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Bayesian Bilinear Inference for Joint Channel Tracking and Data Detection in Millimeter-Wave MIMO Systems

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Abstract—We propose a novel joint channel tracking and data detection (JCTDD) scheme to combat the channel aging phenomenon typical of millimeter-wave (mmWave) multipleinput multiple-output (MIMO) communication systems in high-mobility scenarios. The contribution aims to significantly reduce the communication overhead required to estimate timevarying mmWave channels by leveraging a Bayesian message passing framework based on Gaussian approximation, to jointly perform channel tracking (CT) and data detection (DD). The proposed method can be interpreted as an extension of the Kalman filter-based two-stage tracking mechanism to a Bayesian bilinear inference (BBI)-based joint channel and data estimation (JCDE) framework, featuring the ability to predict future channel state information (CSI) from both reference and payload signals by using an auto-regressive (AR) model describing the time variability of mmWave channel as a state transition model in a bilinear inference algorithm. The resulting JCTDD scheme allows us to track the symbol-by-symbol time variation of channels without embedding additional pilots, leaving any added redundancy to be exploited for channel coding, dramatically improving system performance. The efficacy of the proposed method is confirmed by computer simulations, which show that the proposed method not only significantly outperforms the stateof-the-art (SotA) but also approaches the performance of an idealized Genie-aided scheme.

Index Terms—mmWave communications, data detection, channel aging, channel tracking, Bayesian bilinear inference.

I. INTRODUCTION

MILLIMETER-WAVE (mmWave) technology is a promising solution to provide high data rate and low

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latency wireless communications services by exploiting the available wide spectrum in the 30 GHz to 300 GHz range [1], [2], [3], and has therefore been adopted in various recently-developed systems including 5G cellular and Wi-Fi 6. In order to fully realize the potential of mmWave communications, however, propagation losses must be effectively mitigated via beamforming techniques that require accurate channel state information (CSI).

Various effective beamforming schemes have therefore been proposed that leverage the statistical properties of mmWave wireless channels, such as their low-rankness and sparsity [4], [5], [6], [7]. These works assume, however, that the estimated mmWave channel remains constant over the duration of data transmission, while in practice the high directivity of mmWave signals makes their propagation highly susceptible to changes in the environment, such as mobility, reflections from obstacles, and the weather, which can result in significant variations in the channel characteristics [8], [9], [10], [11], [12], [13]. In particular, static or quasi-static fading assumptions are not valid for high-mobility scenarios [14], [15], [16] in time-varying mmWave wireless channels.

A primary challenge for wireless communications over mmWave multiple-input multiple-output time-varying (MIMO) channels is the increase in the communication overhead required for CSI acquisition [17], [18], [19], [20], [21], [22], [23]. In sharp beamforming, which uses a large number of antenna elements to concentrate power over a limited angular spread, it has been shown that even millisecond-scale fluctuations in the surrounding environment can cause the beam to lose its integrity with respect to the channel, causing significant performance degradation [13]. However, since reliable channel estimation (CE) inherently involves a pilot/training overhead that increases proportional to the number of antennas, frequent CE to maintain accurate CSI knowledge may result in non-negligible losses in spectrum efficiency.

To tackle this channel aging issue, several channel estimation/tracking (CE/CT) methods have been proposed for time-varying mmWave wireless communications. In [20], for instance, a two-stage channel tracking algorithm for downlink mmWave multi-user MIMO systems over time-varying channels was proposed under the assumption that the time variations of angles of arrival/departure (AoA/AoD) are much slower than the dynamics of the channel gains. For such

a scenario, a novel pilot transmission frame was designed, where angle parameters are estimated at the beginning of the transmission frame while channel gains are tracked using shorter pilot sequences periodically inserted multiple times within the transmission frame. By separating the phenomena according to their time-varying rates and estimating each corresponding parameter separately, the required pilot overhead can be reduced. A similar separation and two-stage transmission frame were also employed in [21] and [22], in which the time-varying CE problem is formulated as a tensor decomposition problem solved by the least square (LS) approach, while taking Doppler shifts into consideration.

Another solution is the expectation maximization-based channel tracking (CT) method [23], which exploits the low-rank property of the mmWave MIMO channel. By making the assumption that the channel is quasi-static for a given time, and varies from block-by-block, this method achieves time-varying CE by tracking the model parameters of the sparse virtual channel with the Kalman filter (KF). The more realistic symbol-by-symbol time-varying nature of wireless channels, *i.e.*, channel aging, is often modeled as an auto-regressive (AR) process [24], [25], [26], [27], [28], but even here, the KF-based CT approach can still be utilized [25], [26], although machine learning (ML)-aided counterparts are also emerging, examples of which are the schemes in [26] and [27], where a deep neural network (DNN) was employed to perform channel prediction.

From the theoretical aspect, a rigorous analysis of the signal-to-interference-plus-noise ratio (SINR) and mean square error (MSE) performance of a system under time-variant Rayleigh fading was presented in [28]. After deriving a quasi-closed form of the average SINR leveraging random matrix theory, the importance of taking the auto-correlation coefficients into consideration in algorithm design was clarified.

We highlight that all the aforementioned studies considered CE/CT based only on reference signaling, *e.g.*, pilot sequences, which suggests that further overhead reduction can be achieved if estimated data symbols can be exploited as soft references for channel estimation. The latter approach is hereafter referred to as joint channel tracking and data detection (JCTDD).

A similar idea has been employed in the design of conventional joint channel and data estimation (JCDE) algorithms based on the Bayesian bilinear inference (BBI) framework [29], [30], [31], [32], [33] and has been shown, both in theory and implementation, to achieve high performance in a variety of wireless communication systems. Indeed, the authors have also recently shown that the BBI framework can be employed in the design of grant-free (GF) access schemes [34], joint activity and channel estimation (JACE) for extra-large MIMO (XL-MIMO) systems [35], and JCDE of cell-free massive MIMO (CF-mMIMO) systems [36], all of which were demonstrated to outperform earlier state-ofthe-art (SotA) methods. Although the tracking aspect of the problem dramatically increases its difficulty, because both channel coefficients and data symbols are time-varying at the scale of symbol duration, the BBI framework at the base of SotA JCDE algorithms is also a key ingredient of the JCTDD algorithm introduced here as a novel solution to overcome the

challenges related to time-varying mmWave MIMO systems. The idea of an extension of the BBI framework to the JCTDD problem requires elaborate algorithmic additions/modifications and is therefore not straightforward, which must incorporate a channel state transition model while appropriately combining messages to account for channel aging.

With that in mind, we extend the BBI framework to the JCTDD problem, theoretically enabling the compensation of channel aging effect without any additional pilots, via the alternation of the proposed CT and data detection (DD) solutions. This indicates that the processing of the proposed algorithm is completed inside the DD block and does not require any changes in frame format, higher-level functions, or protocols. The objective of this article is to provide new insight into the efficacy of the BBI framework in the mitigation of the time-varying nature of mmWave wireless communication channels. Specifically, we contribute with a customized BBI-based JCTDD receiver design to address the aforementioned inherent problems of time-varying mmWave MIMO systems, including CT and DD in the uplink.

Our contribution, summarized below, is fundamentally algorithmic, such that our results are presented in terms of the normalized mean square errors (NMSEs) of estimated quantities and bit error rates (BERs) computed from actual constellation points:

- A novel JCTDD algorithm is presented, wherein a BBIbased channel prediction (CP)-aided message passing is performed while exploiting the AR model describing the time-varying nature of mmWave wireless channels as the state transition model. The basic concept of the method is inherited from the two-stage tracking mechanism of the KF, and consists of a CP phase that generates prior estimates of current and future CSI based on past channel estimates, and a JCDE phase that generates posterior estimates of channel coefficients and data symbols based on those prior estimates, which are repeated sequentially. The main challenge to achieve JCTDD is, however, that only one snapshot is available for a given channel realization, since both the channel coefficients and the data symbols are time-varying, and the diversity gain across the time dimension cannot be obtained by applying the JCDE algorithm as-is. This is solved by also incorporating a CP mechanism based on the state transition model into the process to generate beliefs that propagate along edges on the factor graph (FG) in order to extract information about the current CSI from past and future observations. In other words, unlike the KF, here the prediction mechanism is present in both phases. An appropriate sequential update rule is also designed to ensure that the proposed JCTDD algorithm successfully captures the time variability of the channel.
- A new insight into the design of transceivers for timevarying mmWave MIMO systems is given, in that it is shown that, thanks to the BBI-based JCTDD algorithm, the addition of pilots within a transmission frame is not a suboptimal approach to exploit redundancy in the combat of time-varying channels, since the latter

is outperformed by channel coding. To elaborate, our receiver design is found to capitalize on available degrees of freedom (DoF) via its BBI framework, which enables highly accurate CT and DD without any additional pilots, even in relatively high-mobility communication scenarios with relative speed of 45 [kmph] or higher. In fact, this algorithmic feature allows the proposed method to operate based on the Bayesian framework in different transmission frame formats (e.g., frame configurations with additional pilots), utilizing the additional available knowledge as prior information, without any change in the algorithm structure. Simulation results show that the proposed method approaches the ideal genie-aided performance using only an initial CSI estimated at the beginning of the frame, and channel coding thereafter.

In addition to the aforementioned contributions, we highlight that, to the best of our knowledge, there is no previous work in the literature offering a systematic JCTDD receiver design for time-varying mmWave MIMO communication systems via Bayesian bilinear inference.

Notation: The following notation is used throughout, unless when otherwise specified. Sets of counting, integer, real, and complex numbers are denoted by \mathbb{N} , \mathbb{Z} , \mathbb{R} , and \mathbb{C} , respectively. Vectors and matrices are denoted in lower- and upper-case bold-face fonts, respectively. The conjugate, transpose, and conjugate transpose operators are denoted by $(\cdot)^*$, $(\cdot)^T$, and $(\cdot)^{H}$, respectively. The expectation of a given random variable is denoted by $\mathbb{E}[\cdot]$. Random variables and their outcomes are denoted in sans serif and italic fonts, respectively, as in a and a, such that the conditional probability density function (PDF) and the conditional expectation of the outcome a of a, given the occurrence b of b are respectively denoted by $p_{a|b}(a|b)$ and $\mathbb{E}_{\mathsf{a}|\mathsf{b}}[a|b]$. The real and imaginary parts of a complex quantity are respectively denoted by $\Re\{\cdot\}$ and $\Im\{\cdot\}$. The $a \times a$ square identity matrix is denoted by I_a . The (i, j)-th element, the j-th column vector, and the sub-matrix consisting of rows a_1 to a_2 and columns b_1 to b_2 of a matrix \boldsymbol{A} are respectively denoted by $[A]_{i,j}$, $[A]_{:,j}$ and $[A]_{a_1:a_2,b_1:b_2}$. The complex Gaussian distribution with mean a and variance b is denoted by $\mathcal{CN}(a,b)$. The notation $a \sim p_{\mathbf{a}}(a)$ indicates that a variable a obeys $p_a(a)$. The symbols \propto and \otimes are used to denote proportionality and Kronecker product, respectively. Finally, following the style of related literatures [32], [33], [34], [35], and [36], we omit the integrating variable differential from all integrals and use the notation $\sum_{i\neq j}^I a_i \triangleq \sum_{i=1}^I a_i - a_j$, for

II. SYSTEM MODEL

A. Channel Model

Consider a mmWave MIMO system with $N_{\rm TX}$ transmit (TX) antennas and $N_{\rm RX}$ receive (RX) antennas that simultaneously supports elevation and azimuth beamforming. Following existing literatures [37], [38], [39], and [40], the well-known clustered mmWave channel model with L clusters, each having C_ℓ rays with $\ell \in \mathcal{L} \triangleq \{1,2,\ldots,L\}$ is considered, so as to capture the sparsely scattered nature of mmWave channels. The corresponding $N_{\rm RX} \times N_{\rm TX}$ channel matrix can then be

expressed as [41]:

$$\begin{split} \hat{\boldsymbol{H}} &= \frac{1}{\sqrt{L}} \sum_{\ell=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{\sigma_{\ell,c}}{\sqrt{C_{\ell}}} \underbrace{\boldsymbol{a}_{N_{\mathrm{RX}}} \left(\boldsymbol{\theta}_{\ell,c}^{\mathrm{RX}}, \boldsymbol{\phi}_{\ell,c}^{\mathrm{RX}}\right) \boldsymbol{a}_{N_{\mathrm{TX}}}^{\mathrm{H}} \left(\boldsymbol{\theta}_{\ell,c}^{\mathrm{TX}}, \boldsymbol{\phi}_{\ell,c}^{\mathrm{TX}}\right)}_{\triangleq \hat{\boldsymbol{A}}_{\ell,c}: \text{ Array response matrix}}, \end{split} \tag{1}$$

where $\theta_{\ell,c}^{\rm RX}$ and $\theta_{\ell,c}^{\rm TX}$ are respectively the elevation angle of arrival (AoA) and angle of departure (AoD) corresponding to the c-th ray of the ℓ -th scattering cluster, $\phi_{\ell,c}^{\rm RX}$ and $\phi_{\ell,c}^{\rm TX}$ are respectively the azimuth AoA and AoD corresponding to the c-th ray of the ℓ -th scattering cluster, and $\sigma_{\ell,c} \sim \mathcal{CN} (0,1)$ is a small-scale fading coefficient. Assuming that both the transmitter and receiver are equipped with uniformly spaced planar antenna arrays (UPAs), each with half-wavelength antenna element separations along the elevation-and-azimuth-axis, the array response vector in (1) is then given by

$$a_P(\theta, \phi) \triangleq c_{\sqrt{P}}(\sin(\theta)\cos(\phi)) \otimes c_{\sqrt{P}}(\cos(\theta)),$$
 (2)

with

$$c_{\sqrt{P}}(v) \triangleq \frac{1}{\sqrt{P}} \left[1, e^{j\pi v}, \dots, e^{j\pi \left(\sqrt{P}-1\right)v} \right]^{\mathsf{T}}.$$
 (3)

The block fading assumption that the channel remains constant during the transmission of several data symbols holds for low-mobility telecommunication systems, but for mmWave orthogonal frequency-division multiplexing (OFDM)-MIMO systems, especially in high-mobility scenarios, the channel aging phenomenon cannot be ignored and this assumption often does not hold [14], [15], [16].

