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ABSTRACT

We investigate flow-induced scission of wormlike micelles with dissipative particle dynamics simulations of nonionic surfactant solutions under shear flow. To understand flow-induced scission in terms of micellar timescales, we propose a method to evaluate the longest relaxation time of unentangled surfactant micelles from the rotational relaxation time and the average lifetime at equilibrium. The mean squared displacement of surfactant molecules provides evidence that the longest relaxation time estimated by the proposed method serves as the characteristic timescale at equilibrium. We also demonstrate that the longest relaxation time plays an essential role in flow-induced scission. Using conditional statistics based on the aggregation number of micelles, we examine the statistical properties of the lifetime of wormlike micelles. We then conclude that flow-induced scission occurs when the Weissenberg number defined as the product of the longest relaxation time and the shear rate is larger than a threshold value.

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I. INTRODUCTION

Surfactants consist of hydrophilic and hydrophobic moieties. Above a critical concentration, surfactants spontaneously assemble into aggregates such as spherical micelles, rodlike micelles, and wormlike micelles in aqueous solutions. Since these micelles exhibit unique properties, they can serve as additives in working fluids for various applications, including rheology control,² turbulent drag reduction,³ and drug delivery systems.⁴ Therefore, it is crucial to understand the structures and dynamics of micelles in flowing solutions for industrial applications of surfactants.

Flow-induced scission of surfactant micelles is among the crucial phenomena. Although thermal fluctuations induce scission of micelles at equilibrium, flow with high velocity gradients promotes their scission. 5-7 This phenomenon may be intuitively obvious, but it is difficult to quantitatively predict the conditions and degree of flow-induced scission, which are required for practical use of surfactants. An increase in scission frequency brings about a drastic change in micellar structures and distributions, leading to a significant modification of the flow properties of surfactant solutions. In addition, since the constitutive equations for surfactant solutions need to include the effect of scission and recombination kinetics explicitly, 11-13 insight into flow-induced micellar scission leads

to an understanding of the rheology and turbulent drag reduction phenomenon of surfactant solutions. In other words, to reveal the macroscopic flow behavior of surfactant solutions, we need to understand the properties of flow-induced micellar scission. In the present study, we focus on a uniform shear flow, which is often used in rheological measurements, and investigate flow-induced scission of wormlike surfactant micelles in detail.

Although some experimental studies succeeded in evaluating the average lifetime of micelles, 14-16 it is difficult to experimentally observe the structures and dynamics of individual micelles in flowing solutions. Molecular simulations allow us to overcome this difficulty with measurements. When we are interested in the slow dynamics of micelles rather than the fast dynamics at the atomic level, coarse-graining, in which several atoms or molecules are considered as a single particle, is often used to reduce the computational cost associated with all-atom molecular dynamics simulations. The coarse-grained molecular dynamics (CGMD) method using the MARTINI force field is one of the most popular approaches based on coarse-graining. With CGMD, we can simulate micellar scission to evaluate relevant micellar properties directly. 17,18 Regarding flowinduced scission, Sambasivam et al. 19 conducted CGMD simulations of a single rodlike micelle under shear flow and found that elongation of micelles by a shear flow increased the potential energy, thus leading to the scission of micelles. Although CGMD simulations have revealed the detailed dynamics of micellar scission, many studies simulated a single micelle or a few micelles only. 17-19 Therefore, the statistical properties of flow-induced scission and its effect on the micellar distribution remain unclear.

Another coarse-graining approach relies on the introduction of a kinetic model for scission and recombination, and several models^{20–22} have been proposed. These models significantly reduce the computational cost and allow systematic investigation of the statistical properties of scission and recombination. Kröger and Makhloufi²⁰ proposed the FENE-C model, which introduces scission and recombination into a finitely extensible nonlinear elastic (FENE) potential. They reported the shear-rate dependence of the average micellar length and lifetime under shear flow. Padding et al.²² modeled a wormlike micelle as a string of thin rods and found that the average breaking rate varied depending on the scission energy and shear rate \(\bar{y}\). However, there is still room for consideration of these results concerning flow-induced scission because scission and recombination were explicitly modeled in these previous studies. Moreover, the explanation of the shear-rate dependence of flow-induced scission was unsatisfactory because relevant timescales of individual micelles were not considered.

It is well known that the relaxation time of micelles, which repeatedly break and recombine, is sometimes affected by scission. Regarding entangled micelles, Cates²³ proposed a theory that predicts the relaxation time from the average lifetime and reptation time of micelles. On the other hand, for unentangled micelles, Faivre and Gardissat²⁴ proposed a theory that incorporated the process of scission and recombination into the Rouse model, although they aimed at describing the viscoelasticity of amorphous selenium. Huang et al.²⁵ numerically confirmed the validity of this theory. According to the concept proposed by Faivre and Gardissat, Huang et al. defined the relaxation time τ_{Λ} of micelles, which corresponds to the relaxation time of a segment of size Λ for which the lifetime is equal to the Rouse relaxation time. They found that chain deformation, orientation, and rheological properties under shear flow are expressed by universal functions of the dimensionless number $\beta_{\Lambda} = \tau_{\Lambda} \dot{\gamma}$. However, their simulations used a mesoscopic model incorporating a kinetic model for scission and recombination into linear chains. To our knowledge, no study has examined whether τ_{Λ} also plays a crucial role in unentangled micelles composed of surfactant molecules. Since surfactant micelles have complicated internal structures compared with polymer-like linear chains, they exhibit complex dynamics of scission and recombination. Therefore, the applicability of τ_{Λ} to surfactant micelles is not obvious and is

In the present study, we intend to quantitatively reveal the shear-rate dependence of micellar scission and identify the timescales relevant to flow-induced scission. For this purpose, we conduct molecular simulations of nonionic surfactant solutions using the dissipative particle dynamics (DPD) method. DPD was proposed by Hoogerbrugge and Koelman²⁶ and then improved by Español and Warren.²⁷ Many researchers^{28–34} have extensively investigated surfactant solutions using the DPD method. Since particles interact via soft repulsive interactions in DPD, we can make time steps larger than CGMD, which allows us to simulate large systems for long timescales with a low computational cost. Therefore, we can evaluate the statistical properties of flow-induced scission and its effect on the micellar distribution. Since previous studies^{20,22,25} have analyzed the average properties over all the micelles in the system, their results could demonstrate only the combined effect of the changes in micellar properties and distributions. We overcome this problem using conditional statistics based on the aggregation number of micelles, which offer deeper insight into the shear flow effect on individual micelles. In addition, we introduce the longest relaxation time of unentangled micelles to demonstrate that a single dimensionless number can characterize flow-induced scission. More concretely, we extend the theory of Faivre and Gardissat²⁴ to unentangled surfactant micelles. We then prove the importance of this timescale in micellar scission under shear flow using the simulation results for various temperatures.

