions calculated for various temperatures. As temperature decreases, the thermalization energy moves upward. The intensity of deep nonequilibrium occupancy varies slightly with temperature for $\alpha = 0$, due to the attempt-to-escape frequency $N_c C$ being weakly dependent on temperature. In the presence of tunneling interactions, on the other hand, a strong temperature dependence emerges. The probability of tunneling transitions depends on the density of accessible states, as explicitly indicated by Eq. (21), so that the thermalization process is markedly influenced by the DOS distribution. This is in sharp contrast to the strong localization limit present without such a correlation. It is logical to expect that the thermalization of trapped electrons is accelerated for a higher DOS. This is confirmed by the calculations with varying the slope of exponential band tail.

Figure 3 illustrates the frequency resolved spectra of drift mobility amplitude $|\hat{\mu}|$ computed for various tempera-
FIG. 3. Frequency dependence of normalized drift mobility $u$ for various temperatures $T = 180, 220, 260, 300, 340$, and 380 K at a frequency $\omega/2\pi = 10^4$ Hz. Dashed and solid lines represent the results computed for $\alpha=0$ and 10 Å, respectively. In the calculation, $T_c = 260$ K is assumed.

III. EXPERIMENTAL DETAILS

A 6-μm-thick sample of intrinsic $a$-Si:H deposited by glow discharge on a glass substrate at a substrate temperature of 200 °C was used in the present study. The contacts were coplanar Al electrodes with a gap of 1 mm deposited on top of the sample. In the MPC experiments, the sample was mounted in a temperature-controlled cryostat. The measurement temperature was varied between 160 and 380 K. The sample was uniformly illuminated by a 679 nm light from a diode laser. The light intensity was modulated sinusoidally at a frequency $\omega=2\pi f$ with $f$ varying between 10 Hz and 40 MHz. The highest frequency corresponds to a time scale of 4 ns, which is comparable to the shortest time resolvable in transient photocurrent experiments. The electric field applied between the electrodes was typically $E = 10$ kV/cm. At a frequency higher than $f = 10$ kHz, the amplitude of MPC $|\Delta\sigma|$ was detected by a rf spectrum analyzer and a wideband preamplifier. A standard lockin amplifier was also employed for low frequency measurements. The magnitude of drift mobility was determined by using the relation

$$|\bar{\mu}| = \frac{\omega |\Delta\sigma|}{q\Delta G}.$$ 

Prior to the drift mobility measurement, a linear response assumed in the theoretical analysis of MPC has been tested experimentally by varying the modulation amplitude $\Delta G$ while keeping the steady-state background intensity $G_0$ constant. The experiment actually showed excellent linearity over the modulation depths $\Delta G/G_0$ ranging from 1% to 100%. All the data to be presented in this article were acquired in the linear response regime. Effects of the electric field applied between electrodes and the steady-state light intensity have also been carefully examined. It was found experimentally that an increase in high frequency MPC occurs to an extent that depends on power dissipation $\sigma_0 E^2$ because of a thermally activated drift mobility. Consequently, the MPC-derived drift mobility decays appreciably following the light induced degradation of the steady-state photoconductivity. The apparent instability under light soaking can be eliminated by monitoring MPC with a sufficiently weak field and illumination. It has been confirmed from such measurements that light induced degradation of drift mobility is less than 10% after prolonged light exposure (679 nm, 18 mW/cm², 7 h). Further details of the light-soaking experiments will be given in a separate article. In the following section, the results obtained for the light-soaked sample with a negligible heating effect throughout a series of measurements are presented and discussed.

IV. RESULTS AND DISCUSSION

Figure 4 displays the frequency dependence of MPC amplitude measured at various temperatures. These plots show a plateau in the lower frequency region, while in the higher frequency region they go downward with frequency. The low frequency behavior is indicative of the constant mobility-lifetime product that is expected for a quasiequilibrated transport system. On the other hand, the high frequency MPC is considered to be drift mobility controlled. Figure 5 illustrates the drift mobility spectra derived from the MPC data, which consist of two branches separated by a knee. Note that the translation into drift mobility can be validated...
only for the high frequency branch. The low frequency branch, showing a linear increase with frequency, merely represents $\bar{\mu}\bar{T}$ multiplied by frequency.