To represent the OFDM symbol-by-symbol time-varying nature of wireless channels, *i.e.*, channel aging, in high-mobility mmWave communication systems based on the channel model described above, at the discrete time index k, the time-varying characteristics of small-scale fading coefficients $\sigma_{\ell,c}$ in (1) can be expressed by using AR model as

$$\sigma_{\ell,c}[k] = \begin{cases} \mathcal{CN}(0,1) & k = 0, \\ r\sigma_{\ell,c}[k-1] + \sqrt{1 - r^2} \omega_{\ell,c}[k] & k \in \mathbb{N}, \end{cases}$$
(4)

where $\omega_{\ell,c}[k] \sim \mathcal{CN}\left(0,1\right)$ is the time-varying component and r is the correlation parameter, *i.e.*, the AR coefficient of frequency-domain channels experienced by two consecutive OFDM symbols (corresponding to two consecutive discrete time indices), where the time correlation function is defined

$$\rho(\Delta k) \triangleq \frac{\mathbb{E}\left[\sigma_{\ell,c}^*[k]\sigma_{\ell,c}[k+\Delta k]\right]}{\mathbb{E}\left[\left|\sigma_{\ell,c}[k]\right|^2\right]} = r^{\Delta k},\tag{5}$$

with a discrete time-lag $\Delta k \in \mathbb{Z}$.

Consider a representative value of r in an OFDM system. According to [42], [43], and [44], the coherence time interval within which the channel auto-correlation function is above 0.5 is given by

$$T_{\rm c} \triangleq 0.423 \cdot \frac{v_{\rm c}}{v} \cdot \frac{1}{f_{\rm c}},$$
 (6)

where $v \geq 0$ [m/s] denotes the relative velocity between transmitter and receiver, v_c [m/s] denotes the speed of light, and f_c [Hz] denotes the carrier frequency, respectively.

Given that the OFDM system operates with a discrete Fourier transform (DFT) of size $N_{\rm DFT}$ and a sampling rate $f_{\rm s}$ [Hz], the duration of each OFDM symbol is given by [16]

$$T_{\rm s} \triangleq N_{\rm DFT} \cdot \frac{(1 + N_{\rm GI})}{f_{\rm s}} = (1 + N_{\rm GI}) \frac{1}{\Delta f},$$
 (7)

where $N_{\rm GI}$ is the guard interval and $\Delta f \triangleq f_{\rm s}/N_{\rm DFT}$ is the subcarrier spacing [45], [46].¹

From (5)–(7), the maximum number of OFDM symbols within the coherence time is given by $K_{\rm max} \triangleq \lfloor T_{\rm c}/T_{\rm s} \rfloor$, and the time correlation parameter r used in (4) can then be calculated as²

$$r = \exp\left[\frac{\ln(0.5)}{K_{\text{max}}}\right]. \tag{8}$$

From (1) and (4), denoting the number of OFDM symbols during data transmission by $K \leq K_{\max}$, such that the discrete time index $k \in \mathcal{K} \triangleq \{0,1,\ldots,K-1\}$, the aged frequency-domain channel at the k-th discrete time instance can be expressed as [15] and [16]

$$\mathbf{\acute{H}}[k] = \frac{1}{\sqrt{L}} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{\sigma_{\ell,c}[k]}{\sqrt{C_{\ell}}} \mathbf{\acute{A}}_{\ell,c}$$

$$= r^{k'} \mathbf{\acute{H}}[k-k']$$

$$+ \sqrt{\frac{1-r^{2}}{L}} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{\mathbf{\acute{A}}_{\ell,c}}{\sqrt{C_{\ell}}} \sum_{\kappa=0}^{k'-1} r^{\kappa} \omega_{\ell,c}[k-\kappa]$$

$$\stackrel{\triangleq \beta_{\ell,c}(k,k')}{= r^{k} \mathbf{\acute{H}}[0]} + \sqrt{\frac{1-r^{2}}{L}} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{\beta_{\ell,c}(k,k)}{\sqrt{C_{\ell}}} \mathbf{\acute{A}}_{\ell,c}, \quad (9)$$
Errors due to channel aging

where $\hat{\boldsymbol{H}}[0]$ is the initial CSI (estimated from the most recent pilots).

Similarly as in [37], it is assumed that the AoAs and AoDs are constant during the OFDM frame interval, while the channel coefficient may change rapidly. From the Gaussian-PDF multiplication rule [29], the cumulative change in small-scale fading due to channel aging, *i.e.*, $\beta_{\ell,c}(k,k')$, follows a Gaussian distribution with

$$\mathbb{E}\left[\beta_{\ell,c}(k,k')\right] = 0, \tag{10a}$$

$$\mathbb{E}\left[\left|\beta_{\ell,c}(k,k')\right|^2\right] = \mathbb{E}\left[\left|\sum_{\kappa=0}^{k'-1} r^{\kappa} \omega_{\ell,c}[k-\kappa]\right|^2\right]$$

 1 It is assumed that the time variability of channels during $T_{\rm s}$ is negligibly small and that there is no effect of inter-subcarrier interference.

 $^2{\rm The}$ term inside the exponential in equation (8) is always non-positive, since $\ln(0.5)<0$, indicating that the correlation parameter r becomes smaller as $T_{\rm c}$ decreases (v and $f_{\rm c}$ increase) and $T_{\rm s}$ increases (Δf decreases), as intuited. When oversampling is performed, r becomes smaller as expected because $T_{\rm s}$ is inversely proportional to the sampling rate $f_{\rm s}$.

$$= \sum_{\kappa=0}^{k'-1} r^{2\kappa} \underbrace{\mathbb{E}\left[\left|\omega_{\ell,c}[k-\kappa]\right|^{2}\right]}_{=1}$$

$$= \frac{1-r^{2k'}}{1-r^{2}} \triangleq \phi_{\ell,c}^{\beta}(k'). \tag{10b}$$

B. Signal Model

Based on the time-varying mmWave channel model described in the previous subsection, we describe the RX signal model of a point-to-point OFDM-MIMO communication system with a fully-digital TX/RX beamforming architecture. Denoting the TX and RX beamforming matrices respectively by $\boldsymbol{F}_{\mathrm{TX}} \in \mathbb{C}^{N_{\mathrm{TX}} \times M}$ $(M \leq N_{\mathrm{TX}})$ and $\boldsymbol{F}_{\mathrm{RX}} \in \mathbb{C}^{N_{\mathrm{RX}} \times N}$ $(N \leq N_{\mathrm{RX}})$, after cyclic prefix removal and DFT processing at the receiver, the frequency-domain RX vector of the f-th subcarrier at the k-th discrete time instance can be expressed as the following linear regression model

$$\mathbf{y}_{f}[k]$$

$$\triangleq [y_{f,1}[k], \dots, y_{f,n}[k], \dots, y_{f,N}[k]]^{\mathsf{T}}$$

$$= \mathbf{F}_{\mathrm{RX}}^{\mathsf{H}} \mathbf{\acute{H}}_{f}[k] \mathbf{F}_{\mathrm{TX}} \mathbf{x}_{f}[k] + \mathbf{z}_{f}[k] = \mathbf{H}_{f}[k] \mathbf{x}_{f}[k] + \mathbf{z}_{f}[k],$$
(11)

where $\boldsymbol{x}_f[k] \triangleq [x_{f,1}[k], \dots, x_{f,m}[k], \dots, x_{f,M}[k]]^\mathsf{T}$ is a TX vector, $\boldsymbol{H}[k] \triangleq [\boldsymbol{h}_{f,1}[k], \dots, \boldsymbol{h}_{f,m}[k], \dots, \boldsymbol{h}_{f,M}[k]] \triangleq \boldsymbol{F}_{\mathrm{RX}}^\mathsf{H} \boldsymbol{H}_f[k] \boldsymbol{F}_{\mathrm{TX}} \in \mathbb{C}^{N \times M}$ is an effective channel matrix in the beam domain, and $\boldsymbol{z}_f[k] \triangleq [z_{f,1}[k], \dots, z_{f,n}[k], \dots, z_{f,N}[k]]^\mathsf{T} \sim \mathcal{CN}(0, N_0 \boldsymbol{I}_N)$ is an independent and identically distributed (i.i.d.) circularly symmetric additive white Gaussian noise (AWGN) vector. Note that large-scale fading factors such as path-loss between the transmitter and receiver are estimated in advance and their effects are eliminated in (11). Hereafter, we will focus our discussion on a single subcarrier and therefore omit the subcarrier index f for notational simplicity.

In similarity to (9) in Subsection II-A, the effective beam-domain channel can be expressed as

$$\boldsymbol{H}[k] = r^{k'} \boldsymbol{H}[k - k'] + \sqrt{\frac{1 - r^2}{L}} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{\beta_{\ell,c}(k, k')}{\sqrt{C_{\ell}}} \boldsymbol{A}_{\ell,c}$$
$$= r^{k} \boldsymbol{H}[0] + \sqrt{\frac{1 - r^2}{L}} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{\beta_{\ell,c}(k, k)}{\sqrt{C_{\ell}}} \boldsymbol{A}_{\ell,c}, \quad (12)$$

where $\mathbf{A}_{\ell,c} \triangleq \mathbf{F}_{\mathrm{RX}}^{\mathsf{H}} \hat{\mathbf{A}}_{\ell,c} \mathbf{F}_{\mathrm{TX}} \in \mathbb{C}^{N \times M}$ and $\mathbf{h}_{m}[k] \triangleq [h_{1m}[k], \ldots, h_{nm}[k], \ldots, h_{Nm}[k]]^{\mathsf{T}}$. For the sake of readability and future convenience, the second-order statistics of errors due to channel aging are computed based on (12) and summarized in Appendix.

C. Static TX/RX Beamforming Strategy

In practice, mmWave communications using TX/RX beamforming are realized by a two-step process: beam training to form static beams based on predesigned codebook and/or long-term channel statistics, and CT to maintain acceptable communication quality by tracking instantaneous channel variations due to small-scale fading [18], [19], [20], [21], [22].

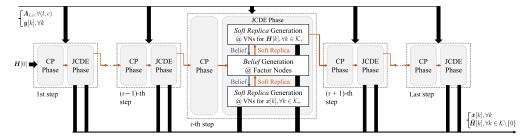


Fig. 1. Schematic of the belief propagation process employed in the proposed bilinear inference algorithm.

In this article, under the assumption that the beam training is conducted ideally, the optimal static digital beamforming is performed based on the singular value decomposition (SVD) of the initial CSI $\acute{H}[0] = U\Sigma V^{\rm H}$ as³

$$F_{\text{TX}} = [V]_{:.1:M}, \quad F_{\text{RX}} = [U]_{:.1:N}.$$
 (13)

If the block fading assumption holds, interference-free SVD-based MIMO communication can be achieved. However, in the presence of channel aging, the equivalent channel matrix after equalization, *i.e.*, $\boldsymbol{H}[k]^{\mathsf{H}}\boldsymbol{H}[k]$, has off-diagonal components for $k \in \mathcal{K} \setminus \{0\}$ due to mismatch between the beam and channel, resulting in non-negligible performance degradation as k increases.

The goal of the article can now be stated concisely: design a novel JCTDD algorithm that enables the receiver to simultaneously detect the intended TX vectors $\boldsymbol{x}[k], \forall k$, and accurately estimate/track the effective channel matrices $\boldsymbol{H}[k], \forall k \in \mathcal{K} \setminus \{0\}$, out of the RX vectors $\boldsymbol{y}[k], \forall k$, given in (11), the initial effective channel matrix $\boldsymbol{H}[0] = \boldsymbol{F}_{\mathrm{RX}}^{\mathsf{H}} \boldsymbol{H}[0] \boldsymbol{F}_{\mathrm{TX}}$ estimated as a result of beam training, and the long-term channel statistics that change only slowly, *i.e.*, $\boldsymbol{A}_{\ell,c}, \forall (\ell,c)$. Unless otherwise specified, the TX/RX beamformers given by (13) shall be used.

III. BAYESIAN JOINT CHANNEL TRACKING AND DATA DETECTION

In this section, a CP-aided message passing algorithm based on the BBI framework to design JCTDD receivers for time-varying mmWave MIMO architectures is described. To capture the time variability of wireless channels due to channel aging, the proposed algorithm has two phases: the CP phase and the JCDE phase. By iterating between these phases alternately, as illustrated in Fig. 1, the unknown data vectors $\boldsymbol{x}[k], \forall k$, and effective channel matrices $\boldsymbol{H}[k], \forall k \in \mathcal{K} \setminus \{0\}$, can be sequentially estimated, given the knowledge of RX vectors $\boldsymbol{y}[k], \forall k$, the known (estimated) effective channel matrix $\boldsymbol{H}[0]$, and the effective array response matrices $\boldsymbol{A}_{\ell,c}, \forall (\ell,c)$, obtained from long-term observation at the receiver.