II. SIMULATION METHOD

A. DPD governing equations

In DPD simulations, we regard a group of atoms and molecules as a single DPD particle. The motion of a DPD particle obeys

$$m_i \frac{\mathrm{d} v_i}{\mathrm{d} t} = \sum_{j(\neq i)} F_{ij}^C + \sum_{j(\neq i)} F_{ij}^D + \sum_{j(\neq i)} F_{ij}^R, \tag{1}$$

where m_i and v_i are the mass and velocity of the *i*th particle, respectively, and F_{ij}^C, F_{ij}^D , and F_{ij}^R are the conservative, dissipative, and random forces exerted on the ith particle by the ith particle, respectively. The conservative force acts as a repulsive force in the form of

$$\mathbf{F}_{ij}^{C} = \begin{cases} a_{ij} \left(1 - \frac{r_{ij}}{r_c} \right) \mathbf{e}_{ij} & \text{for } r_{ij} \leq r_c, \\ 0 & \text{for } r_{ij} > r_c, \end{cases}$$
 (2)

where a_{ij} is the conservative force coefficient between the ith and jth particles, r_c is the cutoff distance, $r_{ij} = r_i - r_j$, $r_{ij} = |r_{ij}|$, and $e_{ij} = r_{ij}/r_{ij}$ with r_i being the position of the *i*th particle. The dissipative and random forces are expressed as

$$F_{ij}^{D} = -\gamma w^{D}(r_{ij})(\boldsymbol{e}_{ij} \cdot \boldsymbol{v}_{ij})\boldsymbol{e}_{ij} \quad (\boldsymbol{v}_{ij} = \boldsymbol{v}_{i} - \boldsymbol{v}_{j})$$
(3)

and

$$\boldsymbol{F}_{ij}^{R} = \sigma w^{R}(r_{ij})\theta_{ij}\boldsymbol{e}_{ij}, \qquad (4)$$

where γ and σ are the dissipative and random force coefficients, respectively, and $w^D(r_{ij})$ and $w^R(r_{ij})$ are the weight functions of the dissipative and random forces, respectively. In Eq. (4), θ_{ij} is a random variable that satisfies

$$(\theta_{ij}(t) = \theta_{ji}(t), \tag{5}$$

$$\left\langle \left\langle \theta_{ij}(t)\right\rangle =0,\right. \tag{6}$$

$$\begin{cases} \langle \theta_{ij}(t) \rangle = 0, \\ \langle \theta_{ij}(t)\theta_{kl}(t') \rangle = (\delta_{ik}\delta_{jl} + \delta_{il}\delta_{jk})\delta(t - t'), \end{cases}$$
 (6)

where δ_{ij} is the Kronecker delta, $\delta(t)$ is the delta function, and $\langle \cdot \rangle$ denotes the ensemble average. The fluctuation dissipation theorem requires that γ , σ , $w^D(r_{ij})$, and $w^R(r_{ij})$ satisfy

$$w^{D}(r_{ij}) = \left[w^{R}(r_{ij})\right]^{2} \tag{8}$$

and

$$\sigma^2 = 2\gamma k_B T,\tag{9}$$

where k_B is the Boltzmann constant and T is the temperature of the system.²⁷ Following Ref. 35, we set the weight function $w^R(r_{ii})$ as

$$w^{R}(r_{ij}) = \begin{cases} 1 - \frac{r_{ij}}{r_c} & \text{for } r_{ij} \leq r_c, \\ 0 & \text{for } r_{ij} > r_c. \end{cases}$$
(10)

In what follows, we use simulation units with $k_BT_0 = m = r_c = 1$, where T_0 is the reference temperature.

B. Surfactant model

The system is composed of water and nonionic surfactants. Since we focus on the general properties of flow-induced scission, we do not assume any specific species of surfactant molecule in the following. As shown in Fig. 1, a surfactant molecule contains a hydrophilic particle and two hydrophobic particles, which are connected by harmonic springs expressed by

$$\boldsymbol{F}_{ij}^{B} = -k_{s}(r_{ij} - r_{eq})\boldsymbol{e}_{ij}, \tag{11}$$

where k_s is the spring constant and r_{eq} is the equilibrium bond distance. We show the simulation parameters in Table I. Here, N is the total number of DPD particles, ρ is the number density of DPD particles, ϕ is the volume fraction of surfactants, and a_{ij} is the conservative force coefficient between different types of particles. The subscripts indicate the types of particles: h, t, and w denote the head, tail, and water particles, respectively. Here, we determine a_{ij} according to Ref. 36 because wormlike micelles are found to be formed for this model above a certain volume fraction. We choose $\phi = 0.05$ for a sufficient number of wormlike micelles to exist in the system. For a specific species of surfactant molecule, a_{ij} can be obtained using a parameterization scheme. $^{35,37-39}$ When we vary $k_B T$, γ changes so that it satisfies Eq. (9) while fixing the value of σ at 3.

TABLE I. DPD simulation parameters. N is the total number of DPD particles, ρ is the number density of DPD particles, σ is the random force coefficient, ϕ is the volume fraction of surfactants, $k_{\rm S}$ is the spring constant, $r_{\rm eq}$ is the equilibrium bond distance, and $a_{\rm ij}$ is the conservative force coefficient between different types of particles. The subscripts indicate the types of particles: h, t, and w denote head, tail, and water particles, respectively.

N	ρ	σ	ϕ	k_s	$r_{\rm eq}$	$a_{\rm hh}$	$a_{\rm ht}$	$a_{\rm hw}$	a_{tt}	a_{tw}	$a_{\rm ww}$
648 000	3	3	0.05	50	0.8	25	60	20	25	60	25

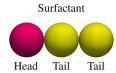




FIG. 1. Schematic of the coarse-grained model of a surfactant and water. The head of the former is a hydrophilic particle, and the tails are hydrophobic particles.

C. Simulation details

To integrate the equations of motion, we use the modified velocity Verlet method, 35

$$r_{i}(t + \Delta t) = r_{i}(t) + \Delta t v_{i}(t) + \frac{1}{2}(\Delta t)^{2} F_{i}(t),$$

$$\widetilde{v}_{i}(t + \Delta t) = v_{i}(t) + \lambda \Delta t F_{i}(t),$$

$$F_{i}(t + \Delta t) = F_{i}(r(t + \Delta t), \widetilde{v}_{i}(t + \Delta t)),$$

$$v_{i}(t + \Delta t) = v_{i}(t) + \frac{1}{2} \Delta t (F_{i}(t) + F_{i}(t + \Delta t)),$$
(12)

where Δt is the time step, F_i is the force exerted on the ith particle, λ is the parameter introduced in this algorithm, and \widetilde{v}_i is the predicted velocity of the ith particle. The random force defined by Eq. (4) is expressed by

$$\boldsymbol{F}_{ij}^{R} = \sigma w_{R}(r_{ij}) \zeta_{ij} \Delta t^{-1/2} \boldsymbol{e}_{ij}$$
(13)

when we calculate Eq. (12). In Eq. (13), ζ_{ij} is a Gaussian random variable with zero mean and unit variance. According to Ref. 35, we choose $\lambda = 0.65$ and $\Delta t = 0.04$. We have confirmed that these parameters realize sufficiently accurate temperature control.

In the present study, we use the Lees–Edwards boundary condition⁴⁰ and the so-called SLLOD equations⁴¹ to generate a uniform shear flow as shown in Fig. 2. The SLLOD equations read

$$\dot{\mathbf{r}}_i = \mathbf{p}_i / m_i + \mathbf{r}_i \cdot \nabla \mathbf{u},
\dot{\mathbf{p}}_i = \mathbf{F}_i - \mathbf{p}_i \cdot \nabla \mathbf{u}, \tag{14}$$

where p_i is the so-called peculiar momentum and u is the fluid stream velocity. In the case of a uniform shear flow, we can express ∇u as

$$\nabla u = \begin{pmatrix} 0 & 0 & 0 \\ \dot{\gamma} & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix}, \tag{15}$$

with $\dot{\gamma}$ being the shear rate. We impose a random initial configuration and conduct equilibrium simulations for 20 000 time units,

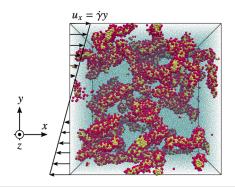


FIG. 2. Visualization of a system composed of surfactants and water. Hydrophilic and hydrophobic particles are indicated in red and yellow, respectively. For clarity, water particles are represented by blue dots.

achieving statistically steady values of the potential energy. After that, we conduct nonequilibrium simulations by imposing shear flow. We perform all the DPD simulations using our in-house code.