A direct way to investigate transport processes involved is to quantitatively compare the experimental data with the theoretical results. To begin with, the traditional multiple trapping model that ignores carrier interactions between localized states is examined. The temperature dependence of drift mobility measured at $f=10$ MHz is plotted in Fig. 6, together with the theoretical plots based on the DOS distributions given by Eq. (36) with various characteristic temperatures $T_c$. The experimental data exhibit a relatively steep decrease for lower temperatures, which significantly depart from the model calculations. Other probable types of DOS including a single exponential distribution, have also been considered for this assessment. These alternatives fail to reproduce the drift mobility behavior experimentally observed. In contrast, the transport model that takes tunneling interactions into consideration successfully accounts for the drift mobility data. The result of calculation using the DOS distribution given by Eq. (36) is assumed in the calculation. The extended-state mobility evaluated here does not contradict the previous estimate, $\mu_c=10–15$ cm$^2$/V s, whereas the characteristic temperature $T_c=220$ K is low as compared with those implied from the TOF experiments, $T_c=250–300$ K. It should be noticed, however, that the previous evaluation relies on the multiple trapping model constructed with the simplification that $\alpha=0$. This predicts a pretransit TOF current that shows a power-law time dependence $t^\beta$, with a temperature dependent slope $\beta=-(1-T/T_c)$ for $T<T_c$. The temperature dependence of the slope $\beta$ observed in low-field TOF experiments is summarized in Fig. 8. It is found in the figure that the theoretical prediction is valid only in a medium temperature range around 200 K, leading to $T_c=260$ K. The sizable effect of tunneling interactions demonstrated by the present measurements tempts us to reexamine the time-domain results. In Appendix C, TOF solutions in the pretransit time regime are obtained quantitatively, in association with the transient drift mobility concept. The simulated result with characteristic temperature $T_c=230$ K gives the best fit to the experimental data, respectively. Good agreement is also confirmed for the drift mobility spectra shown in Fig. 5 where the theoretical plots are drawn by solid lines.
where the energy scale is given by the thermalization energy of the above formulas. To examine this, a numerical simulation allowing tunneling interactions to take a part in the MPC process, throwing doubt on the DOS reconstructed by means of Eq. (36) with \( T_c = 230 \text{ K} \) is assumed in the calculation.

Again, the problem lies in a finite localization radius that shows that the disagreement is greatly emphasized for an insufficient accuracy in the DOS deduced from MPC.

V. SUMMARY

Frequency-domain measurements of drift mobility of photocarriers by means of MPC technique have been applied to explore transport process in \( a\)-Si:H. Theoretically, MPC transport is controlled by trapping and release from isolated localized states, the spectroscopic method is devised with a general model that considers possible tunneling interactions between localized states in a mean field approach. Prime effects of incorporating tunneling transitions are viewed from the theoretical analysis as an accelerated thermalization of nonequilibrium carriers as well as a reduced magnitude of drift mobility. Using a finite localization length \( \alpha=10 \text{ Å} \), the theory accounts well for MPC experiments performed for \( a\)-Si:H over a wide range of frequency and temperature. The suggested incomplete localization is consistent with transient drift mobility data obtained from TOF experiments. The model consideration also reveals that the MPC methodology devised on the basis of isolated localized states yields an incorrectly mapped DOS distribution.

APPENDIX A: RECOMBINATION

Our theory for drift mobility measurements assumes a particular frequency that characterizes MPC behavior. The assumed changeover in frequency domain is here elucidated by inclusion of the monomolecular recombination mechanism. This is formally achieved by appending onto Eqs. (27) and (28) additional terms \( \Delta n/\tau \) and \( \Delta n_j/\tau_j \), respectively. For simplicity, we consider a tunneling recombination consisting of downward tunneling transitions of band tail electrons to holes deeply trapped in the gap, to which an energy-independent \( \tau_j \) would be adapted reasonably. The results of calculation incorporating the recombination processes described above are illustrated in Fig. 10. The simulated spectra show two branches separated by a knee. It is readily found that in the high frequency branch, the spectrum is not affected by the recombination. We have confirmed that varying lifetime parameters shifts the frequency at which the knee appears while the high frequency branch stays unchanged. These observations lend credence to the present interpretation of MPC-derived drift mobility.