For later convenience, the basic process consisting of one CP phase and one subsequent JCDE phase is defined as one

 3 In case of hybrid beamforming architectures [47], where analog beamformers perform port reduction based on beam search methods without channel estimation, the SVD is calculated based on the effective channel matrix comprising of the actual channel and the analog beamformer. The proposed method described later is still compatible with such scenarios, since it can track the effective beam-domain channel matrix for a fixed analog beamformer. Notice that the SVD beamformer on $\hat{H}[0]$ as used in this article serves as the upper bound of such analog beam search-based alternatives.

step, and the set of discrete-time indices corresponding to the variables to be estimated in the process of the τ -th step, denoted by $\mathcal{K}_{\tau} \subset \mathcal{K}$, is designed flexibly according to the intended sequential processing. For example, in this problem setting, where the knowledge of H[0] is given, it is reasonable to perform estimation from k=0 to k=K-1 in that order. In addition, since it is assumed that the relative velocity between the transmitter and receiver is constant during the OFDM frame interval, \mathcal{K}_{τ} is generated under a static rule with respect to τ . Following these remarks, the *active* set for each step of the algorithm is given by

$$\mathcal{K}_{\tau} \triangleq \left\{ k \in \mathcal{K} \middle| (\tau - D) W \le k \le \tau W - 1 \right\},$$

$$\forall \tau \in \{1, 2, \dots, \tau_{\text{max}}\},$$
(14)

with $\tau_{\max} = \frac{K}{W} + D - 1$, where $W \in \mathbb{N}$ is the number of new indices added to the active set for each step, while $D \in \mathbb{N}$ is a "window-sliding" parameter that determines the number of variables estimated simultaneously for each step. In view of (14), it will prove convenient to define the set \mathcal{K}_{τ}^+ , with $|\mathcal{K}_{\tau}^+| = \{0, W\}$, of discrete-time indices to be added to the active set between each step. For an intuitive understanding, Table I lists the sets \mathcal{K}_{τ} and \mathcal{K}_{τ}^+ at each step when we set (K, W, D) = (64, 2, 3) as an example.

Let us next shift our focus to each phase at the τ -th step. In the CP phase, the channels estimated in the previous $(\tau - 1)$ -th step are used to generate an initial estimate of channels corresponding to the indices newly added to the active set in the current τ -th step, i.e., $H[k], \forall k \in \mathcal{K}_{\pi}^+$. It is worth noting that these predicted channels are prior estimates that do not include information from the observations at $k \in \mathcal{K}_{\tau}^+$. In turn, in the JCDE phase, estimates of $x[k], \forall k \in \mathcal{K}_{\tau}$, and $H[k], \forall k \in \mathcal{K}_{\tau}$, are computed employing the bilinear Gaussian belief propagation (BiGaBP) approach, using the knowledge of $y[k], \forall k \in \mathcal{K}_{\tau}$, of the predicted channels obtained in the $(\tau - 1)$ -th CP phase, and of the estimates of $x[k], k \in \mathcal{K}_{\tau-1}$, obtained in the $(\tau - 1)$ -th JCDE phase. However, only the DD mechanism is based on the probabilistic data association (PDA) approach [48], which suppresses the interference using inverse matrices while taking into account the spatial correlation among fading coefficients.

The bilinear inference in the JCDE phase is performed by exchanging *beliefs* (*i.e.*, likelihood information reflecting detection reliability) and *soft replicas* (*i.e.*, tentative estimates) on the tripartite FG consisting of factor nodes (FNs) and two variable nodes (VNs), which correspond to the channel

 ${\it TABLE~I}$ Examples of ${\cal K}_{\tau}$ and ${\cal K}_{\tau}^+$ for the Case of (K,W,D)=(64,2,3)

τ	$\mathcal{K}_{ au}$	$\mathcal{K}_{ au}^{+}$	τ	$\mathcal{K}_{ au}$	\mathcal{K}_{τ}^{+}
1	{0,1}	{0,1}	:	:	:
2	{0,1,2,3}	{2,3}	30	{54, 55, 56, 57, 58, 59}	{58, 59}
3	{0,1,2,3,4,5}	$\{4, 5\}$	31	{56, 57, 58, 59, 60, 61}	{60,61}
4	{2,3,4,5,6,7}	{6,7}	32	{58, 59, 60, 61, 62, 63}	{62,63}
5	{4,5,6,7,8,9}	{8,9}	33	{60, 61, 62, 63}	Ø
:	:	:	34	{62,63}	Ø

coefficients and TX data symbols, respectively. We remark that although the algorithm of the JCDE phase is designed based on the existing BiGaBP [33] and PDA approaches [48], both the belief generation in the FNs, which incorporate a new prediction mechanism to capture the time variation of channels and the resulting message aggregation mechanism, and the derivation of the resulting posterior probabilities are novel contributions of this article.

In what follows, we provide detailed descriptions of the CP and JCDE phases of the proposed technique briefly explained above.

Let us define the soft replicas of $x_m[k]$ and $h_{nm}[k]$ as \hat{x}_{mk} and $\hat{h}_{k,nm}$, respectively, such that their MSEs can be respectively expressed as

$$\hat{\psi}_{mk}^{\mathbf{x}} \triangleq \mathbb{E}\left[\left|\tilde{x}_{mk}\right|^{2}\right], \text{ with } \tilde{x}_{mk} \triangleq x_{m}[k] - \hat{x}_{mk}, \tag{15a}$$

$$\hat{\psi}_{k,nm}^{\mathbf{h}} \triangleq \mathbb{E}\left[\left|\tilde{h}_{k,nm}\right|^{2}\right], \text{ with } \tilde{h}_{k,nm} \triangleq h_{nm}[k] - \hat{h}_{k,nm}, \tag{15b}$$

where the quantities \tilde{x}_{mk} and $\tilde{h}_{k,nm}$ denote the estimation errors, respectively.

Denoting the soft replicas of $h_m[k]$ and H[k] by $\hat{h}_{k,m} \triangleq \left[\hat{h}_{k,1m}, \dots, \hat{h}_{k,nm}, \dots, \hat{h}_{k,Nm}\right]^\mathsf{T}$ and $\hat{H}_k \triangleq \left[\hat{h}_{k,1}, \dots, \hat{h}_{k,m}, \dots, \hat{h}_{k,M}\right] \in \mathbb{C}^{N \times M}$, respectively, in similarity to the above, their corresponding error covariance matrices can be expressed as

$$\hat{\boldsymbol{\varPsi}}_{k,m}^{\mathrm{h}} \triangleq \mathbb{E}\left[\tilde{\boldsymbol{h}}_{k,m}\tilde{\boldsymbol{h}}_{k,m}^{\mathsf{H}}\right] \in \mathbb{C}^{N \times N}, \text{ with } \tilde{\boldsymbol{h}}_{k,m} \triangleq \boldsymbol{h}_{m}[k] - \hat{\boldsymbol{h}}_{k,m}, \tag{16a}$$

$$\hat{\boldsymbol{\varPsi}}_{k}^{\mathrm{h}} \triangleq \mathbb{E}\left[\tilde{\boldsymbol{H}}_{k}\tilde{\boldsymbol{H}}_{k}^{\mathsf{H}}\right] \in \mathbb{C}^{N \times N}, \text{ with } \tilde{\boldsymbol{H}}_{k} \triangleq \boldsymbol{H}[k] - \hat{\boldsymbol{H}}_{k}. \tag{16b}$$

For simplicity, we assume that quadrature phase-shift keying (QPSK) modulation with unit power is employed, where the constellation is expressed as $\mathcal{X} = \left\{ \pm \frac{1}{\sqrt{2}} \pm j \frac{1}{\sqrt{2}} \right\}$.

A. CP Phase

Let us start with the CP phase, which uses (12) describing channel state transitions to generate the prior estimates (i.e., initial soft replicas used in the subsequent JCDE phase) of $\boldsymbol{H}[k], \forall k \in \mathcal{K}_{\tau}$. Since soft replicas are not available at the first step ($\tau = 1$), the initial conditional expectation of $\boldsymbol{H}[k]$,

given H[0], is calculated via (12) as⁴

$$\hat{\boldsymbol{H}}_{k} = \mathbb{E}_{\mathbf{H}[k]|\mathbf{H}[0]} \left[\boldsymbol{H}[k] \middle| \boldsymbol{H}[0] \right] = r^{k} \boldsymbol{H}[0], \tag{17}$$

where its corresponding second-order statistics can be obtained from (44) in Appendix as

$$\hat{\boldsymbol{\varPsi}}_{k}^{\mathrm{h}} = \mathbb{E}_{\mathbf{H}[k]|\mathbf{H}[0]} \left[\boldsymbol{H}[k]\boldsymbol{H}[k]^{\mathsf{H}} \middle| \boldsymbol{H}[0] \right] = \boldsymbol{\Omega}_{k} \in \mathbb{C}^{N \times N},$$
(18a)

$$\hat{\boldsymbol{\varPsi}}_{k,m}^{\mathrm{h}} = \mathbb{E}_{\mathbf{h}_{m}[k]|\mathbf{h}_{m}[0]} \left[\boldsymbol{h}_{m}[k]\boldsymbol{h}_{m}[k]^{\mathsf{H}} \middle| \boldsymbol{h}_{m}[0] \right] = \boldsymbol{\Omega}_{k,m} \in \mathbb{C}^{N \times N},$$
(18b)

$$\psi_{k,nm}^{h} = \mathbb{E}_{\mathsf{h}_{nm}[k]|\mathsf{h}_{nm}[0]} \left[|h_{nm}[k]|^2 \left| h_{nm}[0] \right] = \omega_{k,nm}.$$
(18c)

Owing to the availability of soft replicas as prior information at the second and subsequent steps $(\tau \neq 1)$, the conditional expectation of H[k] can thereafter be obtained as

$$\hat{\boldsymbol{H}}_{k} = \mathbb{E}_{\mathbf{H}[k]|\mathbf{H}[0], \hat{\mathbf{H}}_{k}, \forall k \in \check{\mathcal{K}}_{\tau-1}} \left[\boldsymbol{H}[k] \middle| \boldsymbol{H}[0], \hat{\boldsymbol{H}}_{k}, \forall k \in \check{\mathcal{K}}_{\tau-1} \right]
\approx \mathbb{E}_{\mathbf{H}[k]|\hat{\mathbf{H}}_{k}, \forall k \in \mathcal{K}_{\tau-1}} \left[\boldsymbol{H}[k] \middle| \hat{\boldsymbol{H}}_{k}, \forall k \in \mathcal{K}_{\tau-1} \right]$$

$$\approx \mathbb{E}_{\mathbf{H}[k]|\hat{\mathbf{H}}_{|\check{\mathcal{K}}_{\tau-1}|-1}} \left[\boldsymbol{H}[k] \middle| \hat{\boldsymbol{H}}_{|\check{\mathcal{K}}_{\tau-1}|-1} \right],$$
(19b)

where for simplicity we have denoted $\check{\mathcal{K}}_{\tau} \triangleq \bigcup_{i=1}^{\tau} \mathcal{K}_{\tau}$. Since all estimates are computed based on the previous estimates and H[0], the given knowledge is not independent of each other. Therefore, if the sequential estimation process works well based on the Bayes-optimal inference framework, it is sufficient to use as prior information only the estimates obtained in the immediately previous step, as in (19a). In addition, as will be explained later in the JCDE phase, $\hat{H}_k, \forall k \in \mathcal{K}_{\tau-1}$, is generated using all knowledge of $y[k], \forall k \in \mathcal{K}_{\tau-1}$, so in theory, we can create $\hat{\boldsymbol{H}}_k$ from any appropriate estimate contained in $\mathcal{K}_{\tau-1}$, e.g., the latest estimated channel $H_{|\check{\mathcal{K}}_{\tau-1}|-1}$, as in (19b). However, the JCDE algorithm is sub-optimal; hence, the reliability of H_k varies randomly for each k, depending on the convergence behavior of iterative estimation, and thus the low accuracy of the selected estimate may induce serious performance degradation due to error propagation.