We define micelles adopting the method used in previous studies. 37,42 In this method, we judge that two surfactant molecules belong to a common cluster if a hydrophobic particle of one surfactant molecule is within $r_c(=1)$ of a hydrophobic particle of the other. If a cluster has an aggregation number $N_{\rm ag}$ larger than a threshold value $n_{\rm mic}(=10)$, then we regard the cluster as a micelle. Since we focus mainly on micelles with $N_{\rm ag} \gtrsim 50$, our results are practically insensitive to the choice of $n_{\rm mic}$. When we investigate the $N_{\rm ag}$ dependence of micellar properties, we use conditional statistics based on $N_{\rm ag}$. More concretely, to evaluate the micellar properties for a given $N_{\rm ag}$, we use the data for micelles having aggregation numbers that lie in $\left[N_{\rm ag} - \Delta N_{\rm ag}, N_{\rm ag} + \Delta N_{\rm ag}\right]$, where we set $\Delta N_{\rm ag} = 0.05 N_{\rm ag}$.

III. RESULTS AND DISCUSSION

A. Timescales of micelles

One of the main goals of the present study is to elucidate the shear-rate dependence of flow-induced scission. For this purpose, we first identify the relevant timescales of micelles at equilibrium (i.e., in the absence of shear flow). As will be shown below, the rotational relaxation time τ_r and the average lifetime τ_b of micelles are the keys to understanding the dynamics of unentangled wormlike micelles under shear flow. More concretely, τ_r and τ_b determine their longest relaxation time τ .

The target of the present study is the scission of rodlike and wormlike micelles. As shown in Appendix A, micelles are rodlike when $50 \lesssim N_{\rm ag} \lesssim 200$ and wormlike when $N_{\rm ag} \gtrsim 200$. To estimate τ_r of rodlike and wormlike micelles, we evaluate the rotational autocorrelation function,

$$C(t) = \left\langle \mathbf{e}^{(1)}(t_0 + t) \cdot \mathbf{e}^{(1)}(t_0) \right\rangle, \tag{16}$$

where $e^{(1)}$ is the unit eigenvector of the gyration tensor G_{ij} corresponding to the largest eigenvalue. Here, G_{ij} is defined by

$$G_{ij} = \frac{1}{N_{\text{sur}}} \sum_{k=1}^{N_{\text{sur}}} \Delta r_{k,i} \Delta r_{k,j}, \tag{17}$$

where $\Delta r_{k,i}$ is the *i*th component of the relative position vector of the *k*th surfactant particle with respect to the center of mass of the

micelle and $N_{\rm sur}(=3N_{\rm ag})$ is the number of surfactant particles in the micelle. Since $-e^{(1)}$ is also a unit eigenvector of G_{ij} , we determine $e^{(1)}(t)$ so that $e^{(1)}(t-\delta t)\cdot e^{(1)}(t)>0$, where we set $\delta t=100\Delta t$. Then we fit C(t) with an exponential function,

$$C(t) = C_0 \exp(-t/\tau_r), \tag{18}$$

where C_0 is a constant, to determine τ_r . Note that we use conditional statistics based on $N_{\rm ag}$ to obtain C(t) for a given $N_{\rm ag}$. For each micelle, we evaluate $e^{(1)}(t_0+t)\cdot e^{(1)}(t_0)$ until scission, which is defined below, occurs. We show in Fig. 3(a) that C(t) can be expressed well by Eq. (18). Figure 3(b) shows τ_r as a function of $N_{\rm ag}$. The slope of τ_r for $N_{\rm ag} \gtrsim 200$ is smaller than that for $N_{\rm ag} \lesssim 200$. Since as shown in Appendix A, rodlike micelles change into wormlike micelles above $N_{\rm ag} \simeq 200$, micellar structures affect $N_{\rm ag}$ dependence of τ_r . As shown in Fig. 3(a), it is difficult to obtain C(t) for large $N_{\rm ag}$ with enough accuracy to estimate τ_r . As discussed below, large micelles break into small micelles rapidly, thus making it difficult to acquire data for large t. Therefore, C(t) for $N_{ag} = 400$ is shown within a limited range and fluctuates significantly for large t. As a result, the error bars of τ_r for large $N_{\rm ag}$ are larger than those for small N_{ag} . However, in the case of the parameters used in the present study, the accuracy of τ_r for large $N_{\rm ag}$ has little effect on the determination of the longest relaxation time introduced below.

Next, we investigate the characteristic timescale of micellar scission at equilibrium. Micelles repeatedly break and recombine due to the thermal effect. Here, we focus on the time required for micellar scission and evaluate the average lifetime τ_b of micelles at equilibrium. First, we explain how to detect the scission of micelles. We monitor $N_{\rm ag}$ of each micelle at a certain time interval $\delta t (= 100 \Delta t)$, and when a micelle is decomposed into two or more groups, each of which contains more than $n_{\text{mic}}(=10)$ surfactant molecules, we consider that the micelle breaks. Then, we obtain the lifetime t_b of each micelle. By conducting the analysis for different values of $n_{\rm mic}$ in the range $5 \le n_{\rm mic} \le 30$, we have confirmed that the choice of $n_{\rm mic}$ has little effect on the following results. To describe the statistics of t_b , we investigate the survival function $S(t_b)$, which gives the probability that micelles survive beyond a certain time t_b . We estimate $S(t_b)$ using the Kaplan-Meier method.⁴³ Figure 4(a) shows $S(t_b)$ for several N_{ag} . We find that $S(t_b)$ obeys an exponential function, which means that micellar scission events occur with a constant probability per unit time. To obtain τ_b , we fit $S(t_b)$ with $C_0 \exp(-t_b/\tau_b)$ except for short times where $S(t_b)$ does not show

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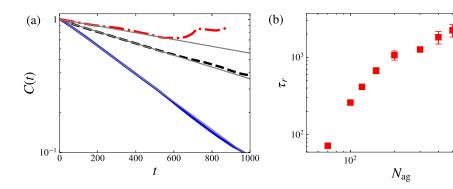
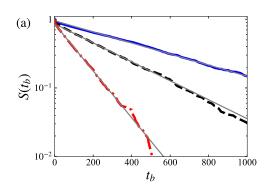


FIG. 3. (a) Rotational autocorrelation function C(t) of micelles for $N_{\rm ag}=120$ (blue solid line), 200 (black dashed line), and 400 (red dotted-dashed line) at equilibrium with $k_BT=1$. Gray lines are exponential fits to the data. (b) Rotational relaxation time τ_r of micelles as a function of $N_{\rm ag}$ with $k_BT=1$. The error bars in (b) denote the standard deviations for three independent simulations.