APPENDIX B: HOPPING MOBILITY

The mean transition rate of electrons from an occupied level \( i \) to an unoccupied level \( j \) with density \( N_j(\ll n_j) \) is written by

\[
\langle w_{ij} \rangle = C_{ij} N_j.
\]
Therefore, the contribution to the drift mobility in MPC transport is out to be electrons situated at a level $i$. Applying the Einstein relationship, we have the mobility of $\bar{\mu}_i$ given above can be assessed from the configuration, for instance, a $p$-$i$-$n$ diode. The continuity equation is expressed by

\begin{equation}
\mu_{ci} = \frac{q \alpha^2}{2kT} C_{im} N_m. \quad (B3)
\end{equation}

The hopping mobility given above can be assessed from the numerical solution of the rate Eqs. (27) and (28). The results of calculation for $\alpha = 10 \text{Å}$ and $T_c = 220 \text{K}$ are shown in Fig. 11. The computed hopping mobility, which is smaller by orders of magnitude than the measured mobility plotted in Fig. 5, supports the validity of the present analysis which neglects hopping transport.

\section*{APPENDIX C: TRANSIENT DRIFT MOBILITY}

Here, we shall consider electron transport in a TOF configuration, for instance, a $p$-$i$-$n$ diode. The continuity equation is expressed by

\begin{equation}
\frac{\partial}{\partial t} \tilde{N}(t) = 0, \quad (C2)
\end{equation}

can be directly derived from Eq. (C1), where $\tilde{N}$ denotes the spatial average defined by the integration from $x=0$ to $x=d$. The pretransit TOF current $J(t)$ observed under a uniform electric field is therefore related to the transient drift mobility as

\begin{equation}
\bar{\mu}(t) = \frac{\mu_c \tilde{n}(t)}{N(0)} = \frac{J(t)d}{Q E}, \quad (C3)
\end{equation}

where $Q = q \tilde{N}(0)d$ refers to the injected charge. The expression coincides with that deduced previously. In the small-signal TOF experiment, the trap saturation can be avoided so that the concentrations of electrons in the extended states $\tilde{n}$ and in the localized states $\tilde{n}_i$ obey the linearized rate equations

\begin{equation}
\frac{d\tilde{n}_i}{dt} = -\sum_j (\tilde{n} C_{ij} - \epsilon_i \tilde{n}_i), \quad (C4)
\end{equation}

\begin{equation}
\frac{d\tilde{n}}{dt} = \tilde{n} C_{ij} - \epsilon_i \tilde{n}_i = \sum_j \tilde{n}_i C_{ij} N_j + N_i \sum_j \tilde{n}_j C_{ji}. \quad (C5)
\end{equation}

We have to keep in mind that the discussion ignores possible contributions of hopping transport. A time-dependent hopping mobility can be defined as

\begin{equation}
\bar{\mu}_{hop}(t) \approx \frac{\sum_i \mu_{ci} \tilde{n}_i(t)}{\tilde{N}(0)}. \quad (C6)
\end{equation}

Our preliminary calculation has revealed the trivial role played by hopping mobility in determining the transient photocurrents, at least for temperatures above 100 K. However, it is known experimentally that even at a temperature around 200 K, the transient photocurrent measured for $a$-$Si:H$ is significantly modified when an electric field exceeding...
$10^5$ V/cm is applied, due to a field-enhanced band-tail hopping. The present model does not include the field-related effect and concerns the low-field transient drift mobility.

Figure 12 shows the transient drift mobility $\bar{\mu}(t)$ obtained from numerically solving the differential Eqs. (C4) and (C5) for the DOS given by Eq. (36). The decay of transient drift mobility follows approximately a power law time dependence like $t^{-\beta}(\beta<0)$ for long times. Note that such a long time portion can be usually observed in the experiments. A faster decay in the presence of tunneling interactions is interpreted as being due to a faster thermalization, which is confirmed from the time evolution of occupation function simultaneously computed.