To alleviate this inconvenience, we employ a simple criterion to select as prior information the estimate with the minimum MSE among the estimates used in the τ -th step, as follows:

$$k_{\tau} = \underset{\underline{k} \in \mathcal{K}_{\tau} \setminus \mathcal{K}_{\tau}^{+}}{\operatorname{argmin}} \sum_{m=1}^{N} \sum_{m=1}^{M} \hat{\psi}_{\underline{k},nm}^{h}, \tag{20}$$

$$\hat{\boldsymbol{H}}_{k} = \mathbb{E}_{\mathbf{H}[k]|\hat{\mathbf{H}}_{k_{\tau}}} \left[\boldsymbol{H}[k] \middle| \hat{\boldsymbol{H}}_{k_{\tau}} \right] = r^{k-k_{\tau}} \hat{\boldsymbol{H}}_{k_{\tau}}, \ \forall k \in \mathcal{K}_{\tau}^{>k_{\tau}},$$
(21)

where $\mathcal{K}_{\tau}^{>k_{\tau}} \triangleq \{k \in \mathcal{K}_{\tau} | k > k_{\tau}\}$, and its second-order statistics can be obtained from (15b), (16), and (44) as

$$\hat{\boldsymbol{\varPsi}}_{k}^{\mathrm{h}} = \mathbb{E}_{\mathbf{H}[k]|\hat{\mathbf{H}}_{k_{\tau}}} \left[\boldsymbol{H}[k]\boldsymbol{H}[k]^{\mathsf{H}} \middle| \hat{\boldsymbol{H}}_{k_{\tau}} \right]$$

 $^4\mathrm{In}$ order to avoid being repetitive, we hereafter omit the qualifier "\$\forall k \in \mathcal{K}_{\tau}\$" when obvious.

$$= r^{2(k-k_{\tau})} \hat{\boldsymbol{\Psi}}_{k_{\tau}}^{h} + \boldsymbol{\Omega}_{k-k_{\tau}}, \qquad (22a)$$

$$\hat{\boldsymbol{\Psi}}_{k,m}^{h} = \mathbb{E}_{\mathbf{h}_{m}[k]|\hat{\mathbf{h}}_{k_{\tau},m}} \left[\boldsymbol{h}_{m}[k]\boldsymbol{h}_{m}[k]^{\mathsf{H}} \middle| \hat{\boldsymbol{h}}_{k_{\tau},m} \right]$$

$$= r^{2(k-k_{\tau})} \hat{\boldsymbol{\Psi}}_{k_{\tau},m}^{h} + \boldsymbol{\Omega}_{k-k_{\tau},m}, \qquad (22b)$$

$$\psi_{k,nm}^{h} = \mathbb{E}_{\mathsf{h}_{nm}[k]|\hat{\mathsf{h}}_{k_{\tau},nm}} \left[|h_{nm}[k]|^{2} \left| \hat{h}_{k_{\tau},nm} \right] \right]$$

$$= r^{2(k-k_{\tau})} \hat{\psi}_{k_{\tau},m}^{h} + \omega_{k-k_{\tau},nm}. \tag{22c}$$

In the above, a single CP phase is described. For the discrete-time indices that were included in the active set $\mathcal{K}_{\tau-1}$ and were not updated in the τ -th CP phase, the soft replicas obtained at the $\tau-1$ step is used as the prior estimate as they are.

B. JCDE Phase

Herein, the JCDE algorithm for estimating $x_m[k]$ and $h_{nm}[k]$ is focused upon. Note that the following process is performed on the RX symbols $y_n[k], \forall n \in \mathcal{N} \triangleq \{1,2,\ldots,N\}, \forall k \in \mathcal{K}_{\tau},$ in parallel to estimate all TX symbols $x_m[k], \forall m \in \mathcal{M} \triangleq \{1,2,\ldots,M\}, \forall k \in \mathcal{K}_{\tau},$ and channel coefficients $h_{nm}[k], \forall (n,m), \forall k \in \mathcal{K}_{\tau},$ simultaneously. In the sequel, we refrain from explicitly including the qualifier " $\forall k \in \mathcal{K}_{\tau}$ " after each equation, in order to avoid being repetitive.

1) FN Process for DD: The iterative process, which is carried out for the RX vector, starts at the FNs with soft interference cancellation (soft IC) performed on y[k] with utilizing all the soft replicas obtained in the previous JCDE iteration $(t \neq 1)$. At the first iteration (t = 1), the soft replicas $\hat{x}_{mk}, \forall k \in \mathcal{K}_{\tau}$, are appropriately initialized, e.g., $\hat{x}_{mk} = 0, \forall k \in \mathcal{K}_{\tau}$, and $\hat{h}_{k,nm}, \forall k \in \mathcal{K}_{\tau}$, are obtained in the CP phase. In the detection of an arbitrary TX symbol $x_m[k]$, the cancellation process is expressed as (23), shown at the bottom of the next page. The residual interference-plus-noise component of (23) can be approximated as a multivariate complex Gaussian random vector; this approximation is referred to as vector Gaussian approximation (VGA) [49]. Thus, the conditional PDF of (23), given $x_m[k]$, can be expressed as

$$p_{\tilde{\mathbf{y}}_{m,k}|\mathbf{x}_{m}[k]}\left(\tilde{\mathbf{y}}_{m,k}|x_{m}[k]\right) \\ \propto \exp\left[-\left(\tilde{\mathbf{y}}_{m,k}-\hat{\mathbf{h}}_{k,m}x_{m}[k]\right)^{\mathsf{H}} \boldsymbol{\Xi}_{k,m}^{-1}\left(\tilde{\mathbf{y}}_{m,k}-\hat{\mathbf{h}}_{k,m}x_{m}[k]\right)\right], \tag{24}$$

with

$$\boldsymbol{\Xi}_{m,k} \triangleq \mathbb{E}\left[\boldsymbol{\kappa}_{k,m}^{\mathbf{x}} \left(\boldsymbol{\kappa}_{k,m}^{\mathbf{x}}\right)^{\mathsf{H}}\right]$$

$$= \underbrace{\sum_{m=1}^{M} \hat{\psi}_{mk}^{\mathbf{x}} \hat{\boldsymbol{h}}_{k,m} \hat{\boldsymbol{h}}_{k,m}^{\mathsf{H}} + \hat{\boldsymbol{\Psi}}_{k}^{\mathsf{h}} + N_{0} \boldsymbol{I}_{N} - \hat{\psi}_{mk}^{\mathbf{x}} \hat{\boldsymbol{h}}_{k,m} \hat{\boldsymbol{h}}_{k,m}^{\mathsf{H}}.$$

$$\triangleq \boldsymbol{\Xi}_{k} \in \mathbb{C}^{N \times N}$$
(25)

2) VN Process for DD: From (24), the beliefs corresponding to $x_m[k]$ are combined over all RX antenna indices via linear minimum mean square error (MMSE) filters, which results in the PDF of a joint belief $l_{mk}^{\mathbf{x}}$ for $x_m[k]$. This is expressed as

$$p_{\mathsf{l}_{mk}^{\mathsf{x}}|\mathsf{x}_{m}[k]}\left(l_{mk}^{\mathsf{x}}|x_{m}[k]\right) = p_{\tilde{\mathbf{y}}_{m,k}|\mathsf{x}_{m}[k]}\left(\tilde{\boldsymbol{y}}_{m,k}|x_{m}[k]\right)$$

TABLE II $\begin{tabular}{ll} {\sf EXAMPLES} \mbox{ of } \mathcal{S}_{k,\tau} \mbox{ for the Case of } \\ (W,D,G)=(2,3,6), \mbox{ Where } K=8 \end{tabular}$

τ	0	1	2	3	4	5	6	7
1	{1}	{0}	-	-	-	-	-	-
2	$\{1, 2, 3\}$	$\{0, 2, 3\}$	{0,1,3}	$\{0, 1, 2\}$	-	-	-	-
3	{1,2,3}	$\{0, 2, 3, 4\}$	$\{0, 1, 3, 4, 5\}$	{0, 1, 2, 4, 5}	$\{1, 2, 3, 5\}$	$\{2, 3, 4\}$	-	-
4	-	-	$\{0,1,3,4,5\}$	$\{0, 1, 2, 4, 5\}$	{1, 2, 3, 5, 6, 7}	$\{2, 3, 4, 6, 7\}$	{3, 4, 5, 7}	$\{4, 5, 6\}$
5	-	-	-	-	$\{1, 2, 3, 5, 6, 7\}$	$\{2, 3, 4, 6, 7\}$	$\{3, 4, 5, 7\}$	$\{4, 5, 6\}$
- 6	-	-	-	-	-	-	{3, 4, 5, 7}	{4,5,6}

$$\propto \exp\left[-\frac{\left|x_m[k] - \overline{x}_{mk}\right|^2}{\overline{\psi}_{mk}^{\mathsf{x}}}\right],$$
 (26)

where $\overline{x}_{mk} = \frac{1}{\eta_{mk}} \hat{\boldsymbol{h}}_{k,m}^{\mathsf{H}} \boldsymbol{\Xi}_k^{-1} \tilde{\boldsymbol{y}}_{m,k}, \ \overline{\psi}_{mk}^{\mathsf{x}} = \frac{1 - \eta_{mk} \hat{\psi}_{mk}^{\mathsf{x}}}{\eta_{mk}}$, and $\eta_{mk} = \hat{\boldsymbol{h}}_m^{\mathsf{H}} \boldsymbol{\Xi}_k^{-1} \hat{\boldsymbol{h}}_m$, which are derived by applying the matrix inversion lemma to eliminate the dependency of $\boldsymbol{\Xi}_{m,k}$ in (24) on the index $m \in \mathcal{M}$, enabling us to share the same inverse matrix $\boldsymbol{\Xi}_k^{-1}$ for $\forall m$ [50].

Assuming that the effective noise components in l_{mk}^{\times} , $\forall (m,k)$, are not correlated to each other under VGA, using Bayes' rule, the soft replica of $x_m[k]$ and its MSE can be in general obtained from the symbol-wise conditional expectation, given l_{mk}^{\times} , as

$$\hat{x}_{mk} = \sum_{\chi \in \mathcal{X}} \frac{\chi \cdot p_{|_{mk}^{\times}|\times_{m[k]}}(l_{mk}^{\times}|\chi) \, p_{\times_{m[k]}}(\chi)}{\sum_{\chi' \in \mathcal{X}} p_{|_{mk}^{\times}|\times_{m[k]}}(l_{mk}^{\times}|\chi') \, p_{\times_{m[k]}}(\chi')}, \tag{27a}$$

$$\hat{\psi}_{mk}^{x} = \sum_{\chi \in \mathcal{X}} \frac{\left| \chi - \hat{x}_{mk} \right|^{2} \cdot p_{l_{mk}^{x} | x_{m}[k]} \left(l_{mk}^{x} | \chi \right) p_{x_{m}[k]} \left(\chi \right)}{\sum_{\chi' \in \mathcal{X}} p_{l_{mk}^{x} | x_{m}[k]} \left(l_{mk}^{x} | \chi' \right) p_{x_{m}[k]} \left(\chi' \right)},$$
(27b)

where the denominator in the integrand is introduced for normalization purposes.

In Gray-coded QPSK signaling with unit power, (27) can be readily obtained by the following *denoiser* as [51]

$$\hat{x}_{mk} = \frac{1}{\sqrt{2}} \cdot \left(\tanh \left[\frac{\sqrt{2} \Re\{\overline{x}_{mk}\}}{\overline{\psi}_{mk}^{x}} \right] + j \tanh \left[\frac{\sqrt{2} \Im\{\overline{x}_{mk}\}}{\overline{\psi}_{mk}^{x}} \right] \right),$$
(28a)

$$\hat{\psi}_{mk}^{\mathbf{x}} = 1 - \left| \hat{x}_{mk} \right|^2. \tag{28b}$$

3) FN Process for CE: In the CE process, it is necessary to perform belief combining across the discrete-time dimension; however, since the channels vary with respect to k, the conventional belief consensus mechanism does not work well, which results in significant loss of diversity gain. Therefore, it is essential to perform state transitions using (12) in the belief domain as well. Furthermore, it is effective to restrict the beliefs to be combined to those generated based on discrete-time observations close to the index k to be estimated.

In this article, a set of discrete-time indices of the beliefs to be combined when estimating the entries of H[k] at the τ -th step is given by the vicinity of k as

$$\mathcal{S}_{k,\tau} \triangleq \left\{ s \in \check{\mathcal{K}}_{\tau} \setminus \{k\} \left| k - \frac{G}{2} \le k \le k + \frac{G}{2} \right. \right\},$$
 (29)

where G is the number of beliefs to be combined and should be even. Table II lists the sets $S_{k,\tau}$ for each k when we set to (W, D, G) = (2, 3, 6), with K = 8, as an example.