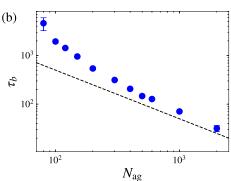


FIG. 4. (a) Survival function $S(t_b)$ of micelles for $N_{\rm ag}=200$ (blue solid line), 300 (black dashed line), and 600 (red dotted-dashed line) at equilibrium with $k_BT=1$. Gray lines are exponential fits to the data. (b) Average lifetime τ_b of micelles as a function of the aggregation number $N_{\rm ag}$ with $k_BT=1$. The black dashed line indicates $\tau_b \propto N_{\rm ag}^{-1}$. The error bars in (b) denote the standard deviations for three independent simulations.

an exponential decay. In Fig. 4(b), we show τ_b as a function of $N_{\rm ag}$. Figure 4(b) shows $\tau_b \propto N_{\rm ag}^{-1}$ for $N_{\rm ag} \gtrsim 300$. This scaling is consistent with the model proposed by Cates, ²³ which assumes that scission of chains occurs with a constant probability per unit time per unit length.

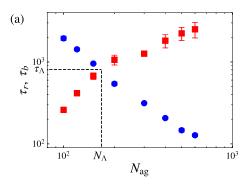
We have seen that τ_r is a monotonically increasing function of $N_{\rm ag}$ [Fig. 3(b)], whereas τ_b is a monotonically decreasing function of $N_{\rm ag}$ [Fig. 4(b)]. In Fig. 5(a), we show τ_r and τ_b as functions of $N_{\rm ag}$ with $k_BT=1$. These two timescales τ_r and τ_b cross each other at a certain aggregation number N_Λ and we define τ_Λ as $\tau_r(N_\Lambda)$. Since $\tau_b(N_{\rm ag}) < \tau_r(N_{\rm ag})$ for $N_{\rm ag} > N_\Lambda$ [Fig. 5(a)], the rotational relaxation of micelles with $N_{\rm ag} \gtrsim N_\Lambda$ proceeds with the aid of scission. Here, note that τ_r corresponds to the rotational relaxation time of micelles without scission kinetics. In order to evaluate their longest relaxation time τ including the effect of scission kinetics, we extend the theory for the Rouse chain with the scission and recombination processes²⁴ to unentangled micelles. In contrast to the original theory, we do not assume that relaxation modes obey the Rouse theory. Instead, we use numerical results of τ_r and τ_b [Fig. 5(a)]. We then expect τ to follow

$$\tau(N_{\rm ag}) = \begin{cases} \tau_r(N_{\rm ag}) & (N_{\rm ag} \lesssim N_{\Lambda}), \\ \tau_{\Lambda} & (N_{\rm ag} \gtrsim N_{\Lambda}). \end{cases}$$
(19)

For $N_{\rm ag} \lesssim N_{\Lambda}$, since τ_b is larger than τ_r , the rotational relaxation of micelles is not affected by their scission, leading to $\tau(N_{\rm ag}) = \tau_r(N_{\rm ag})$. In contrast, for $N_{\rm ag} \gtrsim N_{\Lambda}$, micelles can break into small micelles in a shorter time than $\tau_r(N_{\rm ag})$. As a result, their rotational relaxation proceeds through that of these small micelles

with a shorter relaxation time than $\tau_r(N_{ag})$. Similarly, the generated small micelles are likely to break into even smaller micelles before their rotational relaxation if $\tau_b < \tau_r$. Consequently, micelles such that $\tau_r \simeq \tau_b$ (i.e., $N_{ag} \simeq N_{\Lambda}$) determine the longest relaxation time. Therefore, micelles with $N_{\rm ag} \gtrsim N_{\Lambda}$ relax with a characteristic time of the order of τ_{Λ} for which τ_r is comparable to τ_b [Fig. 5(a)]. This means that the slower relaxation timescales $(\tau_r > \tau_{\Lambda})$ disappear due to the rapid scission of large micelles with $N_{\rm ag} \gtrsim N_{\Lambda}$. In other words, N_{Λ} defines the largest segment that behaves in a similar way to polymer chains (i.e., chains without scission kinetics). This is why micelles with $N_{\rm ag} \gtrsim N_{\Lambda}$ have a common longest relaxation time irrespective of $N_{\rm ag}$. We show τ_{Λ} as a function of $1/k_BT$ in Fig. 5(b) and confirm the Arrhenius dependence. In addition, the inset in Fig. 5(b) shows that N_{Λ} is also a monotonically increasing function of $1/k_BT$. To the best of our knowledge, this is the first evaluation of the longest relaxation time of unentangled surfactant micelles from the rotational relaxation time τ_r and the average lifetime τ_h using molecular simulations.

To confirm the validity of τ_{Λ} obtained by our extended method of Faivre and Gardissat, 24 we first examine the mean squared displacement (MSD) $\langle \Delta r^2 \rangle$ of surfactant molecules. Regarding polymer chains, the MSD of monomers is known to exhibit a subdiffusive regime when $t \lesssim \tau$ and a normal regime when $t \gtrsim \tau$ in DPD simulations, 44 where τ is the longest relaxation time of polymer chains. Huang et al. 21 reported that linear chains with a kinetic model for scission and recombination showed a similar crossover from subdiffusion to normal diffusion around τ_{Λ} obtained with the original method of Faivre and Gardissat. 24 We show the compensated MSD $\langle \Delta r^2 \rangle / t$ of surfactant molecules for various $k_B T$ as a function of t/τ_{Λ}



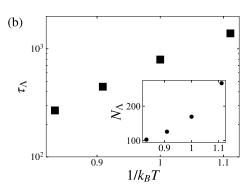


FIG. 5. (a) Rotational relaxation time τ_r (red square) and average lifetime τ_b (blue circle) as functions of the aggregation number $N_{\rm ag}$ with $k_BT=1$. Their intersection defines the longest relaxation time τ_Λ of micelles for $N_{\rm ag} \gtrsim N_\Lambda$. The error bars denote the standard deviations for three independent simulations. (b) Longest relaxation time τ_Λ as a function of $1/k_BT$. The inset shows N_Λ as a function of $1/k_BT$.

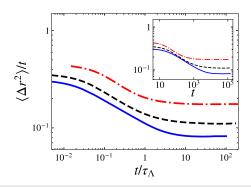


FIG. 6. Compensated MSD $\langle \Delta r^2 \rangle / t$ of surfactant molecules as a function of the normalized time t/τ_{Λ} with $k_BT=0.9$ (blue solid line), $k_BT=1$ (black dashed line), and $k_BT = 1.2$ (red dotted-dashed line). The inset shows $\langle \Delta r^2 \rangle / t$ as a function

in Fig. 6. For $0.1 \lesssim t/\tau_{\Lambda} \lesssim 1$, $\langle \Delta r^2 \rangle / t$ has a negative slope, indicating the subdiffusion of surfactant molecules. In contrast, for $t/\tau_{\Lambda} \gtrsim 10$, $\langle \Delta r^2 \rangle / t$ is flat, indicating the normal diffusion. Thus, we confirm that $\langle \Delta r^2 \rangle$ shows a gradual crossover from subdiffusion to normal diffusion around $t/\tau_{\Lambda} = O(1)$, which is consistent with the property of the MSD in other systems mentioned above. For comparison, we show $\langle \Delta r^2 \rangle / t$ as a function of t in the inset of Fig. 6. It is then more evident that τ_{Λ} serves as an appropriate timescale. However, $\langle \Delta r^2 \rangle$ includes the contribution from all the surfactant molecules, which belong to micelles of different sizes. We need to conduct a more detailed analysis of the MSD to directly prove the relevance of τ_{Λ} , which is beyond the scope of the present study.

To summarize this section, we evaluated the longest relaxation time τ_{Λ} of unentangled surfactant micelles from the rotational relaxation time τ_r and the average lifetime τ_b of micelles at equilibrium by extending the concept proposed by Faivre and Gardissat.²⁴ We confirmed that the longest relaxation time serves as the relevant timescale at equilibrium by investigating the MSD. In Sec. III B, we

focus on micelles with $N_{\rm ag} \gtrsim N_{\Lambda}$ and verify the relevance of τ_{Λ} under shear flow by using conditional statistics based on $N_{\rm ag}$.

B. Flow-induced scission

In this section, we investigate the flow-induced scission of wormlike micelles under shear flow. We demonstrate that flowinduced scission occurs when the Weissenberg number $Wi_{\Lambda} = \tau_{\Lambda}\dot{\gamma}$ is larger than a threshold value.

To reveal the effect of flow-induced scission, we investigate the statistical properties of the micellar lifetime under shear flow. We show in Fig. 7(a) the survival function $S(t_b)$ of micelles for $N_{ag} = 300$ with $k_BT = 1$ for different Wi_{Λ} . For $Wi_{\Lambda} = 4.0$, $S(t_b)$ hardly differs from $S(t_b)$ at equilibrium ($Wi_{\Lambda} = 0$), whereas for $Wi_{\Lambda} = 8.0$ and 16, $S(t_b)$ declines with Wi_{Λ} . This indicates that, in addition to scission through thermal fluctuations, flow-induced scission occurs more significantly as Wi_{Λ} increases. Figure 7(b) shows the $N_{\rm ag}$ dependence of τ_b for the same Wi_{Λ} as in Fig. 7(a). As shown in Fig. 7(a), for Wi_{Λ} = 4.0, the shear flow does not affect τ_b for any $N_{\rm ag}$ considered here. In contrast, for Wi_{Λ} = 8.0 and 16, the shear flow reduces τ_b more significantly as Wi_{Λ} increases. Note that $N_{\rm ag}$ dependence of τ_b remains unchanged under shear flow for all Wi_{Λ} considered here. In other words, the shear flow affects τ_b of micelles such that $N_{\rm ag} \gtrsim N_{\Lambda}$ with a factor independent of $N_{\rm ag}$. Figure 7(b) implies that the threshold value of Wi_{Λ} for the decrease in τ_b is also independent of N_{ag} . Therefore, it is reasonable to conclude that micelles with $N_{\rm ag} \gtrsim N_{\Lambda}$ have a common longest relaxation time, as explained in Eq. (19), and, consequently, their scission is promoted to the same degree by the shear flow.

Next, we demonstrate that τ_{Λ} defined as the value for which $\tau_r(N_{\rm ag}) = \tau_b(N_{\rm ag})$ [Fig. 5(a)] serves as the characteristic timescale in flow-induced scission. For this purpose, we consider several systems where τ_{Λ} takes different values by conducting DPD simulations with different k_BT [Fig. 5(b)]. We show τ_b for $N_{ag} = 300, 400$, and 500 as a function of Wi_{Λ} in Fig. 8. Here, τ_b is normalized by the value $\tau_b^{\ 0}$ at equilibrium for a given $N_{\rm ag}$. For comparison, we show $\tau_b/\tau_b^{\ 0}$ as a function of $\dot{\gamma}$ in the inset of Fig. 8. The increase in

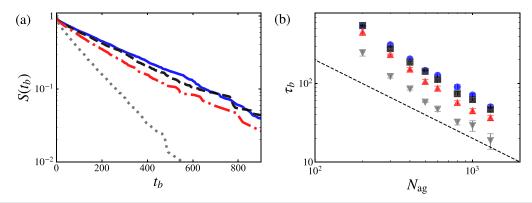


FIG. 7. (a) Survival function $S(t_b)$ of micelles with $N_{ag}=300$ for $Wi_{\Lambda}=0$ (blue solid line), 4.0 (black dashed line), 8.0 (red dotted-dashed line), and 16 (gray dotted line) with $k_BT=1$. (b) Average lifetime τ_b of micelles as a function of the aggregation number $N_{\rm ag}$ for $Wi_{\Lambda}=0$ (blue circle), 4.0 (black square), 8.0 (red triangle), and 16 (gray inverted triangle) with $k_BT=1$. The black dashed line in (b) indicates $\tau_b \propto N_{a0}^{-1}$. The error bars in (b) denote the standard deviations for three independent

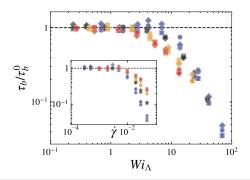


FIG. 8. Average lifetime τ_b normalized by the value $\tau_b{}^0$ at equilibrium as a function of the Weissenberg number $W_{l\Lambda}$ for $N_{ag}=300(\circ)$, $400(\Box)$, and $500(\circ)$ with $k_BT=0.9$ (blue), 1 (black), 1.1 (orange), and 1.2 (red). The inset shows $\tau_b/\tau_b{}^0$ as a function of the shear rate \dot{p} . The black dashed line indicates $\tau_b/\tau_b{}^0=1$. The error bars denote the standard deviations for three independent simulations.

 $\tau_b/\tau_b^{\ 0}$ with k_BT for fixed \dot{y} indicates that scission of micelles is promoted more as the temperature is decreased for given \dot{y} . In other words, the \dot{y} dependence of $\tau_b/\tau_b^{\ 0}$ significantly differs depending on k_BT ; micelles at a lower temperature are more likely to be broken by the shear flow. We emphasize that we can take into account this k_BT dependence by using τ_Λ . More concretely, all the data for different k_BT as well as for different $N_{\rm ag}$ follow a single function of Wi_Λ (Fig. 8). The reason for this collapse is that micelles with $N_{\rm ag} \gtrsim N_\Lambda$ are aligned and elongated by the shear flow with a timescale τ_Λ , as we will discuss below (see Fig. 9). We have also confirmed that if $\phi \lesssim 0.1$, $\tau_b/\tau_b^{\ 0}$ follows the same function shown in Fig. 8. Since ϕ does not significantly change the properties of micelles within the dilute regime, it is reasonable that $\tau_b/\tau_b^{\ 0}$ is independent of $\phi(\lesssim 0.1)$. Interestingly, as shown in Fig. 8, $\tau_b \simeq \tau_b^{\ 0}$ when Wi_Λ is smaller than a threshold value $Wi_c(\simeq 4)$, indicating that flowinduced scission does not occur, whereas τ_b monotonically decreases with Wi_Λ for $Wi_\Lambda > Wi_C$. However, it is difficult to discuss this