In what follows, we provide detailed descriptions of the estimation of an arbitrary $h_{nm}[k]$. Let us start with the soft IC on $y_n[s], \forall s \in \mathcal{S}_{k,\tau}$, with the aid of soft replicas, yields (30), shown at the bottom of the next page. Here, we note that the statistical property of beliefs propagated from past discrete times and those propagated from future discrete times are different, so that we apply state transitions to the channel coefficients in (30) to extract the information of $h_{nm}[k]$. For the beliefs with the discrete-time index s < k, using (12), (30) can be rewritten as

$$\tilde{y}_{s,nm} = \left(r^{s-k}h_{nm}[k] - r^{s-k}\zeta_{s\to k,nm}^{h}\right)\hat{x}_{ms} + \kappa_{s,nm}^{h},$$
(31a)

$$r^{k-s}\tilde{y}_{s,nm} = h_{nm}[k]\hat{x}_{ms} - \zeta_{s\to k,nm}^{h}\hat{x}_{ms} + r^{k-s}\kappa_{s,nm}^{h},$$
(31b)

where we define the errors due to channel aging as

$$\zeta_{s \to k, nm}^{\text{h}} \triangleq \sqrt{\frac{1 - r^2}{L}} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{[\mathbf{A}_{\ell, c}]_{n, m}}{\sqrt{C_{\ell}}} \beta_{\ell, c}(k, k - s).$$
(32)

Assuming that the scalar Gaussian approximation (SGA) [49] can be applied, namely, that the effective noise component of (31b) – which includes errors due to channel aging, residual interference, and AWGN – can be approximated as a complex scalar Gaussian random variable, the conditional PDF of (31b), given $h_{nm}[k]$, can be expressed with (33), shown at the bottom of the next page, as

$$p_{r^{k-s}\tilde{\mathbf{y}}_{s,nm}|\mathbf{h}_{nm}[k]}\left(r^{k-s}\tilde{\mathbf{y}}_{s,nm}|h_{nm}[k]\right)$$

$$\propto \exp\left[-\frac{\left|r^{k-s}\tilde{\mathbf{y}}_{s,nm}-h_{nm}[k]\hat{x}_{ms}\right|^{2}}{\nu_{s\to k,nm}^{h}}\right], \quad (34)$$

where the instantaneous channel gain $|h_{nm}[s]|^2$ is not available, and therefore is here approximated by the true variance, *i.e.*,

$$\theta_{nm} \triangleq \mathbb{E}\left[|h_{nm}[s]|^2\right] = \frac{1}{L} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{\left|[A_{\ell,c}]_{n,m}\right|^2}{C_{\ell}}.$$
 (35)

In a similar manner, for the beliefs with s > k, (31) can be rewritten as

$$\tilde{y}_{s,nm} = \left(r^{s-k}h_{nm}[k] + \underbrace{\sqrt{\frac{1-r^2}{L}} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{[\boldsymbol{A}_{\ell,c}]_{nm}}{\sqrt{C_{\ell}}} \beta_{\ell,c}(s,s-k)}\right) \hat{x}_{ms} + \kappa_{s,nm}^{h},$$

$$= \zeta_{s \to k,nm}^{h} \tag{36a}$$

$$r^{k-s}\tilde{y}_{s,nm}$$

= $h_{nm}[k]\hat{x}_{ms} + r^{k-s}\zeta^{h}_{s\to k,nm}\hat{x}_{ms} + r^{k-s}\kappa^{h}_{s,nm}$. (36b)

It follows that the conditional PDF of (36b), given $h_{nm}[k]$, can be expressed as

$$p_{r^{k-s}\tilde{\mathbf{y}}_{s,nm}|\mathbf{h}_{nm}[k]}\left(r^{k-s}\tilde{\mathbf{y}}_{s,nm}|h_{nm}[k]\right)$$

$$\propto \exp\left[-\frac{\left|r^{k-s}\tilde{\mathbf{y}}_{s,nm}-h_{nm}[k]\hat{x}_{ms}\right|^{2}}{\nu_{s\rightarrow k,nm}^{\mathrm{h}}}\right], \quad (37)$$

with

$$\nu_{s \to k, nm}^{h} = \mathbb{E} \left\{ \left| r^{k-s} \zeta_{s \to k, nm}^{h} \hat{x}_{ms} + r^{k-s} \kappa_{s, nm}^{h} \right|^{2} \right\}$$

$$= r^{2(k-s)} \left(\omega_{s-k, nm} \left| \hat{x}_{ms} \right|^{2} + \nu_{s, nm}^{h} \right). \quad (38)$$

4) VN Process for CE: Again, assuming that a high-precision SGA of the effective noise components among $\tilde{y}_{s,nm}, \forall s \in \mathcal{S}_{k,\tau}$, can be used, the beliefs corresponding to $h_{nm}[k]$ are combined over $\forall s \in \mathcal{S}_{k,\tau}$, which results in the PDF of an extrinsic belief $l_{k,nm}^{\rm h}$, given $h_{nm}[k]$, yielding

$$p_{|\mathbf{h}_{k,nm}||\mathbf{h}_{nm}[k]}(l_{k,nm}^{\mathbf{h}}|h_{nm}[k])$$

$$= \prod_{s \in \mathcal{S}_{k,\tau}} p_{r^{k-s}\tilde{\mathbf{y}}_{s,nm}||\mathbf{h}_{nm}[k]|}(r^{k-s}\tilde{\mathbf{y}}_{s,nm}|h_{nm}[k])$$

$$\propto \exp\left[-\frac{|h_{nm}[k] - \overline{h}_{k,nm}|^{2}}{\overline{\psi}_{k,nm}^{\mathbf{h}}}\right], \tag{39}$$

with

$$\overline{h}_{k,nm} = \overline{\psi}_{k,nm}^{h} \sum_{s \in \mathcal{S}_{k,\tau}} \frac{\hat{x}_{mi}^* r^{k-s} \tilde{y}_{s,nm}}{\nu_{s \to k,nm}^{h}}, \tag{40a}$$

$$\overline{\psi}_{k,nm}^{h} = \left(\sum_{s \in S_{k,\tau}} \frac{|\hat{x}_{ms}|^2}{\nu_{s \to k,nm}^k}\right)^{-1}, \tag{40b}$$

where we define $\overline{h}_{k,m} \triangleq [\overline{h}_{k,1m},\ldots,\overline{h}_{k,Nm}]^{\mathsf{T}}$ and $\overline{\Psi}_{k,m}^{\mathsf{h}} \triangleq \mathrm{diag}\left[\overline{\psi}_{k,1m}^{\mathsf{h}},\ldots,\overline{\psi}_{k,Nm}^{\mathsf{h}}\right]$, respectively.

The extrinsic combining operation in (39) enables significant suppression of the harmful effect of self-feedback from the previous iteration, by removing the beliefs of $\tilde{y}_{k,nm}$ from $l_{n,mk}^{\rm h}$. Assuming that the effective noise components in $l_{k,nm}^{\rm h}, \forall n$, are not correlated to each other under the SGA, the soft replica of $h_m[k]$ can be in general obtained from the vector-wise conditional expectation, given $l_{k,nm}^{\rm h}, \forall n$, as

$$\hat{\boldsymbol{h}}_{k,m} = \frac{\int_{\boldsymbol{h}_{m}[k]} \boldsymbol{h}_{m}[k] \prod_{i=1}^{N} p_{\mathbf{l}_{k,im}^{h}|\mathbf{h}_{im}[k]} \left(l_{k,im}^{h}|h_{im}[k] \right) p_{\mathbf{h}_{m}[k]} \left(\boldsymbol{h}_{m}[k] \right)}{\int_{\boldsymbol{h}_{m}'[k]} \prod_{i=1}^{N} p_{\mathbf{l}_{k,im}^{h}|\mathbf{h}_{im}[k]} \left(l_{k,im}^{h}|h_{im}'[k] \right) p_{\mathbf{h}_{m}[k]} \left(\boldsymbol{h}_{m}'[k] \right)}$$
(41)

$$\tilde{\boldsymbol{y}}_{m,k} = \boldsymbol{y}[k] - \sum_{i \neq m}^{M} \hat{\boldsymbol{h}}_{k,i} \hat{\boldsymbol{x}}_{ik} = \hat{\boldsymbol{h}}_{k,m} \boldsymbol{x}_{m}[k] + \underbrace{\tilde{\boldsymbol{h}}_{k,m} \boldsymbol{x}_{m}[k] + \sum_{i \neq m}^{M} \left(\boldsymbol{h}_{i}[k] \boldsymbol{x}_{i}[k] - \hat{\boldsymbol{h}}_{k,i} \hat{\boldsymbol{x}}_{ik}\right) + \boldsymbol{z}[k]}_{(23)}$$

Using the multiplication rule [29] in (41), with $\boldsymbol{h}_m[k] \sim \mathcal{CN}(r^k\boldsymbol{h}_m[0],\boldsymbol{\Omega}_{k,m}), \forall k$, yields

$$\hat{\boldsymbol{h}}_{k,m} = C \int_{\boldsymbol{h}_{m}[k]} \boldsymbol{h}_{m}[k] \, \mathcal{C} \mathcal{N} \left(\boldsymbol{h}_{m}[k]; \right. \\
\left. \boldsymbol{\Omega}_{k,m} \boldsymbol{\Lambda}_{k,m}^{-1} \overline{\boldsymbol{h}}_{k,m} + r^{k} \overline{\boldsymbol{\Psi}}_{k,m}^{\mathrm{h}} \boldsymbol{\Lambda}_{k,m}^{-1} \boldsymbol{h}_{m}[0], \boldsymbol{\Omega}_{k,m} \boldsymbol{\Lambda}_{k,m}^{-1} \overline{\boldsymbol{\Psi}}_{k,m}^{\mathrm{h}} \right), \tag{42}$$

where $\Lambda_{k,m} \triangleq \Omega_{k,m} + \overline{\Psi}_{k,m}^{\mathrm{h}} \in \mathbb{C}^{N \times N}$, and C is Pearl's normalization constant. From (42), the soft replica of $h_m[k]$ and its MSE are respectively expressed as

$$\hat{\boldsymbol{h}}_{k,m} = \boldsymbol{\Omega}_{k,m} \boldsymbol{\Lambda}_{k,m}^{-1} \overline{\boldsymbol{h}}_{k,m} + r^k \overline{\boldsymbol{\Psi}}_{k,m}^{\mathrm{h}} \boldsymbol{\Lambda}_{k,m}^{-1} \boldsymbol{h}_m[0], \quad (43a)$$

$$\hat{\underline{\boldsymbol{\Psi}}}_{k,m}^{\mathrm{h}} = \boldsymbol{\Omega}_{k,m} \boldsymbol{\Lambda}_{k,m}^{-1} \overline{\underline{\boldsymbol{\Psi}}}_{k,m}^{\mathrm{h}}. \tag{43b}$$

When the number of iterations reaches the predetermined value, one JCDE phase is completed.

C. Algorithm Description

The pseudo-code of the proposed JCTDD algorithm described above is given in Algorithms 1-3. Besides the RX signal vectors $y[k], \forall k$, and the estimated initial effective channel matrix H[0], the algorithm requires only system parameters such as $A_{\ell,c}$, $\forall (l,c)$, the correlation parameter r, the noise spectral density N_0 , the predetermined parameters $\{W, D, G\}$, and the maximum number of iterations in the JCDE phase $t_{\rm max}$, outputting the hard-decision estimates of the TX symbols $\check{x}_m[k], \forall (k, m)$, and the estimates of the channels $H[k], \forall k$. The proposed JCTDD algorithm tracks the channel in order to aid the DD, indicating that it can be seen as an advanced DD algorithm. Besides, the inputs required for the proposed algorithm are the same as the conventional linear MMSE receiver. No additional control signaling is required to perform the proposed method; therefore, to the best of our knowledge, there is no increase in signaling overhead due to the proposed receiver and no changes to higher-level functions or protocols are required. Notice that lines 7 and 23 in Algorithm 3 correspond to a well-known belief damping procedure [33], [49], which aims to avoid the iterative estimation being trapped at a local optimum, especially at the early stage of the iterations by allowing an inertial update of the quantities \hat{x}_{mk} , $\hat{\psi}_{mk}^{x}$, $\hat{h}_{k,m}$, and $\hat{\boldsymbol{\Psi}}_{k,m}^{h}$. This is due to the fact that at the early stage of the iterative process, the Gaussian approximation assumed in (24), (34), and (37) may not capture the actual statistics of the effective noise, which might lead to convergence to a local optimum point [52].

Even if the communication environment changes, the proposed algorithm can be applied as-is if the input covariance matrices contain appropriate statistical information. For instance, it can be implemented as-is regardless of the operating frequency band (although further algorithmic improvements can be made in case of sub-6GHz bands since the current proposed method is tailored for mmWave bands).⁵

One may have already noticed, the proposed algorithm can be interpreted as a natural extension of the KF mechanism to the BBI framework, while approximating the channel aging interference component as white Gaussian noise. However, a method that repeats prediction and update phases every discrete time step (i.e., W = D = 1), as in the classical KF, cannot achieve highly accurate CE/CT, which requires diversity combining in the discrete-time dimension. The proposed method solves the latter problem by employing a "windowsliding" strategy in which each step is processed in time blocks of size $W \times D$. In addition, by setting D > 1, the scheme takes advantage of past estimates, mitigating the inherent instability of initial convergence of the JCDE algorithm. It is also worth mentioning that the harmful effect of channel aging caused by the extension to block-wise processing is suppressed by incorporating the transition model into the belief update rules in (31) and (36), and as a final remark, we emphasize that although we derived the JCTDD algorithm as a pure DD scheme based on the knowledge of the estimated channel H[0]in this article, the approach can also be directly applied to systems that track time variations in the channel by transmitting pilot symbols with short periods. By assigning the pilot symbols to $\hat{x}_{mk}, \forall (k \in \mathcal{K}_p, m)$, and 0 to the corresponding

 5 Similarly, the proposed algorithm can be applied to multi-user scenarios. Of course, large-fading factors (*e.g.* path-loss) and TX power for each user must be estimated in the beam training step or earlier preprocessing. However, if these effects are embedded in the effective channel matrix $\boldsymbol{H}_f[k]$ in (11) and reflected in the corresponding covariance matrices, there is no need to change the structure of the algorithm. Note that the time correlation parameter r becomes a variable that depends on the user index, some trivial mathematical manipulations must be added in the message update formula accordingly.

$$\tilde{y}_{s,nm} = y_n[s] - \sum_{i \neq m}^{M} \hat{h}_{s,ni} \hat{x}_{is} = h_{nm}[s] \hat{x}_{ms} + h_{nm}[s] \tilde{x}_{ms} + \sum_{i \neq m}^{M} \left(h_{ni}[s] x_i[s] - \hat{h}_{s,ni} \hat{x}_{is} \right) + z_n[s]$$

$$= \sum_{i \neq m} \hat{h}_{s,ni} \hat{x}_{is} + \sum_{i \neq m} \hat{h}_{s,ni} \hat{x}_$$

$$\nu_{s\to k,nm}^{h} = \mathbb{E}\left[\left|-\zeta_{s\to k,nm}^{h}\hat{x}_{ms} + r^{k-s}\kappa_{s,nm}^{h}\right|^{2}\right]$$

$$= \omega_{k-s,nm}\left|\hat{x}_{ms}\right|^{2} + r^{2(k-s)}\underbrace{\left[\sum_{i\neq m}^{M}\left\{\left|\hat{h}_{s,ni}\right|^{2}\hat{\psi}_{is}^{x} + \left(\left|\hat{x}_{is}\right|^{2} + \hat{\psi}_{is}^{x}\right)\hat{\psi}_{s,ni}^{h}\right\} + \theta_{nm}\hat{\psi}_{ms}^{x} + N_{0}\right]}_{\triangleq h}, \tag{33}$$