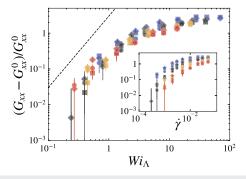


FIG. 9. Relative change $(G_{xx}-G_{xx}^{\ 0})/G_{xx}^{\ 0}$ of diagonal component G_{xx} of the gyration tensor normalized by the value $G_{xx}^{\ 0}$ at equilibrium as a function of the Weissenberg number Wi_{Λ} for $N_{ag}=300(\circ),400(\Box)$, and $500(\circ)$ with $k_BT=0.9$ (blue), 1 (black), 1.1 (orange), and 1.2 (red). The black dashed line indicates $(G_{xx}-G_{xx}^{\ 0})/G_{xx}^{\ 0} \propto Wi_{\Lambda}^2$. The inset shows $(G_{xx}-G_{xx}^{\ 0})/G_{xx}^{\ 0}$ as a function of the standard deviations for three independent simulations

threshold Weissenberg number Wi_c in more detail due to the limited accuracy of τ_b . We examine Wi_c in another way, as described below (see Fig. 11). Since τ_r monotonically increases with $N_{\rm ag}$ [Fig. 3(b)], it may be counterintuitive that the threshold shear rate for flow-induced scission is independent of $N_{\rm ag}$ for fixed k_BT . As mentioned in Sec. III A, since the considered micelles satisfy $\tau_b(N_{\rm ag}) < \tau_r(N_{\rm ag})$ (i.e., $N_{\rm ag} > N_{\Lambda}$), the slower relaxation timescales $(\tau_r > \tau_{\Lambda})$ disappear as a result of scission faster than the rotational relaxation, thus leading to a common threshold shear rate. In other words, the segment of size N_{Λ} determines the effects of shear flow on micelles with $N_{\rm ag} \gtrsim N_{\Lambda}$.

We investigate the gyration tensor defined by Eq. (17), which characterizes the micellar structure, to demonstrate that τ_{Λ} plays a vital role in the orientation and elongation of micelles under shear flow. Figure 9 shows the relative change $(G_{xx} - G_{xx}^{\ 0})/G_{xx}^{\ 0}$ of the diagonal component G_{xx} corresponding to the flow direction, where G_{xx}^{0} is the value at equilibrium for fixed N_{ag} . All the data for different k_BT and N_{ag} approximately collapse on a single function of Wi_{Λ} , which indicates that Wi_{Λ} determines the orientation and elongation of micelles under shear flow. This is consistent with the previous study,²⁵ which used linear chain models including scission and recombination kinetics. Therefore, we conclude that Wi_{Λ} determines the effects of the shear flow on micelles, such as orientation and elongation, thus determining the degree of flow-induced scission, i.e., τ_b/τ_b^0 , because the elongation of micelles causes their scission. ^{19,45} For comparison, we show $(G_{xx} - G_{xx}^{\ 0})/G_{xx}^{\ 0}$ as a function of $\dot{\gamma}$ in the inset of Fig. 9. Without considering τ_{Λ} , $(G_{xx} - G_{xx}^{\ 0})/G_{xx}^{\ 0}$ depends on \dot{y} differently for each k_BT ; its \dot{y} dependence varies greatly depending on k_BT . Therefore, τ_{Λ} is an important property for understanding the shear-rate dependence of the micellar dynamics under shear flow. In addition, $(G_{xx} - G_{xx}^{\ 0})/G_{xx}^{\ 0}$ is independent of N_{ag} for fixed k_BT and $\dot{\gamma}$. This is consistent with our claim that micelles with $N_{ag} \gtrsim N_{\Lambda}$ have a common longest relaxation time for given $k_B T$. In Fig. 9, we find that $(G_{xx} - G_{xx}^{\ 0})/G_{xx}^{\ 0} \propto Wi_{\Lambda}^2$ holds for $Wi_{\Lambda} \lesssim 1$, which is a well-known characteristic of polymers.⁴⁶ This indicates that micelles behave similarly to polymers under shear flow for moderate Wi_{Λ} .

Here, note that $\tau_b/\tau_b^{~0}$ and $(G_{xx}-G_{xx}^{~0})/G_{xx}^{~0}$ do not completely follow a single curve, as shown in Figs. 8 and 9, indicating that there exist other relevant factors. For example, regarding semiflexible polymers, stiffness significantly affects their properties under shear flow. 47 In addition, although we do not consider the effect of branched micellar structures, these complex structures may also play a role in the micellar dynamics as demonstrated in a previous study. 48 Thus, topological characterization of micelles using the recently developed method 49 can provide valuable information about the detailed mechanism of flow-induced scission. This is an important near-future study.

We have seen that our analysis of the lifetime using conditional statistics clearly reveals how flow-induced scission affects individual micelles. Next, to examine how flow-induced scission affects the distribution of $N_{\rm ag}$, we focus on the Wi_{Λ} dependence of the probability density function $P(N_{\rm ag})$ of $N_{\rm ag}$. Figure 10 shows $P(N_{\rm ag})$ for several values of Wi_{Λ} with $k_BT=1$. For $Wi_{\Lambda} < Wi_c (\simeq 4)$, $P(N_{\rm ag})$ is independent of Wi_{Λ} . This indicates that flow-induced scission does not occur for $Wi_{\Lambda} < Wi_c$, which is consistent with the results shown in Fig. 8. For Wi_{Λ} larger than Wi_c , in contrast, $P(N_{\rm ag})$ for large $N_{\rm ag}$ decreases and the distribution shifts to

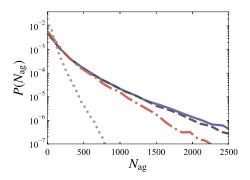


FIG. 10. Probability density function $P(N_{\rm ag})$ of the aggregation number $N_{\rm ag}$ for $Wi_{\Lambda}=0$ (blue solid line), 4.0 (black dashed line), 8.0 (red dotted-dashed line), and 40 (gray dotted line) with $k_{B}T=1$.

smaller $N_{\rm ag}$ as Wi_{Λ} increases. Therefore, it is clear that when Wi_{Λ} exceeds Wi_c , flow-induced scission occurs, and then the population of large micelles declines. Note that for $Wi_{\Lambda}=0$, $P(N_{\rm ag})$ cannot be expressed by a single exponential function, whereas the model proposed by Cates²³ predicts the exponential distribution of micellar length. As shown in Fig. 4(b), micelles with $N_{\rm ag}\lesssim 300$ do not satisfy the assumption that chains can break with a fixed probability per unit length per unit time. Therefore, it is reasonable that $P(N_{\rm ag})$ does not obey a single exponential function, although we focus on $N_{\rm ag}$ instead of micellar length. Dhakal and Sureshkumar⁵⁰ also reported that $P(N_{\rm ag})$ did not obey an exponential function for charged micelles when the salt-to-surfactant concentration ratio was smaller than 1.

Before closing this article, we focus on the average number $\overline{N}_{\rm mic}$ of micelles in the system and the mean aggregation number $\overline{N}_{\rm ag}$, which reflect the onset of flow-induced scission, as discussed below. Figure 11(a) shows $\overline{N}_{\rm mic}$ normalized by the value $\overline{N}_{\rm mic}^{\ 0}$ at equilibrium as a function of Wi_{Λ} . We find that $\overline{N}_{\rm mic}/\overline{N}_{\rm mic}^{\ 0}$ is expressed by a single function of Wi_{Λ} irrespective of k_BT . In addition, Fig. 11(a) provides clear evidence that flow-induced scission occurs for $Wi_{\Lambda} > Wi_c$

(\simeq 4). These observations are also valid for \overline{N}_{ag} shown in Fig. 11(b). These results support the conclusion that τ_{Λ} is a relevant timescale of unentangled surfactant micelles. In the case of the parameters used in the present study, the average properties of the system, such as $\overline{N}_{\text{mic}}$ and \overline{N}_{ag} , are also determined by Wi_{Λ} . Since more than 65% of surfactants in the system belong to micelles with $N_{\rm ag} \gtrsim N_{\Lambda}$ at equilibrium with $k_BT = 1$, it is quite reasonable that τ_{Λ} has a dominant influence on the average properties. Therefore, if we conduct experiments on the surfactant solutions where most surfactant molecules belong to micelles with $N_{\rm ag} \gtrsim N_{\Lambda}$, the longest relaxation time τ_{Λ} will be a relevant timescale of the system. In other words, the experimentally obtained bulk properties such as viscosity are likely to be characterized by τ_{Λ} . Indeed, as shown in Appendix B, Wi_{Λ} determines the rheological properties of the considered solutions. Note that we take full advantage of molecular simulations to evaluate the longest relaxation time. We propose a method to obtain τ_{Λ} through the $N_{\rm ag}$ dependences of τ_r and τ_b , which are usually unavailable in experiments.

IV. CONCLUSIONS

In the present study, we have investigated flow-induced scission of wormlike micelles in nonionic surfactant solutions under shear flow with DPD. Although flow-induced scission may be intuitively obvious, a quantitative understanding of this phenomenon has been unsatisfactory. This was mainly due to the difficulty of obtaining a large amount of micellar scission data for various aggregation numbers $N_{\rm ag}$ and the lack of methods to estimate the relevant timescale of individual unentangled micelles. With the aid of the DPD method, which allows us to simulate large systems for long timescales, we can obtain a sufficient amount of data to discuss the statistical properties of micellar scission in detail.

In order to elucidate flow-induced scission in terms of micellar timescales, we have proposed a method to estimate the longest relaxation time τ_{Λ} of unentangled surfactant micelles from the rotational relaxation time τ_r (Fig. 3) and the average lifetime τ_b (Fig. 4) at equilibrium in the absence of shear flow. Using the concept proposed by Faivre and Gardissat, ²⁴ which originally assumed the Rouse

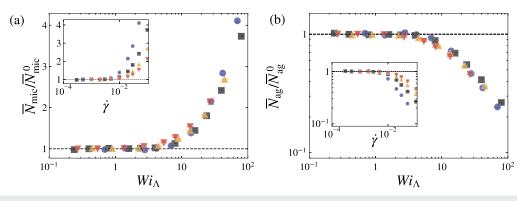


FIG. 11. (a) Average number $\overline{N}_{\text{mic}}$ of micelles in the system normalized by the value $\overline{N}_{\text{mic}}^0$ at equilibrium as a function of the Weissenberg number $W_{i_{\Lambda}}$. The black dashed line indicates $\overline{N}_{\text{mic}}/\overline{N}_{\text{mic}}^0 = 1$. The inset shows $\overline{N}_{\text{mic}}/\overline{N}_{\text{mic}}^0$ as a function of the shear rate \dot{y} . (b) Mean aggregation number \overline{N}_{ag} normalized by the value $\overline{N}_{\text{ag}}^0$ at equilibrium as a function of $W_{i_{\Lambda}}$. The black dashed line indicates $\overline{N}_{\text{ag}}/\overline{N}_{\text{ag}}^0 = 1$. The inset shows $\overline{N}_{\text{ag}}/\overline{N}_{\text{ag}}^0$ as a function of \dot{y} . Different symbols correspond to different values of $k_B T$: blue circle, 0.9; black square, 1; orange triangle, 1.1; red inverted triangle, 1.2.

chain with scission and recombination processes, we have evaluated τ_{Λ} from the intersection of $\tau_r(N_{\rm ag})$ and $\tau_b(N_{\rm ag})$ [Fig. 5(a)]. This concept means that relaxation modes such that $\tau_r \gtrsim \tau_{\Lambda}$ disappear because the timescale of micellar scission is shorter than that of rotational relaxation for these modes. In fact, as shown in Fig. 6, the MSD of surfactant molecules has provided evidence that τ_{Λ} is a crucial timescale at equilibrium. More concretely, τ_{Λ} is comparable to the crossover time from subdiffusion to normal diffusion for different temperatures. These results are in agreement with the previous study using linear chains with a kinetic model for scission and recombination. Thus, we have found that the concept proposed by Faivre and Gardissat is also applicable to unentangled surfactant micelles when we develop the method to evaluate the longest relaxation time using data from molecular simulations.

One of the most important conclusions of the present study is that τ_{Λ} is a crucial timescale for flow-induced scission of wormlike surfactant micelles under shear flow. Our analysis relies on conditional statistics based on the aggregation number $N_{\rm ag}$, which reveals the shear flow effect on individual micelles in detail. Indeed, the survival function $S(t_b)$ of micelles for fixed N_{ag} has demonstrated that flow-induced scission occurs for high shear rates [Fig. 7(a)]. We have also found in Fig. 7(b) that for large $N_{\rm ag}$, $\tau_b \propto N_{\rm ag}^{-1}$ holds even under shear flow, similarly to the equilibrium state [Fig. 4(b)]. To demonstrate the role of τ_{Λ} in the shear-rate dependence of τ_{b} , we have conducted DPD simulations for different temperatures. We have shown that the Weissenberg number Wi_{Λ} , which is defined as the product of the longest relaxation time τ_{Λ} and the shear rate \dot{y} , determines τ_b under shear flow (Fig. 8). To the best of our knowledge, this is the first attempt to show that τ_b can be characterized by the nondimensionalized shear rate. Since Wi_{Λ} also determines the diagonal component G_{xx} of the gyration tensor G_{ij} (Fig. 9), the Wi_{Λ} dependence of τ_b is associated with the elongation of micelles. However, since the collapse is slightly unclear in Figs. 8 and 9, our numerical results suggest that, in addition to Wi_{Λ} , there exist other important factors, such as stiffness and branched micellar structures. We have examined the Wi_{Λ} dependence of the micellar distribution (Fig. 10), the average number of micelles [Fig. 11(a)], and the average aggregation number [Fig. 11(b)]. We then conclude that flow-induced micellar scission occurs when Wi_{Λ} is larger than a threshold Weissenberg number Wi_c . Although $Wi_c \simeq 4$ in the examined system, we speculate that Wi_c depends on various factors, such as the conservative force coefficients a_{ii} in the

In the present study, we have revealed the shear-rate dependence of flow-induced scission focusing on nonionic surfactants. However, further studies are required. First, our results are restricted to the case of nonionic surfactant micelles. Regarding the scission of ionic surfactant micelles, we must consider the effect of counterions. However, the proposed method to evaluate τ_{Λ} from τ_r and τ_b is applicable to molecular simulations of unentangled surfactant micelles regardless of the kind of surfactant. Thus, it is an interesting future study to investigate flow-induced scission of different kinds of surfactant micelles and reveal their differences, which will provide helpful insight into the practical applications of surfactant solutions. Second, we have not revealed the physical mechanism behind the statistical properties of flow-induced scission. To overcome this deficiency, it is necessary to reveal the

dynamics of individual micelles, such as alignment and elongation. ¹⁹ Flow-induced scission is expected to have a great impact on micellar dynamics, thus leading to complicated behavior different from that of polymer chains (i.e., chains without scission kinetics). In addition, it is essential to understand flow-induced scission in terms of mechanics such as stress and energy. ^{18,19} Third, we should take into account the structural diversity in micelles. Here, we focused on conditional statistics based on aggregation numbers. However, as shown in Appendix A, micelles can form different structures even for a given aggregation number. It is, therefore, important to conduct a more detailed conditional analysis considering micellar structures.