Algorithm 1 - BBI-Based JCTDD Algorithm for Time-Varying mmWave MIMO Systems

Input:
$$\{y[k], \forall k\}$$
, $H[0]$, $\{A_{\ell,c}, \forall (\ell,c)\}$, r , N_0 , W , D , G , t_{\max}

Output: $\{\check{x}_m[k], \forall (k,m)\}, \{\check{H}[k], \forall k\}$

- 1: Obtain using Eq. (14) \mathcal{K}_{τ} , and generate \mathcal{K}_{τ}^{+} and $\check{\mathcal{K}}_{\tau}$
- 2: Obtain using Eq. (29) $S_{k,\tau}$

- 2: Obtain using Eq. (29) $\delta_{k,\tau}$ 3: $\forall (k,m,n)$: $\hat{x}_{mk} \leftarrow 0$ and $\psi_{mk}^{\mathsf{x}} \leftarrow 1$ 4: $\forall (m,n)$: $\theta_{nm} \leftarrow \frac{1}{L} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{|[\mathbf{A}_{\ell,c}]_{n,m}|^{2}}{C_{\ell}}$ 5: $\forall (k,m,n)$: $\omega_{k,nm} \leftarrow (1-r^{2k})\theta_{n,m}$ 6: $\forall m$: $\boldsymbol{\Theta}_{m} \leftarrow \frac{1}{L} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{[\mathbf{A}_{\ell,c}]_{:,m}[\mathbf{A}_{\ell,c}]_{:,m}^{\mathsf{H}}}{C_{\ell}}$ 7: $\forall (k,m)$: $\boldsymbol{\Omega}_{k,m} \leftarrow (1-r^{2k})\boldsymbol{\Theta}_{m}$ 8: $\forall k$: $\boldsymbol{\Omega}_{k} \leftarrow \sum_{m=1}^{M} \boldsymbol{\Omega}_{k,m}$ /* Estimation */
- 9: for $\tau = 1, \dots, \tau_{max}$
- 10: Executing Algorithm 2 CP Phase
- 11: Executing Algorithm 3 JCDE Phase
- 12: end for

13:
$$\forall (k,m): \check{x}_m[k] \leftarrow \underset{\chi \in \mathcal{X}}{\operatorname{argmin}} \left| \chi - \hat{x}_{mk} \right|$$

14: $\forall k$: $\dot{\boldsymbol{H}}[k] \leftarrow \hat{\boldsymbol{H}}_k$

Algorithm 2 - CP Phase

$$\begin{aligned} &\textbf{Input:} \ \{ \boldsymbol{\Omega}_k, \forall k \}, \ \{ \boldsymbol{\Omega}_{k,m}, \forall (k,m) \}, \ \{ \omega_{k,nm}, \forall (k,m,n) \}, \\ & \left\{ \hat{\boldsymbol{\psi}}_{k,nm}^{\text{h}}, \forall (k \in \mathcal{K}_{\tau}, m, n) \right\} \\ &\textbf{Output:} \ \left\{ \hat{\boldsymbol{H}}_k, \hat{\boldsymbol{\Psi}}_k^{\text{h}}, \forall k \in \mathcal{K}_{\tau} \right\}, \ \left\{ \hat{\boldsymbol{\Psi}}_{k,m}^{\text{h}}, \forall (k \in \mathcal{K}_{\tau}, m) \right\}, \\ & \left\{ \hat{\boldsymbol{\psi}}_{k,nm}^{\text{h}}, \forall (k \in \mathcal{K}_{\tau}, m, n) \right\} \end{aligned}$$

- 1: if $\tau = 1$ then
- 2: $\forall (k \in \mathcal{K}_{\tau})$: $\hat{\boldsymbol{H}}_{k} \leftarrow r^{k}\boldsymbol{H}[0]$ and $\hat{\boldsymbol{\Psi}}_{k}^{h} \leftarrow \boldsymbol{\Omega}_{k}$ 3: $\forall (k \in \mathcal{K}_{\tau}, m)$: $\hat{\boldsymbol{\Psi}}_{k,m}^{h} \leftarrow \boldsymbol{\Omega}_{k,m}$
- 4: $\forall (k \in \mathcal{K}_{\tau}, m, n) : \hat{\psi}_{k,nm}^{h} \leftarrow \omega_{k,nm}$
- 6: $k_{\tau} \leftarrow \underset{\underline{k} \in \mathcal{K}_{\tau} \setminus \mathcal{K}_{\tau}^{+}}{\operatorname{argmin}} \sum_{n=1}^{N} \sum_{m=1}^{M} \hat{\psi}_{\underline{k},nm}^{h}$, and generate $\mathcal{K}_{\tau}^{>k_{\tau}}$
- 7: $\forall (k \in \mathcal{K}_{\tau}^{>k_{\tau}})$: $\hat{\boldsymbol{H}}_{k} \leftarrow r^{k-k_{\tau}} \hat{\boldsymbol{H}}_{k_{\tau}}$ and $\hat{\boldsymbol{\Psi}}_{k}^{h} \leftarrow r^{2(k-k_{\tau})} \hat{\boldsymbol{\Psi}}_{k_{\tau}}^{h} + \boldsymbol{\Omega}_{k-k_{\tau}}$ 8: $\forall (k \in \mathcal{K}_{\tau}^{>k_{\tau}}, m)$: $\hat{\boldsymbol{\Psi}}_{k,m}^{h} \leftarrow r^{2(k-k_{\tau})} \hat{\boldsymbol{\Psi}}_{k_{\tau},m}^{h} + \boldsymbol{\Omega}_{k-k_{\tau},m}$ 9: $\forall (k \in \mathcal{K}_{\tau}^{>k_{\tau}}, m, n)$: $\hat{\boldsymbol{\psi}}_{k,nm}^{h} \leftarrow r^{2(k-k_{\tau})} \hat{\boldsymbol{\psi}}_{k_{\tau},m}^{h} + \omega_{k-k_{\tau},nm}$

- 10: end if

MSE $\hat{\psi}_{mk}^{x}$, $\forall (k \in \mathcal{K}_{p}, m)$, where \mathcal{K}_{p} is the set of discrete-time indices in which the pilot symbols are embedded, the proposed method achieves Bayesian-optimal inference with the pilot symbols as addition prior information.

It shall be shown in the sequel, however, that the proposed method is already effective in estimating time-varying channels with high accuracy without the addition of pilot signals.

Algorithm 3 - JCDE Phase

$$\begin{split} & \textbf{Input:} \quad \{ \boldsymbol{y}[k], k \in \mathcal{K}_{\tau} \}, \quad N_0, \quad t_{\max}, \quad \{ \boldsymbol{\theta}_{n,m}, \forall (m,n) \}, \\ & \left\{ \hat{x}_{mk}, \hat{\psi}_{mk}^{\mathbf{x}}, \forall (k \in \mathcal{K}_{\tau}, m) \right\}, \qquad \left\{ \hat{\boldsymbol{H}}_{k}, \hat{\boldsymbol{\Psi}}_{k}^{\mathbf{h}}, \forall k \in \mathcal{K}_{\tau} \right\}, \\ & \left\{ \hat{\boldsymbol{\Psi}}_{k,m}^{\mathbf{h}}, \forall (k \in \mathcal{K}_{\tau}, m) \right\}, \quad \left\{ \hat{\psi}_{k,nm}^{\mathbf{h}}, \forall (k \in \mathcal{K}_{\tau}, m, n) \right\} \\ & \textbf{Output:} \quad \{ \hat{x}_{mk}, \forall (k \in \mathcal{K}_{\tau}, m) \}, \quad \left\{ \hat{\boldsymbol{H}}_{k}, \forall k \in \mathcal{K}_{\tau} \right\} \end{split}$$

/* — JCDE Phase for DD: $\forall k \in \mathcal{K}_{\tau}$

- 1: **for** $t = 1, ..., t_{max}$
- 2: $\boldsymbol{\Xi}_k \leftarrow \sum_{m=1}^{M} \hat{\psi}_{mk}^{\mathbf{x}} \hat{\boldsymbol{h}}_{k,m} \hat{\boldsymbol{h}}_{k,m}^{\mathsf{H}} + \hat{\boldsymbol{\varPsi}}_k^{\mathbf{h}} + N_0 \boldsymbol{I}_N$

- $\hat{x}'_{mk} \leftarrow \frac{1}{\sqrt{2}} \cdot \left(\tanh \left[\frac{\sqrt{2} \Re\{\overline{x}_{mk}\}}{\overline{\psi}_{mk}^{\mathsf{X}}} \right] + \mathrm{j} \tanh \left[\frac{\sqrt{2} \Im\{\overline{x}_{mk}\}}{\overline{\psi}_{mk}^{\mathsf{X}}} \right] \right)$
- and $\hat{\psi}_{mk}^{\prime \mathbf{x}} \leftarrow 1 |\hat{x}_{mk}|^2$ 7: $\forall m$: $\hat{x}_{mk} \leftarrow \alpha \hat{x}_{mk}^{\prime} + (1 \alpha)\hat{x}_{mk}$ and $\hat{\psi}_{mk}^{\mathbf{x}} \leftarrow \alpha \hat{\psi}_{mk}^{\prime \mathbf{x}} + (1 \alpha)\hat{\psi}_{mk}^{\mathbf{x}}$ $/* \qquad \qquad \mathbf{JCDE \ Phase \ for \ CE:} \ \forall k \in \mathcal{K}_{\tau}$ 8: $\forall (m,n)$: $\tilde{y}_{k,nm} \leftarrow y_{nk} \sum_{i \neq m}^{M} \hat{h}_{k,ni} \hat{x}_{ik}$
- 9: $\forall (m,n): \nu_{k,nm}^{h} \leftarrow \sum_{i \neq m}^{M} \left\{ \left| \hat{h}_{k,ni} \right|^{2} \hat{\psi}_{ik}^{x} \right\} \right\}$ $+\left(\left|\hat{x}_{ik}\right|^{2}+\hat{\psi}_{ik}^{x}\right)\hat{\psi}_{k,ni}^{h}\right\}+\theta_{nm}\hat{\psi}_{mk}^{x}+N_{0}$
- 10: if $k > s \in \mathcal{S}_{\tau,k}$ then
- 11: $\forall (s \in \mathcal{S}_{\tau,k}, m, n): \quad \nu_{s \to k, nm}^{\text{h}} \leftarrow \omega_{k-s, nm} |\hat{x}_{ms}|^2 +$ $r^{2(k-s)}\nu_{s,nm}^{\mathrm{h}}$
- 12: else if $k < s \in \mathcal{S}_{\tau,k}$ then
- 13: $\forall (s \in \mathcal{S}_{\tau,k}, m, n)$:

$$\nu_{s \to k, nm}^{\text{h}} \leftarrow r^{2(k-s)} \left(\omega_{s-k, nm} \left| \hat{x}_{ms} \right|^2 + \nu_{s, nm}^{\text{h}} \right)$$

- 15: **if** $t = t_{\text{max}}$ **then**
- 16: $\forall (m,n)$: $\overline{h}_{k,nm} \leftarrow \overline{\psi}_{k,nm}^{\text{h}} \sum_{s \in \mathcal{S}_{k,\tau} \cup \{k\}} \frac{\hat{x}_{mi}^* r^{k-s} \tilde{y}_{s,nm}}{\nu_{s \to k,nm}^{\text{h}}}$ and $\overline{\psi}_{k,nm}^{\text{h}} \leftarrow \left(\sum_{s \in \mathcal{S}_{k,\tau} \cup \{k\}} \frac{|\hat{x}_{ms}|^2}{\nu^{\text{h}}}\right)$
- 17: **else if**
- 17: **else if**18: $\forall (m,n) \colon \overline{h}_{k,nm} \leftarrow \overline{\psi}_{k,nm}^{\mathrm{h}} \sum_{s \in \mathcal{S}_{k,\tau}} \frac{\hat{x}_{mi}^* r^{k-s} \tilde{y}_{s,nm}}{\nu_{s \to k,nm}^{\mathrm{h}}} \text{ and }$ $\overline{\psi}_{k,nm}^{\mathrm{h}} \leftarrow \left(\sum_{s \in \mathcal{S}_{k,\tau}} \frac{|\hat{x}_{ms}|^2}{\nu_{s \to k,nm}^{\mathrm{h}}}\right)^{-1}$
- 19: **end if**
- 20: $\forall m$: $\overline{\boldsymbol{h}}_{k,m} \leftarrow \left[\overline{h}_{k,1m}, \dots, \overline{h}_{k,Nm}\right]^{\mathsf{T}}$ and $\overline{\boldsymbol{\varPsi}}_{k,m}^{\mathsf{h}} \leftarrow \operatorname{diag}\left[\overline{\psi}_{k,1m}^{\mathsf{h}}, \dots, \overline{\psi}_{k,Nm}^{\mathsf{h}}\right]$
- 21: $\forall m: \boldsymbol{\Lambda}_{k,m} \leftarrow \boldsymbol{\Omega}_{k,m} + \overline{\boldsymbol{\varPsi}}_{k,m}^{\mathrm{h}}$
- 22: $\forall m$: $\hat{\boldsymbol{h}}_{k,m}' \leftarrow \boldsymbol{\Omega}_{k,m} \boldsymbol{\Lambda}_{k,m}^{-1} \overline{\boldsymbol{h}}_{k,m} + r^k \overline{\boldsymbol{\Psi}}_{k,m}^{\mathrm{h}} \boldsymbol{\Lambda}_{k,m}^{-1} \boldsymbol{h}_m[0]$ and $\hat{oldsymbol{ec{\Psi}}}_{k,m}^{'\mathrm{h}} \leftarrow oldsymbol{\Omega}_{k,m} oldsymbol{ec{\Lambda}}_{k,m}^{-1} \overline{oldsymbol{ec{\Psi}}}_{k,m}^{\mathrm{h}}$
- 23: $\forall m: \hat{\boldsymbol{h}}_{k,m} \leftarrow \alpha \hat{\boldsymbol{h}}'_{k,m} + (1-\alpha)\hat{\boldsymbol{h}}_{k,m} \text{ and } \hat{\boldsymbol{\Psi}}^{\mathrm{h}}_{k,m} \leftarrow \alpha \hat{\boldsymbol{\Psi}}'^{\mathrm{h}}_{k,m} + (1-\alpha)\hat{\boldsymbol{\Psi}}^{\mathrm{h}}_{k,m}$
- **24: end for**