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AUTHOR DECLARATIONS

Conflict of Interest

The authors have no conflicts to disclose.

Author Contributions

Yusuke Koide: Conceptualization (equal); Data curation (lead); Formal analysis (lead); Investigation (lead); Methodology (equal); Validation (lead); Visualization (lead); Writing – original draft (lead); Writing – review & editing (equal). Susumu Goto: Conceptualization (equal); Funding acquisition (lead); Project administration (lead); Resources (lead); Supervision (lead); Writing – original draft (supporting); Writing – review & editing (equal).

DATA AVAILABILITY

The data that support the findings of this study are available from the corresponding author upon reasonable request.

APPENDIX A: STRUCTURAL PROPERTIES OF MICELLES AT EQUILIBRIUM

We adopt conditional statistics based on the aggregation number $N_{\rm ag}$. In this appendix, we show the relationship between the micellar structure and $N_{\rm ag}$.

First, we show snapshots of micelles for various $N_{\rm ag}$ in Fig. 12, which qualitatively demonstrate how micelles grow with $N_{\rm ag}$. Surfactants form spherical, rodlike, wormlike, and branched wormlike micelles as $N_{\rm ag}$ increases. Note, however, that micelles can form various structures even for a given $N_{\rm ag}$. In particular, for $N_{\rm ag} \gtrsim 200$, both linear and branched micelles exist.

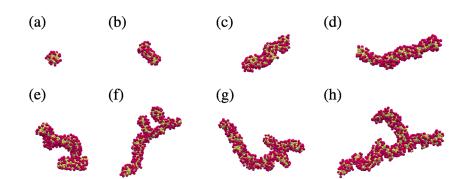


FIG. 12. Snapshots of micelles for (a) $N_{\rm ag}=40$, (b) 70, (c) 200, (d) 300, (e) 400, (f) 500, (g) 600, and (h) 700.

Next, to quantitatively investigate the structures of micelles, we focus on the gyration radius R_g and relative shape anisotropy⁵¹ K^2 . These quantities are expressed as

$$R_g^2 = G_{xx} + G_{yy} + G_{zz} \tag{A1}$$

and

$$K^{2} = 1 - 3 \frac{G_{xx}G_{yy} + G_{yy}G_{zz} + G_{zz}G_{xx} - G_{xy}^{2} - G_{yz}^{2} - G_{zx}^{2}}{(G_{xx} + G_{yy} + G_{zz})^{2}}$$
(A2)

in terms of the gyration tensor G_{ij} defined by Eq. (17). The relative shape anisotropy K^2 can take values between 0 and 1. A spherical structure is characterized by $K^2 \simeq 0$, and a rodlike structure is characterized by $K^2 \simeq 1$. Figure 13 shows R_g and K^2 as functions of $N_{\rm ag}$. Figure 13(a) shows that $R_g \propto N_{\rm ag}^{1/3}$ for $N_{\rm ag} \lesssim 50$. This behavior changes around $N_{\rm ag} = 50$. Since $R_g \propto N_{\rm ag}^{1/3}$ holds for spherical micelles,³¹ the structural transition of micelles occurs around $N_{\rm ag} = 50$. In addition, Fig. 13(b) demonstrates that $K^2 \simeq 0$ for $N_{\rm ag} \lesssim 50$, and K^2 becomes much larger for $N_{\rm ag} \gtrsim 50$. Therefore, micelles are spherical for $N_{\rm ag} \lesssim 50$, whereas micelles are rodlike for $N_{\rm ag} \gtrsim 50$. Note also a gradual decrease of K^2 for $N_{\rm ag} \gtrsim 200$ [Fig. 13(b)]. This is because micelles for $N_{\rm ag} \gtrsim 200$ are wormlike and flexible. These quantitative results are consistent with the visualizations of micellar structures shown in Fig. 12. Thus, R_g and K^2 enable us to estimate the structure of micelles (i.e., spherical, rodlike, or wormlike). According to these criteria for micellar structures in terms of $N_{\rm ag}$, we mainly deal with rodlike and wormlike micelles in the present study. We need to conduct a more detailed analysis to

characterize branched structures. This is an important near-future study.

APPENDIX B: RHEOLOGICAL PROPERTIES OF SURFACTANT SOLUTIONS

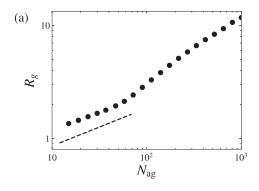
In this appendix, we show the rheological properties of the considered surfactant solutions. The stress tensor σ can be calculated using the Irving–Kirkwood equation, ⁵²

$$\sigma = -\frac{1}{V} \left\langle \sum_{i=1}^{N} m \mathbf{v}_i \mathbf{v}_i + \sum_{i=1}^{N} \sum_{j>i}^{N} \mathbf{r}_{ij} \mathbf{F}_{ij} \right\rangle, \tag{B1}$$

where V is the volume of the system. Then, the viscosity η and the first normal stress coefficient Ψ_1 are evaluated by

$$\eta = \frac{\sigma_{yx}}{\dot{y}} \quad \text{and} \quad \Psi_1 = \frac{\sigma_{xx} - \sigma_{yy}}{\dot{y}^2},$$
(B2)

respectively. Figure 14 shows the Wi_{Λ} dependences of η and Ψ_1 for several k_BT . Here, η is shown in the form of $(\eta - \eta_s)/(\eta_0 - \eta_s)$, where η_s is the viscosity of water at a given k_BT and η_0 is the viscosity of the solution at the lowest shear rate. The value of Ψ_1 is normalized by $\Psi_{1,0}$ at the lowest shear rate. Both η and Ψ_1 decrease with Wi_{Λ} when $Wi_{\Lambda} \gtrsim 1$. One might think that flow-induced scission causes this shear thinning. However, since the alignment of micelles in the flow direction also contributes to the shear thinning, a more detailed analysis is required to identify the effect of flow-induced scission on rheological properties. As shown in Fig. 14(b), the first normal stress



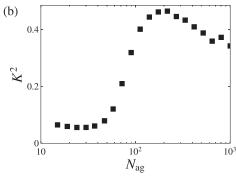
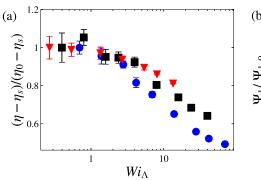


FIG. 13. (a) Gyration radius R_g and (b) relative shape anisotropy K^2 as functions of the aggregation number $N_{\rm ag}$ with $k_BT=1$. The dashed line in (a) indicates $R_g \sim N_{\rm ag}^{1/3}$.



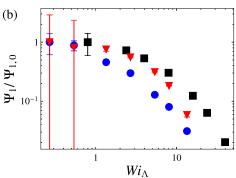


FIG. 14. (a) Increase in viscosity $\eta-\eta_s$ of the solutions from the solvent viscosity η_s normalized by the value $\eta_0-\eta_s$ at the lowest shear rate and (b) first normal stress coefficient Ψ_1 normalized by the value $\Psi_{1,0}$ at the lowest shear rate as functions of the Weissenberg number Wi_{Λ} . Different symbols correspond to different values of k_BT : blue circle, 0.9; black square, 1; red inverted triangle, 1.2. The error bars denote the standard deviations for three independent simulations.

difference is positive, indicating that the surfactant solutions have viscoelasticity.

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