D. Remarks on Complexity

In this subsection, let us offer a brief analysis of the computational complexities of the algorithms presented in the previous subsection. Starting with the CP phase presented

TABLE III
TIME-VARYING CHANNEL PARAMETERS BASED
ON THE SPECIFICATION OF [45]

Relative speed v [kmph]	Coherence time $T_{\rm c}$ [ms]	Time correlation parameter r
15	0.507248838936000	0.999668722580203
30	0.253624419468000	0.999337554905135
45	0.169082946312000	0.999006022041674
60	0.126812209734000	0.998675548643774

in Algorithm 2, the main operations are matrix and scalar multiplications, their additions, and search over W(D-1) elements. With the relationship $|\mathcal{K}_{\tau}^{>k_{\tau}}| < |\mathcal{K}_{\tau}| \leq WD$, the associated complexity is governed by line 8 in Algorithm 2, which is bounded on the order of $\mathcal{O}(N^2MWD)$.

Next, in the JCDE phase presented in Algorithm 3, the complexity of DD part is dominated by the inverse operation of $N \times N$ matrix Ξ_k and matrix and vector multiplications in line 3, which is bounded by the order of $\mathcal{O}((N^3+N^2M)WD)$. On the other hand, the complexity of CE part is dominated by M times inverse operation of $N \times N$ matrix $\Lambda_{k,m}, \forall m$, and matrix multiplications in line 22, which is bounded on the order of $\mathcal{O}(N^3MWD)$. Other operations in the JCDE phase consist of only scalar-by-scalar calculations, whose number of four arithmetic operations is proportional to NM, as shown in [33]. In addition, the computations for the soft replica from the hyperbolic tangent function in line 6 can be handled through a look-up table, which is in order of $\mathcal{O}(MWD)$. Thus, considering the maximum number of iterations t_{max} , the computational complexity of one JCDE phase is in order of $\mathcal{O}(t_{\text{max}}N^3MWD)$.

It follows from the above that the complexity of Algorithms 1-3 is dominated by the JCDE phase, which is bounded on the order of $\mathcal{O}(t_{\text{max}}N^3MWD)$ per step. Since the number of steps is given by $\tau_{\text{max}} = \frac{K}{W} + D - 1$, the overall computational complexity required to estimate all MK TX symbols, i.e., $\check{x}_m[k], \forall (k,m)$, is in order of $\mathcal{O}((t_{\text{max}}D)\cdot N^3MK)$. This complexity is one exponent larger in the RX dimension N than that of the SotA Bayesian DD algorithm represented by expectation propagation (EP) [53] and may seem very large since it is proportional to the cube of N of the effective beam-domain channel H[k]. Note, however, that most of the spatial DoF are used to form pencil beams, and therefore the effective beam-domain channel matrix size $N \times M$ is much smaller than the physical array size $N_{\rm RX} \times N_{\rm TX}$. If N is set larger than the number of major singular values of a channel matrix, i.e., larger than the number of effective clusters L, substantially all available spatial DoF can be used without energy loss, with little loss of accuracy in subsequent processing. Since in an actual mmWave wireless communication channel L rarely exceeds 4 [1], N can be set sufficiently small while maintaining detection performance.

IV. PERFORMANCE ASSESSMENT

Computer simulations were conducted to validate the performance of the proposed receiver under various system conditions. The basic system format was set to follow [45],

in which the carrier frequency was set to $f_c=60$ [GHz], the DFT size was set to $N_{\rm DFT}=512$, the guard interval was assumed to be a quarter of each OFDM symbol length, and the OFDM sampling rate was set to $f_{\rm s}=2.64$ [GHz]. The mmWave wireless communication channels considered consist of L=4 clusters with $C_\ell=15$ rays-per-cluster and varied the relative speed between the transmitter and receiver within the range of [15,60] [kmph], which is commonly used in low-speed urban scenarios of vehicle-to-everything (V2X) communication systems [15], [16].⁶ Table III illustrates the values of each parameter at different relative speeds v. The evaluation at different relative speeds corresponds to verifying the detection performance of the proposed method in problem settings of different r, i.e., different difficulty levels.

Simulated results are offered both in terms of BER and NMSE, averaged over 10000 different time-varying channel realizations; the number of TX/RX antennas, that of RX/TX dimensions of $\boldsymbol{H}[k]$, and that of OFDM symbols assumed to be $N_{\rm TX}=4$, $N_{\rm RX}=16$, M=2, N=8, and K=128, respectively, unless otherwise specified. The damping factor was set to $\alpha=0.5$.

A. Effects of Parameters on Performance and Convergence

Before proceeding to the presentation of performance comparison, we analyze how the internal parameters embedded in the proposed algorithm affect its performance and convergence. In the following, the parameters are set to (W,D,G)=(8,3,6), $t_{\rm max}=8$, and then each parameter is varied one by one to see how the performance changes with v=60 kmph.

Fig. 2 shows the BER performance of the proposed JCTDD algorithm as a function of each parameter at different $E_{\rm s}/N_0$. W is inversely proportional to the number of steps in sequential processing $\tau_{\rm max}$; hence, the smaller W is, the more the sequential processing strategy slides the *estimation window* little by little, which improves CT performance, but at the same time increases processing delay. Fig. 2a shows that the performance degrades as W increases, and by setting W=8, sufficient detection performance can be achieved with as few steps as possible.

Next, D is the parameter that determines the number of variables estimated simultaneously for each step; hence, the complexity is proportional to D. Fig. 2b shows that the performance improvement is almost saturated at D=2; hence, it is not necessary to set the value greater than 3. This fact indicates that the approximation in (19a) holds true with high accuracy as a result of the sequential process operating properly based on the Bayesian inference framework.

Next, G is the number of beliefs to be combined in VNs for CE. The larger G, the greater the number of resources used for belief combining in the discrete time dimension, which

⁶In this simulation, we focus on high-mobility mmWave MIMO communication scenarios with speeds in the order of tens of kilometers per hour, which are expected in vehicle-to-vehicle (V2V) communications, vehicle-to-infrastructure (V2I) communications, as well as communications with vulnerable road users (VRUs) [54].

Note, however, that the discussion and the proposed method in this article are not restricted to any particular V2X scenario. The purpose of this simulation is to verify to what level of time variability CT can be performed by evaluating the proposed algorithm for different values of r.

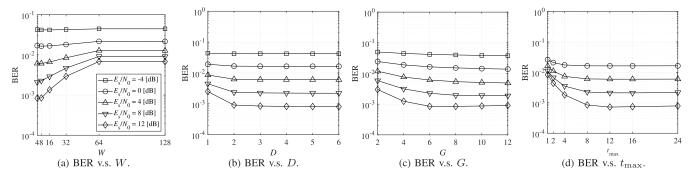


Fig. 2. BER performance of time-varying mmWave MIMO systems with respect to internal parameters (W, D, G) and t_{max} .

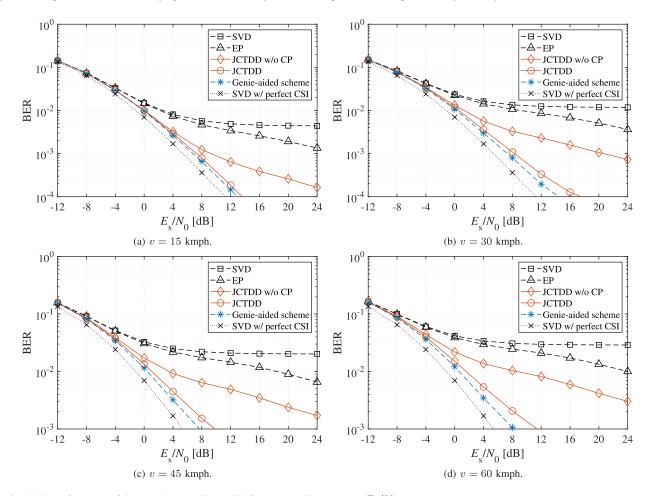


Fig. 3. BER performance of time-varying mmWave MIMO systems with respect to $E_{\rm s}/N_0$.

increases the diversity gain, but at the same time, the adverse effect of errors due to channel aging increases. As expected, Fig. 2c shows that the performance improvement saturates around G=6 to 8, with a slight performance degradation at higher settings, especially in the high $E_{\rm s}/N_0$ region.

Finally, it can be seen in Fig. 2d that the performance improvement saturates around $t_{\rm max}=8$ to 12. The convergence of iterative estimation is observed in the low $E_{\rm s}/N_0$ region with fewer iterations than in the high $E_{\rm s}/N_0$ region, indicating that detection performance can be maximized with fewer iterations, especially in the coding system.

Based on the above results, we will use (W, D, G) = (8, 3, 6), $t_{\rm max} = 8$ in the following evaluation. The results below show that these parameters are not sensitive to various system setups, but at the choice of the system designer, further fine optimization is also possible.

B. BER Performance

Our first set of results is given in Fig. 3, where the BER performances as a function of the $E_{\rm s}/N_0$ and for different relative velocities (i.e., $v \in \{15, 30, 45, 60\}$) of the following mmWave MIMO systems are compared:

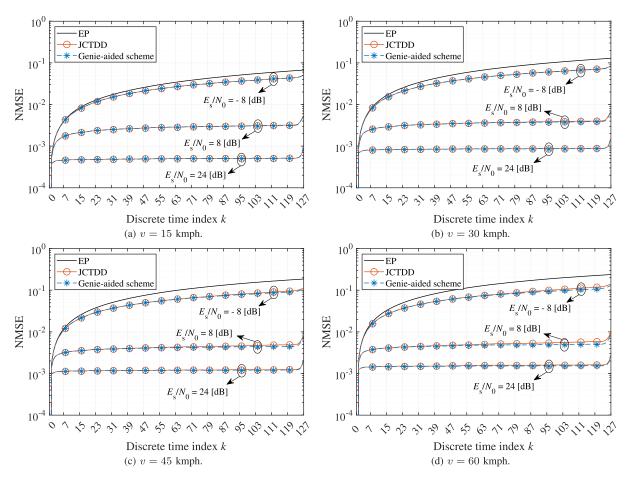


Fig. 4. NMSE performance of time-varying mmWave MIMO systems with respect to discrete time index k.

- *SVD*: Baseline TX/RX beamforming design via SVD of $\acute{H}[0] = U\Sigma V^{\mathsf{H}}$, *i.e.*, $F_{\mathsf{TX}} = [V]_{:,1:M}$ and $F_{\mathsf{RX}} = [U]_{:,1:M}$, as described in Subsection II-C.
- *EP*: SotA Bayesian receiver adopting the EP-based DD algorithm [53], providing a reference performance to verify the gain achieved by the channel aging-aware JCTDD algorithm since it can achieve Bayesian optimal DD utilizing exactly the same prior knowledge as the proposed method. The number of iterations is set to 16.
- JCTDD w/o CP: Proposed JCTDD receiver with (W,D,G)=(K,1,6), where the JCDE phase is applied simultaneously to K OFDM symbols without sequential processing via the CP phase. Provides a reference performance to verify the gain achieved by the CP-aided window-sliding strategy for tracking the time variability of channels.
- *JCTDD*: Proposed JCTDD receiver with (W, D, G) = (8, 3, 6) presented in Algorithms 1-3.
- Genie-aided scheme: Idealized scheme in which perfect knowledge of x[k], ∀k, is provided as prior information at the first iteration of the JCDE phase. Provides an absolute lower bound in terms of the NMSE performance of CE.
- SVD w/ perfect CSI: Baseline TX/RX beamforming design via SVD of $\hat{\boldsymbol{H}}[k] = \boldsymbol{U}_k \boldsymbol{\Sigma}_k \boldsymbol{V}_k^\mathsf{H}, \ \forall k, \ i.e.,$ $\boldsymbol{F}_{\mathrm{TX}}[k] = [\boldsymbol{V}_k]_{:,1:M}$ and $\boldsymbol{F}_{\mathrm{RX}}[k] = [\boldsymbol{U}_k]_{:,1:M}$. Provides a reference lower bound, which can only

be achieved in the absence of channel aging, *i.e.*, v = 0 kmph.

As can be seen from Fig. 3, the SotA methods, *i.e.*, SVD and EP, suffer from high error floors, which stem from the poor CE accuracy, caused by the channel aging. Even in the EP detector, which exploits the long-term channel statistics to suppress the channel aging interference, serious performance degradation is inevitable as v increases. In contrast, "JCTDD w/o CP" can improve the CE accuracy by taking advantage of the estimated data symbols as effective soft pilots, thus significantly outperforming the SotA. However, the slope of the BER curve remains gradual as in the case of EP and deviates from that of the ideal Genie-aided reference.

In comparison to the latter method, the proposed "JCTDD" method exhibits an error-floor free water-fall BER curve, approaching that of the ideal Genie-aided reference, without any additional pilots, *i.e.*, without any change in the transmission frame format. Sequential processing via the CP phase enables highly accurate CT by generating the reliable prior estimates input to the JCDE phase, reducing the degradation from the Genie-aided reference with BER = 10^{-3} to about 0.5 dB, 1.0 dB, 2.0 dB, and 3.5 dB in Figs. 3a–3d, respectively.

C. MSE Performance

Next, we evaluate the CE performance of the proposed method, in terms of the NMSE of the channel estimates at

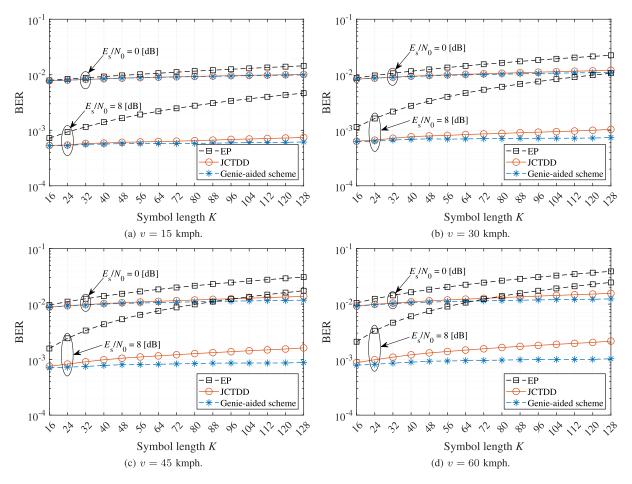


Fig. 5. BER performance of time-varying mmWave MIMO systems with respect to symbol length K.

each discrete time $k \in \mathcal{K}$, where the $E_{\rm s}/N_0$ is fixed at -8 dB, 8 dB, and 24 dB, respectively. In view of Fig. 3, results for "SVD" and "JCTDD w/o CP" are omitted as they have shown to perform poorly, while the Genie-aided scheme has already provided a lower-bounding reference. In "EP," the channel estimate at the k-th discrete time is given by $\check{\boldsymbol{H}}[k] = r^k \boldsymbol{H}[0]$ according to the transition model in (12), which provides a lower bound without the channel tracking (CT) mechanism. With that clarified, the NMSE performances of the remaining three algorithms with the same settings as in Fig. 3 are compared in Fig. 4.

As expected, it is found that the NMSE performances of "EP" deteriorate significantly with increasing $k,\ i.e.$, over time, due to channel aging. In contrast, the proposed method asymptotically approaches the Genie-aided scheme, and only slight deviations from the reference are observed even under the high-mobility communication scenarios in Figs. 4c and 4d. Furthermore, in higher $E_{\rm s}/N_0$ regime, i.e., at 8 dB and 24 dB, NMSEs are almost constant with respect to k, confirming that highly accurate CT can be achieved⁷.

D. Insight on Error Propagation in Channel Tracking

To gain insight into the harmful effect of error propagation in the proposed method, the BER performance as a function of the symbol length K with $E_{\rm s}/N_0=0$ dB and 8 dB are compared in Fig. 5, for the same mobility scenarios of Fig. 4.

As expected from the poor NMSE performance shown in Fig. 4, the performance of "EP" deteriorates rapidly as K increases, even with the DD algorithm to account for the channel aging interference. In contrast, the proposed method achieves significant performance improvement due to its highly accurate CT mechanism. However, particularly in scenarios with large values of v as shown in Figs. 5c and 5d, it is found that the deviation from the performance of the Genie-aided scheme increases with increasing K, albeit quite slowly. This performance degradation can be attributed to the error propagation in sequential processing, and some sort of error correction mechanism must be introduced separately to compensate for it. With that in mind, the following subsections study the effect of inserting additional pilot symbols and using error-correcting codes on system performance, respectively, providing insight into the optimal system configuration.

E. Additional Pilot Insertion

In this subsection, we study the effect of inserting additional pilot symbols. We here define the pilot rate $r_{\rm p}$ as the proportion

 $^{^{7}}$ The increase in NMSE around k=127 is due to the fact that the number of beliefs that contribute to the diversity gain in the belief combining of (39) decreases owing to the unavailability of observations at future times k>127, and this inconvenience can be avoided by properly terminating the process using known control signals in practical systems.

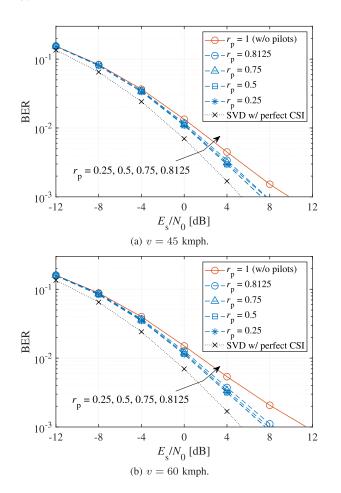


Fig. 6. BER performance of the proposed method with respect to $E_{\rm s}/N_0$.

of data symbols to the symbol length K. That is, when the number of embedded pilot symbols is $K_{\rm p},\,r_{\rm p}\triangleq 1-K_{\rm p}/K$. The $K_{\rm p}$ pilot symbols given by the rows of a $K_{\rm p}\times K_{\rm p}$ DFT matrix are assumed to be placed as evenly spaced as possible to maximize the error correction capability during the iterative estimation process.

Fig. 6 shows the BER performances of the proposed method for different pilot rates, i,e,, $r_p \in \{1, 0.8125, 0.75, 0.5, 0.25\},\$ with the same settings as in Figs. 3c and 3d. From both figures, it can be confirmed that periodically embedded pilot symbols function as a kind of error correction mechanism and suppress error propagation, resulting in improved performance. It is worth noting here that while a small number of pilot symbols provides reasonable performance improvement, excessive piloting (i.e., a lower pilot rate) does not result in corresponding improvement. In fact, the deviation between the performances of $r_{\rm p}=0.8125$ and $r_{\rm p}=0.25$ is less than 1.0 dB at BER = 10^{-3} , and the improvement is almost saturated at $r_{\rm p}=0.75$. This performance is the lower bound that can be achieved by adding pilot symbols, and it can be seen that it is roughly consistent with that of the idealized Genie-aided reference in Fig. 3. These results indicate that in the proposed JCTDD algorithm, the performance gains from adding pilot symbols are limited and that the number of additional pilot symbols, if any, should be small. Furthermore, the existing pilot-based counterparts [20], [21], [22] are unlikely to

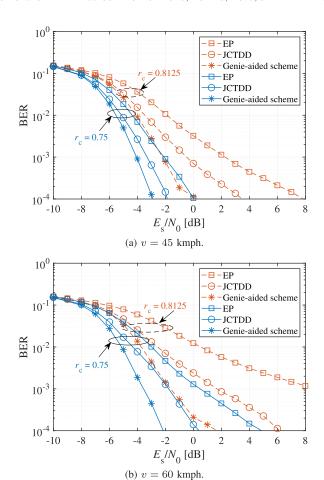


Fig. 7. BER performance of coded mmWave MIMO systems with respect to $E_{\rm s}/N_0$, where the dashed and solid lines indicate performance for $r_{\rm c}=0.8125$ and 0.75, respectively.

achieve performance equal to or better than the saturation performance ($r_{\rm p}=0.25$) since they perform CT/CE based only on reference signaling, suggesting that the proposed algorithm can at least achieve asymptotic performance approaching that of the existing methods, even without an additional piloting ($r_{\rm p}=1$).

F. BER Performance in Coded Systems

Finally, in this subsection we compare the BER performances of coded mmWave MIMO systems adopting the low-density parity-check (LDPC) code with rates $r_{\rm c} \in \{0.8125, 0.75\}$, in alignment with fifth-generation (5G) new radio (NR) specification [55], where the sum-product algorithm (SPA) is employed as the soft-decision decoder. Remarkably, it is found in Fig. 7 that the proposed method exhibits error-floor-free water-fall BER curves in the $E_{\rm s}/N_0$ region observed, despite the relatively high coding rates utilized, namely, $r_{\rm c}=0.8125$ and $r_{\rm c}=0.75$.

However, due to the reduction of the Gaussianity of log-likelihood ratios (LLRs) used as input in the channel decoder, which is caused by interference due to channel aging, a deviation from the ideal Genie-aided reference is also observed, especially at high coding rates, although the gap becomes smaller as $r_{\rm c}$ decreases. Large gains compared to the EP-based

DD method are obtained in all figures, confirming that the proposed method can appropriately benefit from the coding gains from the error correction process.

Comparing the BER performances of the proposed method at a given transmission rate, as shown in Figs. 6 and 7 for $r_{\rm p}=r_{\rm c}=0.75$ and $r_{\rm p}=r_{\rm c}=0.8125$, it can be seen that rather than adding pilot symbols to aid CT, such redundancy is better employed to boost error correction capability via channel coding, which leads to greater performance improvement.

V. CONCLUSION

We proposed a novel BBI-based JCTDD receiver for uplink mmWave MIMO systems with time-varying channels. Taking advantage of the sequential two-step tracking scheme found in the typical KF as the basic framework, new belief generation and belief combining processes were designed by incorporating the AR model, which describes the time variability of wireless channels, into the JCDE algorithm as the state transition model. Under consistent assumptions and approximation accuracy, a new overall belief propagation regime was designed according to the BiGaBP framework, and only the DD mechanism was designed based on the PDA-like approach to account for the spatial correlation among fading coefficients in mmWave wireless channels. Finally, computer simulations were conducted to demonstrate the validity of our proposed method in terms of BER and NMSE performances in various system setups. The results show that the proposed method can continue to track channels with high accuracy without any additional pilots. Furthermore, comparative study with the SotA alternatives and the case studies covering various scenarios provided insight into the optimal system design.

APPENDIX

SECOND-ORDER STATISTICS OF ERRORS DUE TO CHANNEL-AGING PHENOMENON

Based on (12), the covariance matrix of errors due to channel aging can be in general obtained from the conditional expectation of $H[k]H[k]^H$, given H[k-k'] as

 $\Omega_{k'}$

$$\triangleq \mathbb{E}_{\mathbf{H}[k]|\mathbf{H}[k-k']} \left[\mathbf{H}[k]\mathbf{H}[k]^{\mathsf{H}} \middle| \mathbf{H}[k-k'] \right]$$

$$= \mathbb{E} \left[\left(\mathbf{H}[k] - r^{k'}\mathbf{H}[k-k'] \right) \left(\mathbf{H}[k] - r^{k'}\mathbf{H}[k-k'] \right)^{\mathsf{H}} \right]$$

$$= \frac{1 - r^{2k'}}{L} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{\mathbf{A}_{\ell,c} \mathbf{A}_{\ell,c}^{\mathsf{H}}}{C_{\ell}}.$$
(44a)

Similarly, the conditional covariance matrix of channel vector corresponding to each user equipment (UE) can be calculated as

$$\Omega_{k',m} \triangleq \mathbb{E}_{\mathbf{h}_{m}[k]|\mathbf{h}_{m}[k-k']} \left[\mathbf{h}_{m}[k]\mathbf{h}_{m}[k]^{\mathsf{H}} \middle| \mathbf{h}_{m}[k-k'] \right] \\
= \mathbb{E} \left[\left(\mathbf{h}_{m}[k] - r^{k'} \mathbf{h}_{m}[k-k'] \right) \left(\mathbf{h}_{m}[k] - r^{k'} \mathbf{h}_{m}[k-k'] \right)^{\mathsf{H}} \right] \\
= \frac{1 - r^{2k'}}{L} \sum_{k=1}^{L} \sum_{k=1}^{C_{\ell}} \frac{\left[\mathbf{A}_{\ell,c} \right]_{:,m}^{\mathsf{H}} \left[\mathbf{A}_{\ell,c} \right]_{:,m}^{\mathsf{H}}}{C_{\ell}}, \tag{44b}$$

and the conditional element-wise MSE can be calculated as

 $\omega_{k',nm}$

$$\triangleq \mathbb{E}_{\mathsf{h}_{nm}[k]|\mathsf{h}_{nm}[k-k']} \left[|h_{nm}[k]|^2 \left| h_{nm}[k-k'] \right| \right] \\
= \mathbb{E} \left[\left(h_{nm}[k] - r^{k'} h_{nm}[k-k'] \right) \left(h_{nm}[k] - r^{k'} h_{nm}[k-k'] \right)^* \right] \\
= \frac{1 - r^{2k'}}{L} \sum_{l=1}^{L} \sum_{c=1}^{C_{\ell}} \frac{\left| [\mathbf{A}_{\ell,c}]_{n,m} \right|^2}{C_{\ell}}. \tag{44c}$$

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